

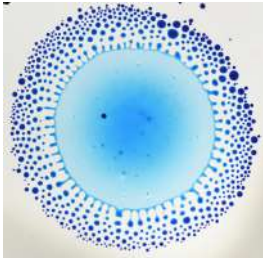
Capillary waves on glass surfaces: from float glass to photonic crystal fibres

Damien Vandembroucq

PMMH, CNRS/ESPCI Paris

Ecole Verre et Optique,
Presqu'île de Giens, 5-10 octobre 2025

Soft matter vs hard glasses



Emulsification of Binary Mixtures on a Liquid Layer

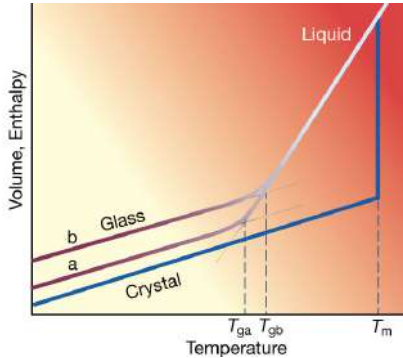
Keyser et al. PRL 2017



Glass ribbon produced with the float glass process

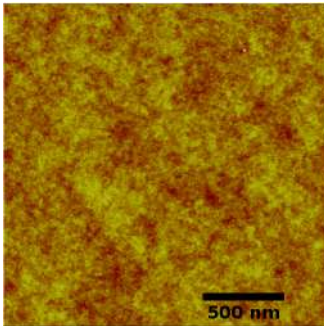
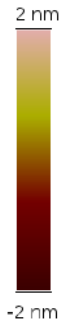
- Coralie Brun, Xavier Buet PMMH, CNRS/ESPCI Paris
- Bruno Bresson, Matteo Ciccotti SIMM, CNRS/ESPCI Paris
- Gilles Tessier, Neurophotonics Lab. Univ. Paris Descartes
- Marco Petrovich, Francesco Poletti, David Richardson, Optoelectronics Research Center, Univ. Southampton
- Thomas Sarlat, Anne Lelarge, Elin Sondergard, CNRS/Saint-Gobain

Basics of glasses

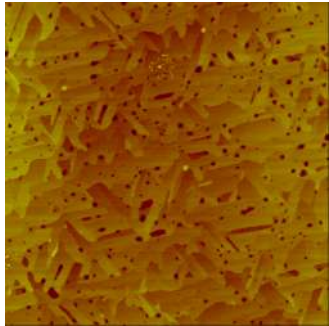


- Glass transition at T_G such that viscosity $\eta \approx 10^{12} \text{Pa.s}$
- Bulk structure $\approx$ snapshot of liquid at T_G

Amorphous vs Crystalline Silica Surface: AFM



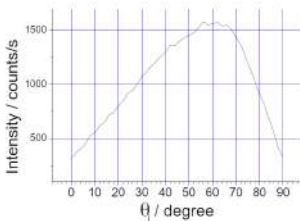
Amorphous silica



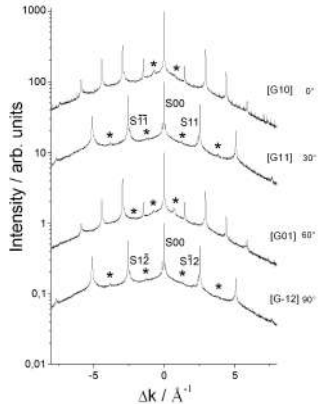
α -SiO₂(0001) quartz

Amorphous vs Crystalline Silica Surface: He scattering

Amorphous silica



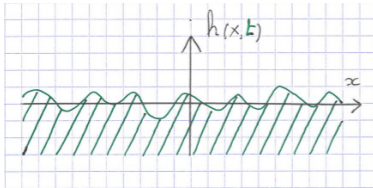
α -SiO₂(0001) quartz



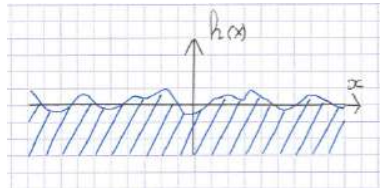
Steurer et al. Surface Sci. (2007)

What is a glass surface ?

Naive answer: a liquid surface that crossed glass transition



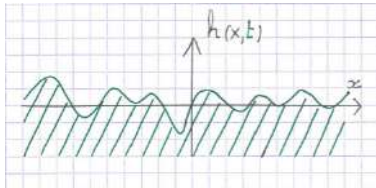
Liquid interface



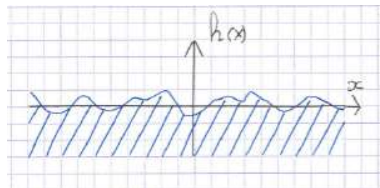
Glass interface

What is a glass surface ?

Naive answer: a liquid surface that crossed glass transition



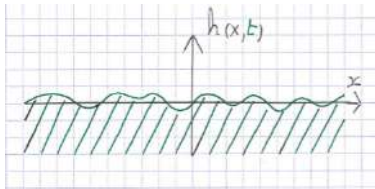
Liquid interface



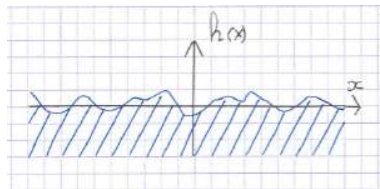
Glass interface

What is a glass surface ?

Naive answer: a liquid surface that crossed glass transition



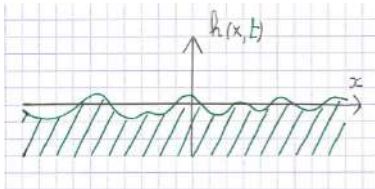
Liquid interface



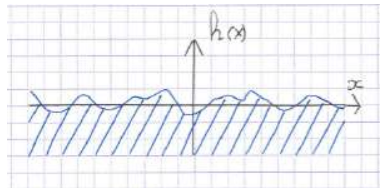
Glass interface

What is a glass surface ?

Naive answer: a liquid surface that crossed glass transition



Liquid interface



Glass interface

Liquid surface: spectrum of capillary waves

Thermal noise kT vs interface tension γ : capillary waves

Interface width $w = \sqrt{\frac{kT}{\gamma}}$, capillary length $\ell_c = \sqrt{\frac{\gamma}{\Delta\rho \cdot g}}$

$$\begin{aligned}\tilde{h}_{\mathbf{q}} &= \int_{\mathcal{S}} d\mathbf{r} h(\mathbf{r}) e^{-i\mathbf{q} \cdot \mathbf{r}} \\ h(\mathbf{r}) &= \frac{1}{S_0} \sum_{\mathbf{q}} \tilde{h}_{\mathbf{q}} e^{i\mathbf{q} \cdot \mathbf{r}}\end{aligned}$$

2D static structure factor: $S_0(\mathbf{q}) \approx S_0 \frac{kT}{\gamma q^2}$, $q \gg \frac{2\pi}{\ell_c}$

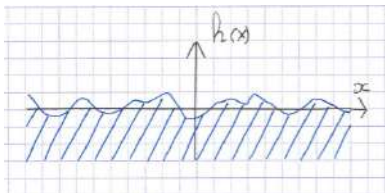
1D height power spectrum: $P(f) \approx \frac{kT}{2\pi\gamma f}$, $f \gg \frac{1}{\ell_c}$

Spatial correlation: $\langle |\Delta h(\Delta r)|^2 \rangle_r \approx \frac{kT}{\pi\gamma} \log\left(\frac{\Delta r}{\ell_{\min}}\right)$, $\Delta r \ll \ell_c$

Glass surface: spectrum of frozen capillary waves?

Thermal noise kT vs interface tension γ : capillary waves

Interface width $w = \sqrt{\frac{kT_G}{\gamma}}$, capillary length $\ell_c = \sqrt{\frac{\gamma}{\Delta\rho \cdot g}}$



$$\tilde{h}_{\mathbf{q}} = \int_{\mathcal{S}} d\mathbf{r} h(\mathbf{r}) e^{-i\mathbf{q} \cdot \mathbf{r}}$$
$$h(\mathbf{r}) = \frac{1}{S_0} \sum_{\mathbf{q}} \tilde{h}_{\mathbf{q}} e^{i\mathbf{q} \cdot \mathbf{r}}$$

2D static structure factor: $S_0(\mathbf{q}) \approx S_0 \frac{kT_G}{\gamma q^2}$, $q \gg \frac{2\pi}{\ell_c}$

1D height power spectrum: $P(f) \approx \frac{kT_G}{2\pi\gamma f}$, $f \gg \frac{1}{\ell_c}$

Spatial correlation: $\langle |\Delta h(\Delta r)|^2 \rangle_r \approx \frac{kT_G}{\pi\gamma} \log\left(\frac{\Delta r}{\ell_{min}}\right)$, $\Delta r \ll \ell_c$

Can we observe capillary waves ?

	water	molten glass
γ	0.07 J.m^{-2}	$0.3\text{-}0.5 \text{ J.m}^{-2}$
η	10^{-3} Pa.s	$10^3 - 10^{13} \text{ Pa.s}$
T	300 K	$900 - 1500 \text{ K}$
ℓ_c	3 mm	$3 - 5 \text{ mm}$
τ_c	10^{-4} s	$10^1 - 10^{10} \text{ s}$
w	0.25 nm	$0.2 - 0.3 \text{ nm}$

A difficult task: interface fluctuations are sub-nanometer!

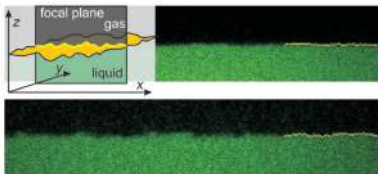
Direct observation in near-critical mixtures

	water	colloidal liquid	molten glass
γ	0.07 J.m^{-2}	$10^{-9} - 10^{-6} \text{ J.m}^{-2}$	$0.3-0.5 \text{ J.m}^{-2}$
η	10^{-3} Pa.s	10^{-3} Pa.s	$10^3 - 10^{13} \text{ Pa.s}$
T	300 K	300 K	900 – 1500 K
ℓ_c	3 mm	$10^{-3} - 10^{-2} \text{ mm}$	3 – 5 mm
τ_c	10^{-4} s	1 – 10s	$10^1 - 10^{10} \text{ s}$
w	0.25 nm	0.05 – 2 μm	0.2 – 0.3 nm

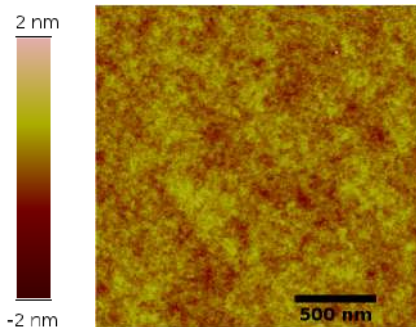
Direct Visual Observation of Thermal Capillary Waves

Dirk G. A. L. Aarts,^{1*} Matthias Schmidt,^{2†}
Henk N. W. Lekkerkerker¹

www.sciencemag.org SCIENCE VOL 304 7 MAY 2004



AFM measurements on an amorphous silica surface



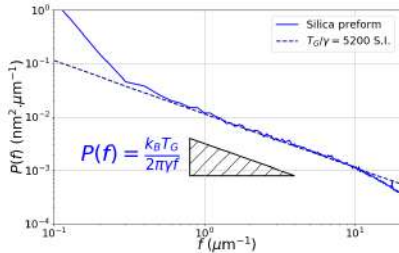
- $T_G \approx 1500 \text{ K}$
- $\gamma \approx 0.3 \text{ J.m}^{-2}$
- molecular length
 $\ell_{\min} \approx 0.3 \text{ nm}$
- capillary length
 $\ell_c \approx 4 \text{ mm}$

AFM measurements consistent with the expected roughness:

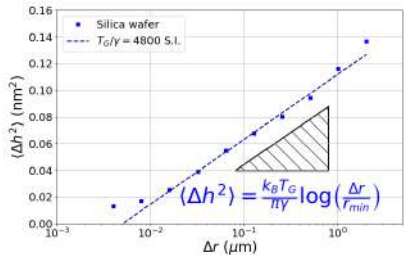
$$w_G = \frac{kT_G}{2\pi\gamma} \log \frac{\ell_c}{\ell_{\min}} \approx 0.4 \text{ nm}$$

Glass roughness: freezing of capillary waves at T_G ?

1D power spectrum



Spatial correlations

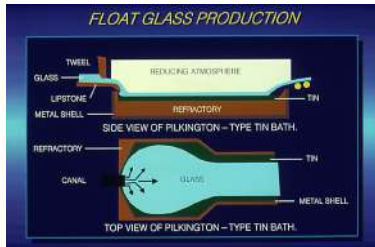


$$T_G \approx 1500 \text{ K}, \gamma \approx 0.3 \text{ J} \cdot \text{m}^{-1}, T_G/\gamma \approx 5000 \text{ S.I.}$$

Glass surface roughness achieves a lower bound:
a thermodynamical noise frozen at T_G !

T. Sarlat, A. Lelarge, E. Sondergard, DV, EPJB, **54**, 121 (2006)

An industrial test case: the float process



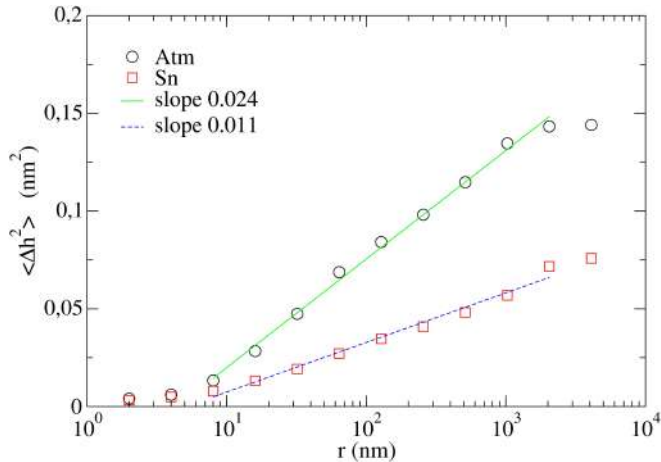
The ribbon of molten glass is cooled down on a liquid tin bath

Two contrasting interfaces:

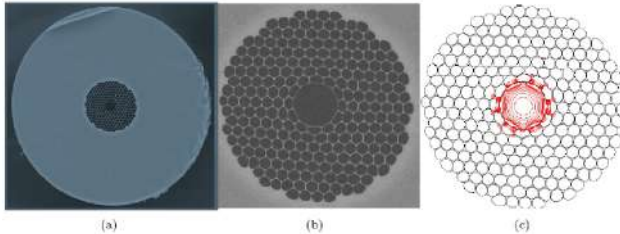
Glass/Gas: $\gamma \approx 0.3 \text{ J.m}^{-2}$

Glass/Tin: $\gamma \approx 0.5 \text{ J.m}^{-2}$

Frozen capillary waves on a float glass surface

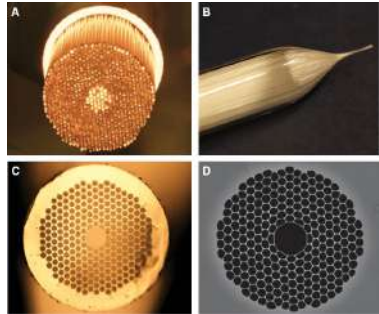
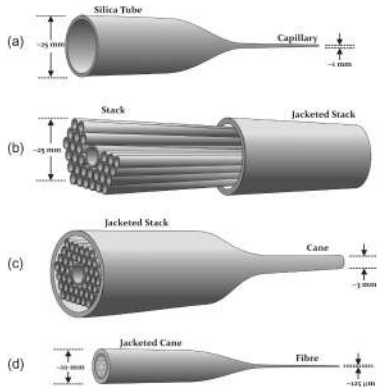


Photonic band-gap fibres

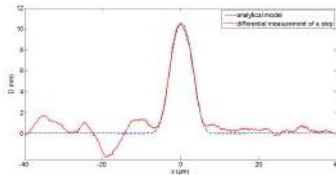
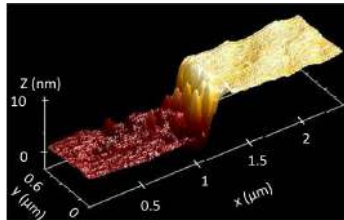
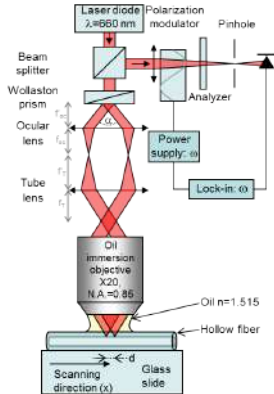


Micro-structured optical fibre : photonic crystal + hollow core
Propagation of light through air instead of glass

Stack and draw process

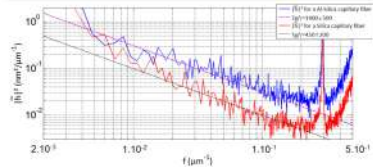
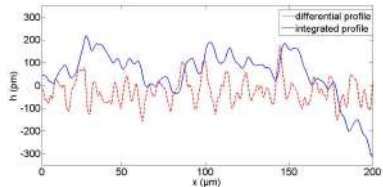
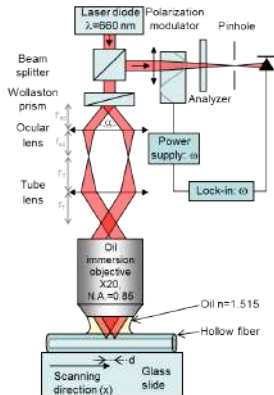


Picometer-scale roughness Measurements by differential optical profilometry



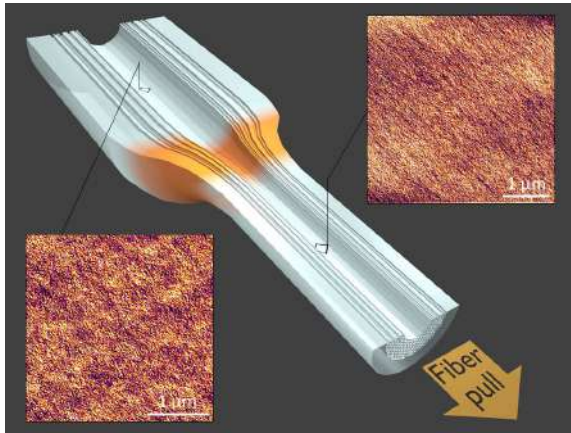
C. Brun et al., Optics Exp. **22** 29554 (2014)

Roughness Measurements of inner surface of silica tubes



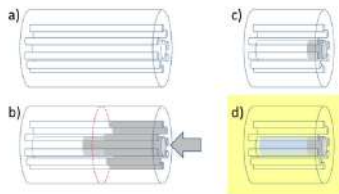
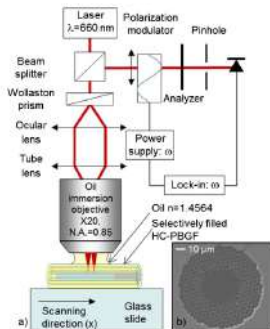
C. Brun et al., Optics Exp. 22 29554 (2014)

Roughness Measurements within Photonic fibres



B. Bresson et al, Phys. Rev. Lett. **119** 235501, (2017)

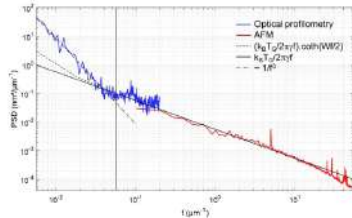
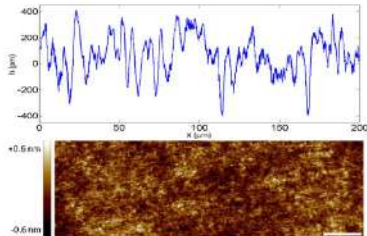
Roughness Measurements within Photonic fibres



Differential profilometry + selective filling: picometer resolution

C. Brun et al. *Opt. Express* **22** 29554, (2014) ; X. Buet et al, *Opt. Lett.* **41** 5089, (2016)

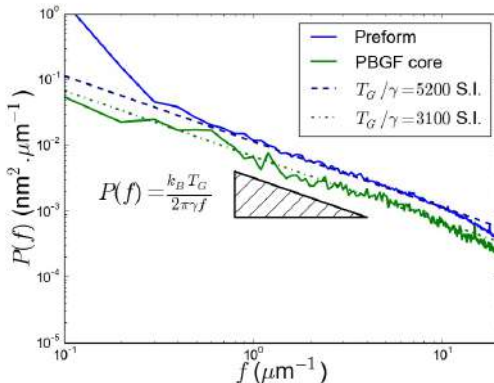
Roughness Measurements within Photonic fibres



Capillary waves on the inner core surface of micro-structured photonic fibres

C. Brun et al. *Opt. Express* **22** 29554, (2014) ; X. Buet et al. *Opt. Lett.* **41** 5089, (2016)

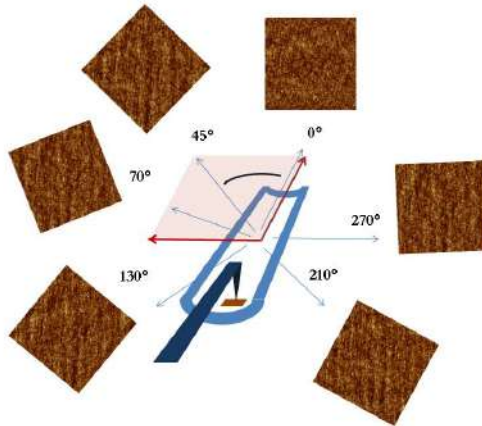
AFM Measurement within Photonic fibres



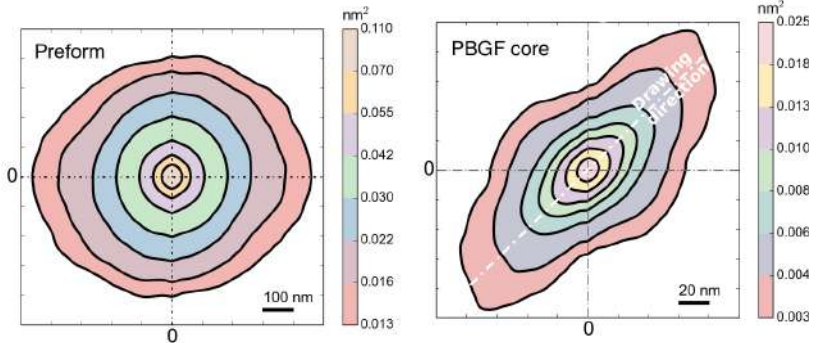
Amorphous silica: $T_G \approx 1500\text{K}$, $\gamma \approx 0.3\text{J.m}^{-2} \Rightarrow T_G/\gamma \approx 5000$, recovered before drawing.

After drawing: effective interface tension 70% larger, height fluctuations 30% lower than thermal fluctuations !

Roughness anisotropy induced by fiber drawing



Anisotropic spatial correlations



Suppression of Thermally Excited Capillary Waves by Shear Flow

Didi Derks,¹ Dirk G. A. L. Aarts,^{2,3} Daniel Bonn,^{3,4} Henk N. W. Lekkerkerker,² and Amount Imhof⁴

¹*Soft Condensed Matter, Debye Institute, Utrecht University, Princetonplein 5, 3584 CC Utrecht, The Netherlands*

²*Van 't Hoff Laboratory, Debye Institute, Utrecht University, Padualaan 8, 3584 CH Utrecht, The Netherlands*

³*Laboratoire de Physique Statistique, Ecole Normale Supérieure, 24 Rue Lhomond, F-75231 Paris Cedex 05, France*

⁴*van der Waals-Zeeman Institute, University of Amsterdam, Valckenierstraat 65, 1018 XE Amsterdam, The Netherlands*

(Received 31 March 2006; published 18 July 2006)

PHYSICAL REVIEW E **81**, 031602 (2010)

Nonequilibrium fluctuations of an interface under shear

Marine Thiébaud and Thomas Bickel*

CPMOH, Université de Bordeaux and CNRS (UMR 5798), 351 Cours de la Libération, 33405 Talence, France

(Received 28 August 2009; published 22 March 2010)

The steady-state properties of an interface in a stationary Couette flow are addressed within the framework of fluctuating hydrodynamics. Our study reveals that thermal fluctuations are driven out of equilibrium by an effective shear rate that differs from the applied one. In agreement with experiments, we find that the mean-square displacement of the interface is reduced by the flow. We also show that nonequilibrium fluctuations present a certain degree of universality in the sense that all features of the fluids can be factorized into a single control parameter. Finally, the results are discussed in the light of recent experimental and numerical studies.

$$S(\mathbf{q}, \sigma_{vis}) \approx S_0(q) [1 - A\alpha^2 |\cos \theta_q|^2], \quad S_{eq}(\mathbf{q}) = \frac{kT}{\gamma |\mathbf{q}|^2}, \quad \alpha = \frac{W\sigma_{vis}}{\gamma}$$

Drawing hollow fibres at different temperatures

- keep same geometry
- different velocities
- different viscosities,
hence stress

Control parameter =
adimensioned drawing stress:

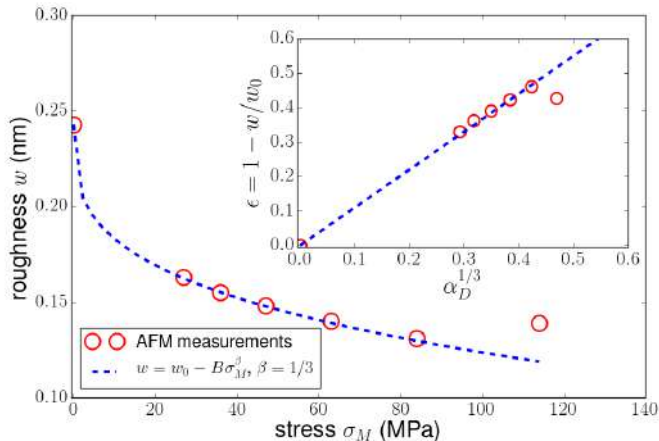
$$\alpha_D = \frac{w\sigma_M}{\gamma}$$

Range of furnace temperature $T_D \in [2000^\circ\text{C} - 2100^\circ\text{C}]$,

Range of drawing stress $\sigma_M \in [20\text{MPa} - 120\text{MPa}]$

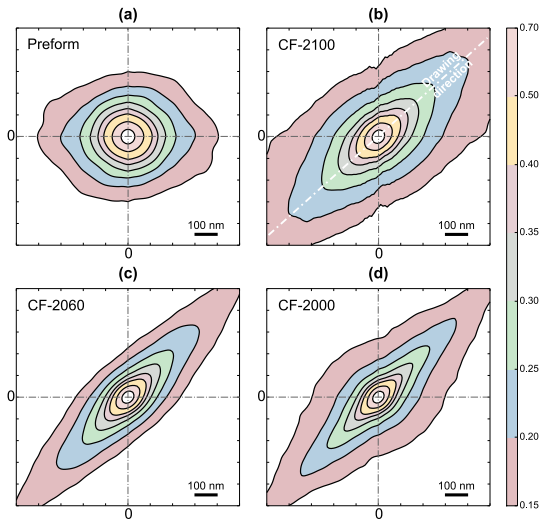
Range of control parameter $\alpha_D \in [0.02 - 0.12]$

Surface roughness attenuation under drawing

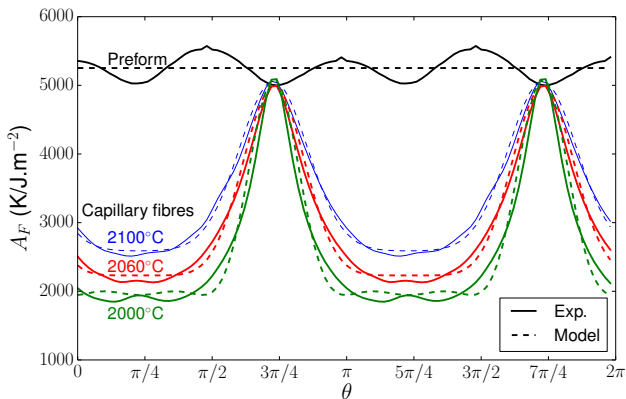


The larger the stress, the lower the roughness: $\frac{w_0 - w(\alpha_D)}{w_0} \approx B\alpha_D^{1/3}$

Stress dependent anisotropy of glass surfaces



Non-linear attenuation of the capillary modes



$$S(\mathbf{q}) = \frac{k_B A_F(\theta_q)}{|\mathbf{q}|^2} \approx \frac{k_B T_G}{\gamma |\mathbf{q}|^2} (1 - a \cos^2[\theta_q + b \sin(\theta_q)])$$

Conclusion: the long memory of glass surfaces

- Glass surfaces keep the memory of their liquid state
- Height fluctuations: frozen capillary waves at T_G
- Under flow: ultra-low roughness, below equilibrium thermodynamics expectation
- Strongly anisotropic correlations
- Non-linear attenuation of the capillary modes under flow

B. Bresson et al, Phys. Rev. Lett. **119** 235501, (2017) J. Osorio et al, Nat. Comm. **14** 1146, (2023)

A stochastic hydrodynamics approach

$$\frac{\partial h_{\mathbf{k}}}{\partial t} + i\dot{\gamma}k_x [h^2]_{\mathbf{k}} = -\frac{\sigma|k|}{\eta}h_{\mathbf{k}} + \eta_{\mathbf{k}}$$

$$S(\mathbf{q}, \sigma_{vis}) \approx S_0(q) [1 - A\alpha^2 |\cos \theta_q|^2] , \quad \alpha = \frac{w}{\ell_c} \dot{\epsilon} \tau_c ;$$

$$C(\mathbf{r}, \sigma_{vis}) \approx C_0(r) \left[1 - \frac{A}{2} \alpha^2 \right] + \frac{A}{8\pi} \alpha^2 w_0^2 \cos 2\theta .$$

Spectrum of (frozen) capillary waves

$$\langle |\tilde{h}_{\mathbf{q}}|^2 \rangle = S_0 \frac{kT}{\gamma q^2} \frac{1}{1 + (q\ell_c)^{-2}}, \quad \tau_q = \frac{4\eta}{\gamma q} \frac{1}{1 + (q\ell_c)^{-2}}$$

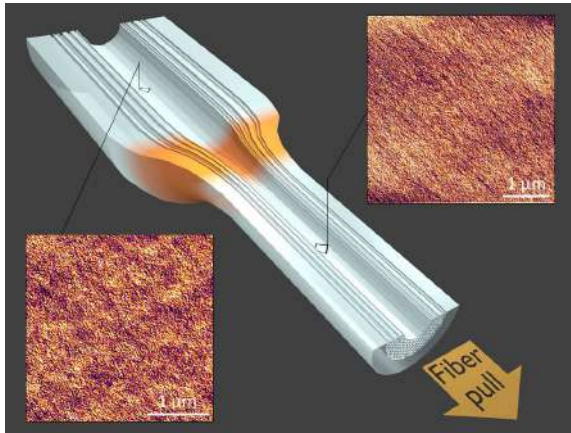
Height correlations:

$$\langle |h(r)h(0)| \rangle = \frac{kT}{2\pi\gamma} K_0\left(\frac{r}{\ell_c}\right) \approx \frac{kT}{2\pi\gamma} \log\left(\frac{r}{\ell_c}\right) \quad \text{for } r \ll \ell_c$$

$$\langle h(\mathbf{r}, t)h(\mathbf{r}, 0) \rangle = \frac{kT}{2\pi\gamma} K_0\left(\frac{t}{\tau_c}\right) \approx \frac{kT}{2\pi\gamma} \log\left(\frac{t}{\tau_c}\right) \quad t \ll \tau_c = \frac{\eta\ell_c}{\gamma}$$

Glass roughness : static correlations of capillary waves at T_G ?

Drawing hollow fibres at different temperatures



B. Bresson et al, PRL 2017

Roughness of fibres drawn at different temperatures

Sample	T_{Furnace} (°C)	σ_M (MPa)	α_D	RMS (nm)
Preform	N.A.	0	0	0.243
Capillary Fibres	2100	27	0.024	0.163
	2080	36	0.031	0.155
	2060	47	0.041	0.148
	2040	63	0.055	0.140
	2020	84	0.074	0.131
	2000	114	0.101	0.139

The larger the stress, the lower the height fluctuations

B. Bresson et al, PRL 2017



Morphologie et rugosité des surfaces de verres



Damien Vandembroucq

Laboratoire PMMH, ESPCI Paris PSL, CNRS,
Sorbonne Université, Université de Paris France
Laboratoire SVI, CNRS/Saint-Gobain

Ecole Verre et Optique, Presqu'île de Giens 05-10 octobre 2025





Float glass process



Verres imprimés



SGG PIXARENA



SGG LISTRAL M



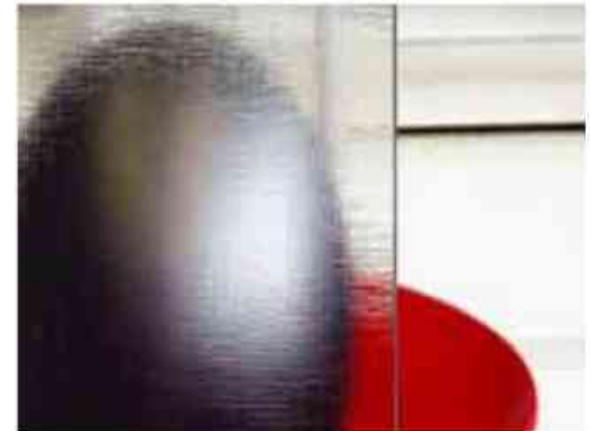
SGG WATERDROP



SGG ENTRELAZADO



SGG MARIS

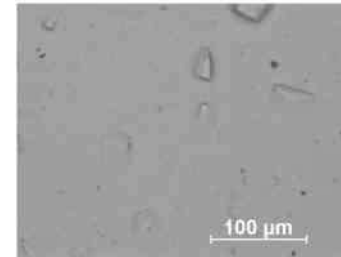
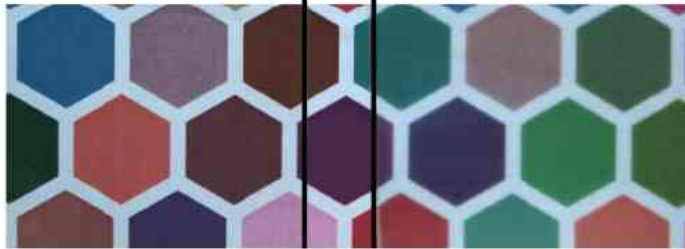


SGG THELA

Verres dépolis

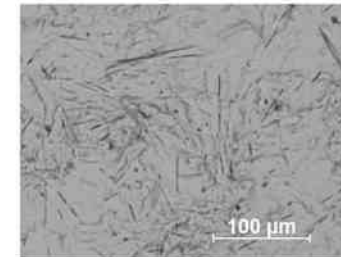
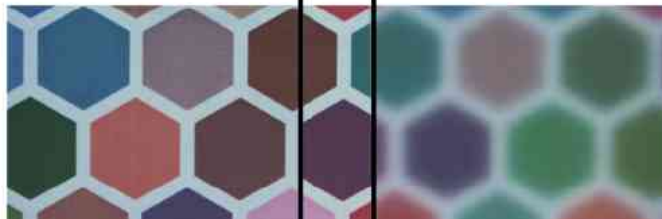
Planilux

G1



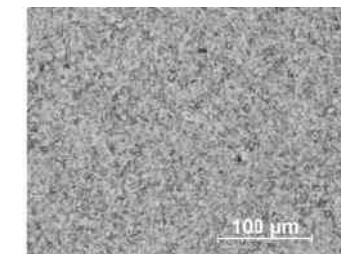
Planilux

G2



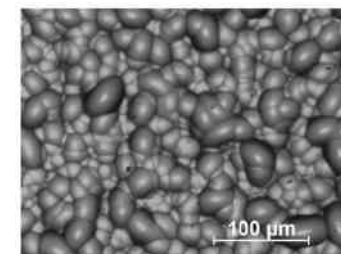
Planilux

G3

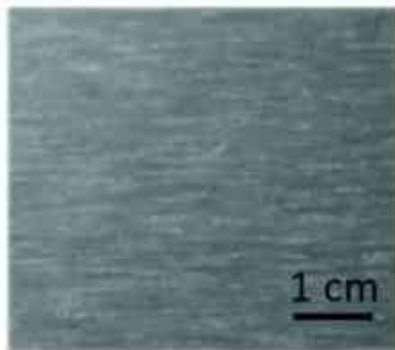


Planilux

G4



Surfaces métalliques sablées



Untreated



Small beads

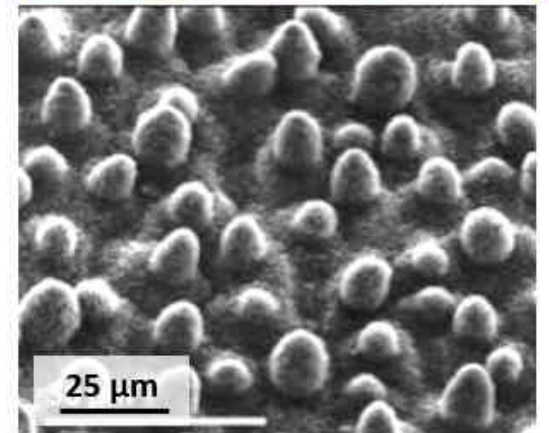
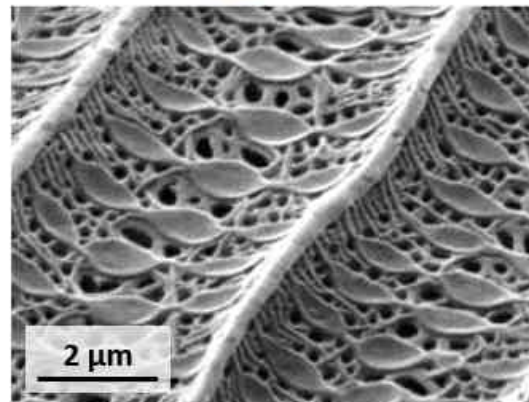
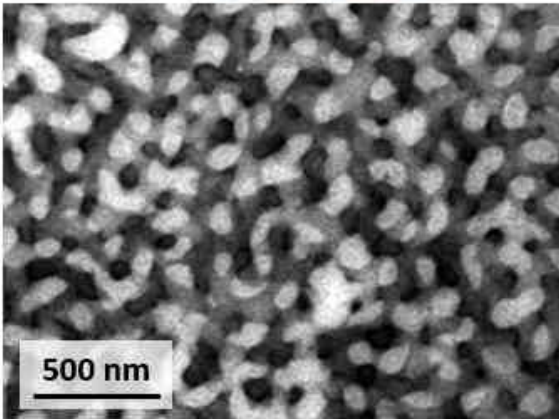


Medium beads



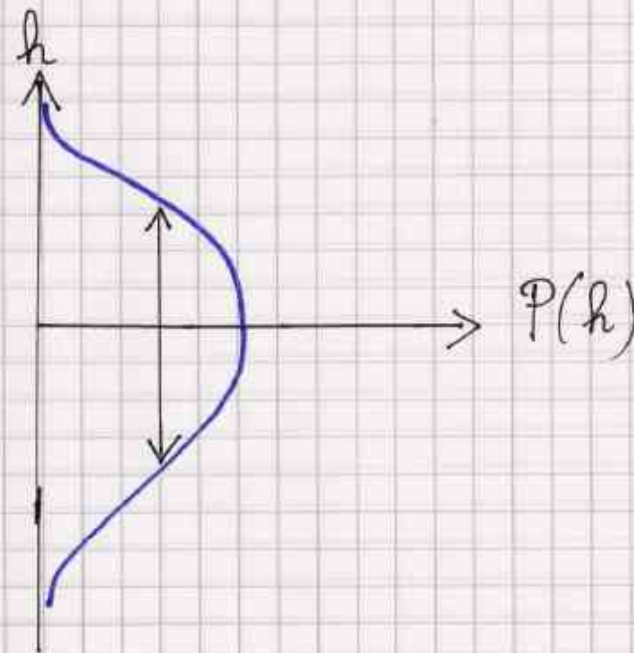
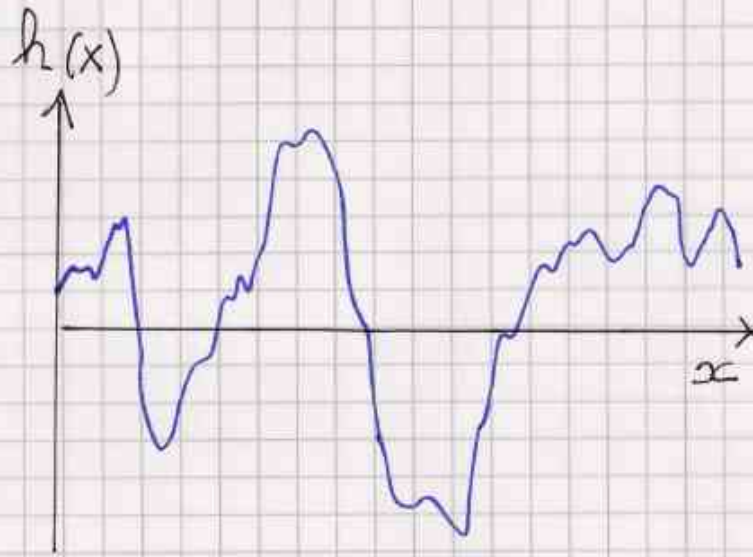
Large beads

Surfaces texturées : bio-inspiration



Interfaces rugueuses

Rugosité : distribution des hauteurs



▣ Approche probabiliste

▣ Un paramètre essentiel : la LARGEUR de la distribution

- plusieurs estimateurs pour une même quantité

$$R_q = \text{RMS} = \text{écart-type de la distribution} = \left(\frac{\sum h_i^2}{N} \right)^{\frac{1}{2}} = \left(\int h^2 P(h) dh \right)^{\frac{1}{2}}$$

$$R_a = \frac{1}{N} \sum_i |h_i| = \int |h| P(h) dh$$

Rugosité : variance, skewness, kurtosis

□ De façon générale la distribution des hauteurs est caractérisée par la donnée de l'ensemble de ses moments

$$M_m = \int h^m P(h) dh$$

M_1 = moyenne = 0

M_2 = variance = RMS^2

M_3 = skewness s

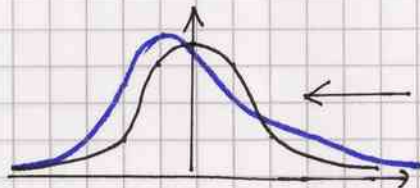
M_4 = kurtosis k

→ largeur de la distribution

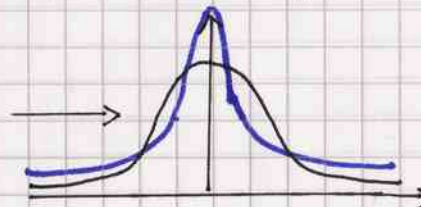
→ symétrie de la distribution

→ forme "piquée" ou aplatie de la distribution

asymétrie
 $|s| > 0$

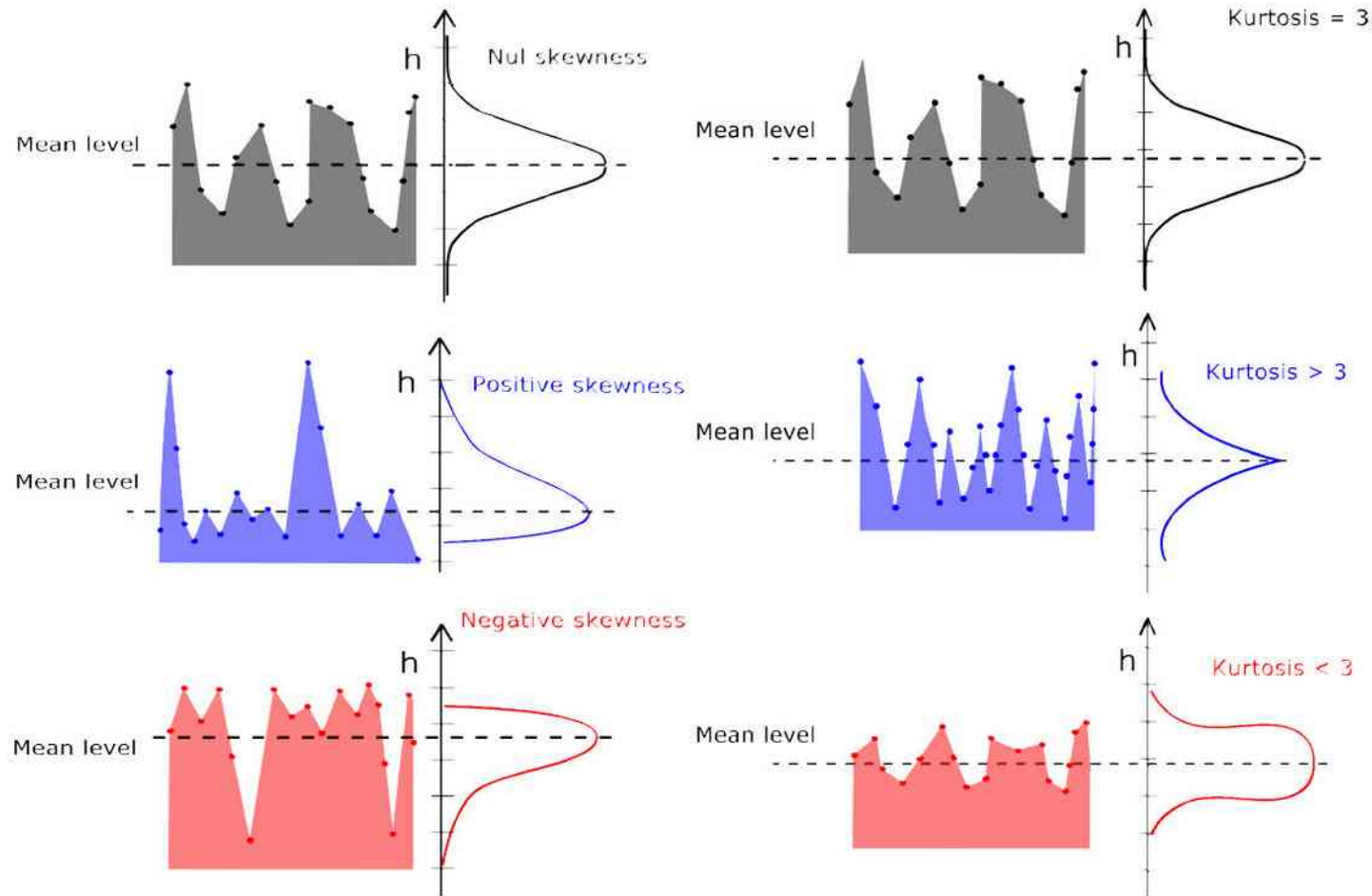


Gaussienne



écart à la Gaussienne
 $k-3 \neq 0$

Skewness et Kurtosis



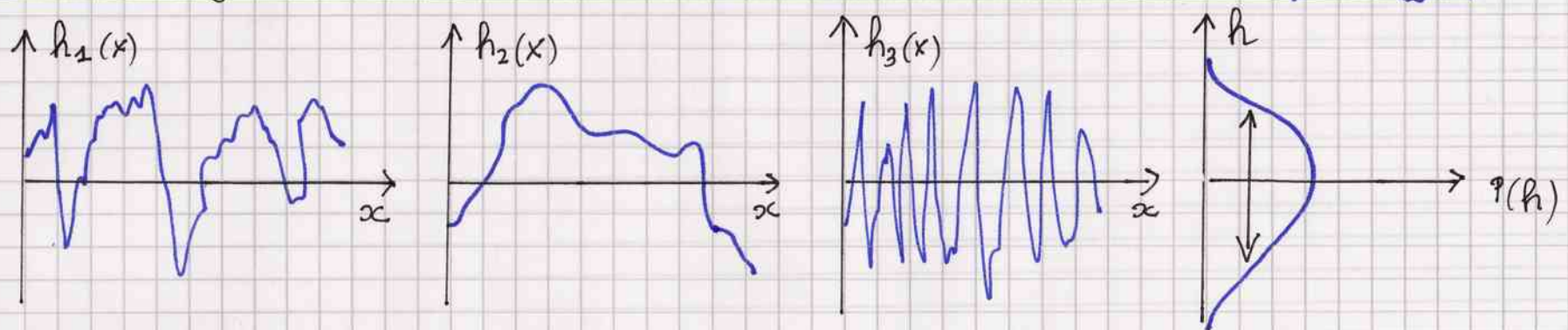
Skewness et kurtosis: utiles, mais délicats à estimer,
Sensibles aux valeurs extrêmes (défauts/erreurs de mesure)

Rugosité: fluctuations verticales vs horizontales

- En pratique, lorsque la surface est Gaussienne, la RMS suffit à caractériser la distribution

$$P(h) = \frac{1}{\sigma \sqrt{2\pi}} \exp\left(-\frac{h^2}{2\sigma^2}\right) \quad \sigma = \text{RMS}$$

- RMS et la fonction distribution des hauteurs = essentielle mais pas suffisante

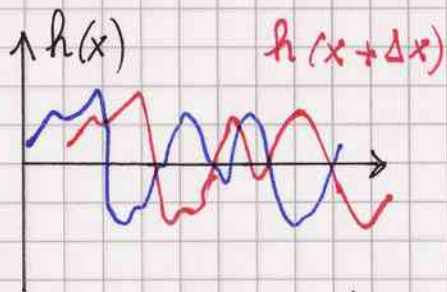


La distribution des hauteurs fournit une information sur les fluctuations **verticales** - Une même RMS, une même distribution peut correspondre à des surfaces très différentes

Corrélations spatiales

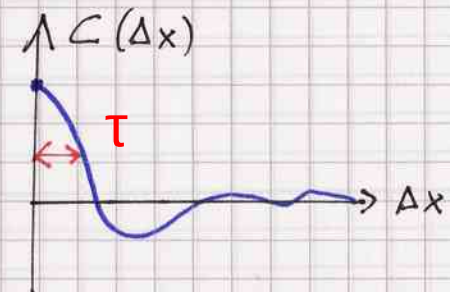
- Dans les cas les plus simples la fonction d'auto-corrélation $C(\Delta x)$ est très rapidement décroissante, exponentielle, Gaussienne
- définition d'1 longueur de corrélation

- Corrélation des hauteurs → information sur les motifs horizontaux



$$C(\Delta x) = \langle h(x)h(x+\Delta x) \rangle$$

fonction d'auto-corrélation



Un paramètre essentiel: la LONGUEUR de CORRÉLATION $\sim$ taille motifs h^{aux}

Longueur de corrélation

□ Dans les cas les plus simples la fonction d'auto-corrélation $C(\Delta x)$ est très rapidement décroissante, exponentielle, Gaussienne
→ définition d'1 longueur de corrélation τ

$$C(\Delta x) = \sigma^2 f(\Delta x/\tau)$$

σ = rugosité RMS

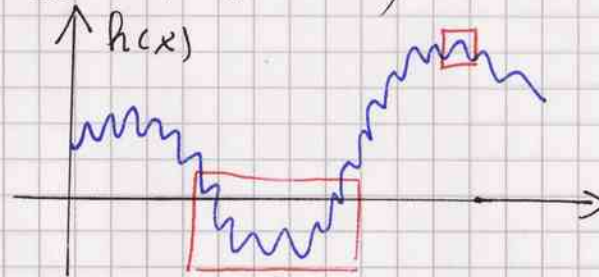
$f(\Delta x/\tau) \rightarrow 1$ si $\Delta x/\tau \rightarrow 0$

$f(\Delta x/\tau) \rightarrow 0$ si $\Delta x/\tau \gg 1$

Pente caractéristique $s = \sigma/\tau$

Longueurs de corrélations

- Parfois la surface est caractérisée par **plusieurs** longueurs de corrélation, voire par un "**continuum**" de longueurs de corrélations (surfaces de type "fractal" ou "auto-affines", cf + loin)

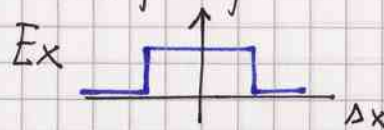


2 motifs caractéristiques
à petite et grande échelle

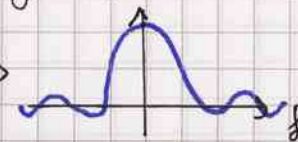
- Sur le plan mathématique, la fonction d'autocorrélation $C(\Delta x)$ est la transformée de Fourier de la densité spectrale de puissance $PSD(f)$

$$PSD(f) = |\tilde{h}|^2$$

→ Toute fonction réelle paire ne peut pas être une fonction d'auto-corrélation, sa TF doit être **positive**!



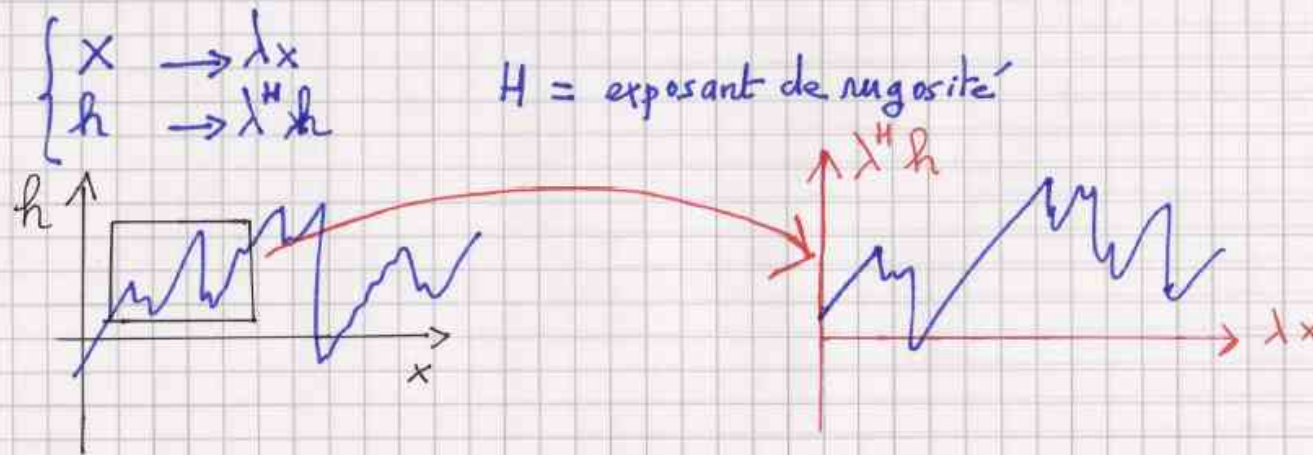
TP →



≠ fonction
autocorrélation

Echelles de mesure vs longueurs de corrélations

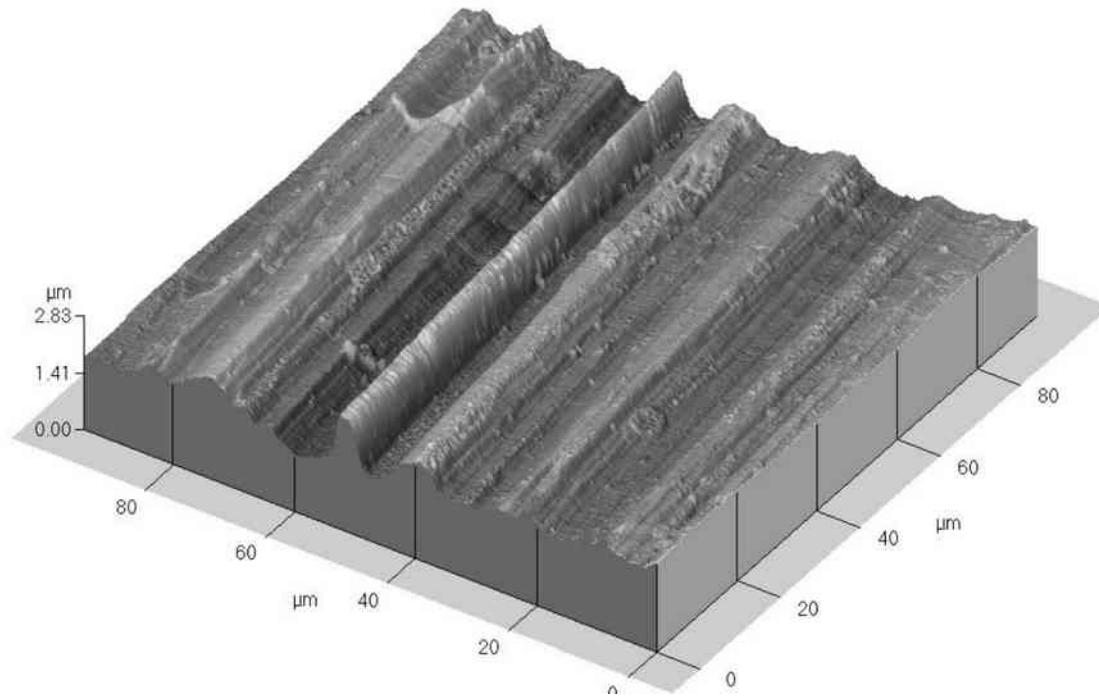
- Dans certains cas la surface n'est pas caractérisée par 1 mais par un continuum de longueurs de corrélation
- Une symétrie particulière: la symétrie auto-affine
la surface reste statistiquement invariante par des "zooms" anisotropes



- Sur le plan pratique, cette invariance a une conséquence importante:
la rugosité RMS dépend de l'échelle sur laquelle on la mesure!

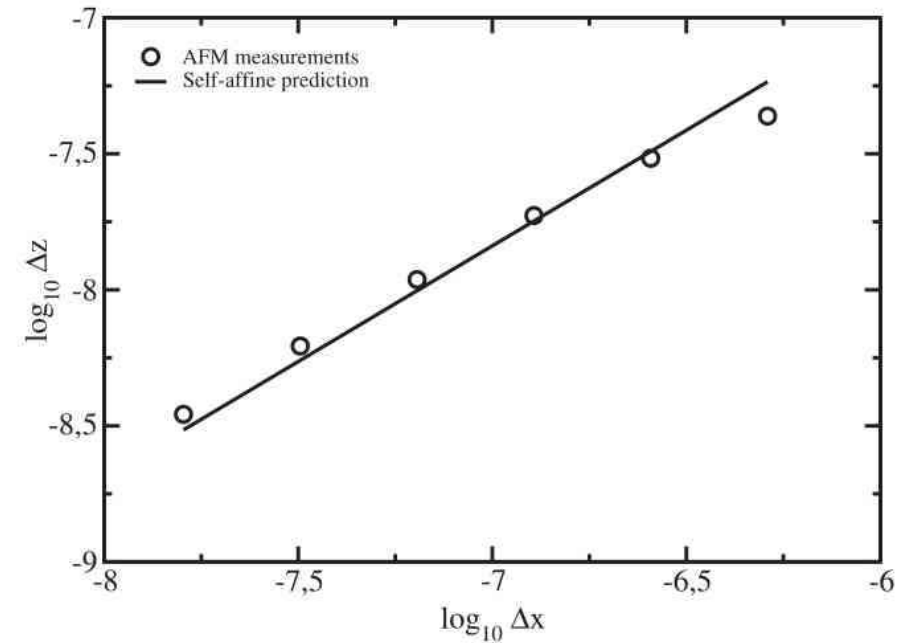
$$\sigma(\Delta x) \propto \Delta x^H$$

Surface d'une feuille d'aluminium laminée à froid



Corrélations autoaffines :

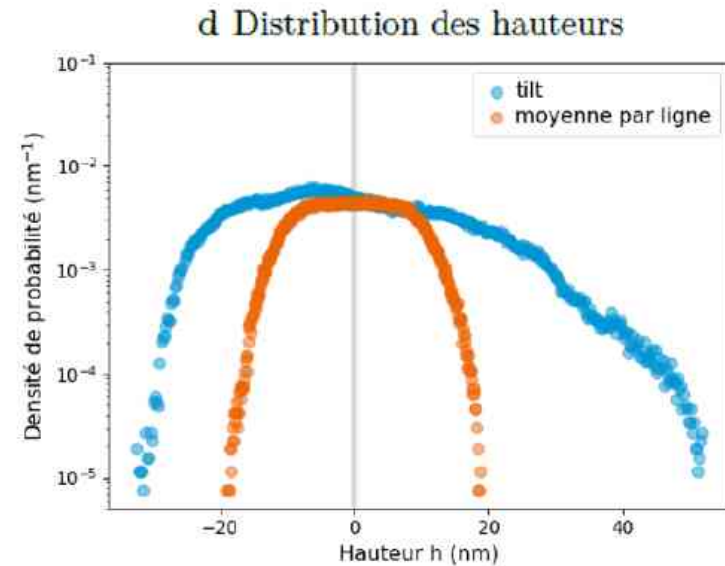
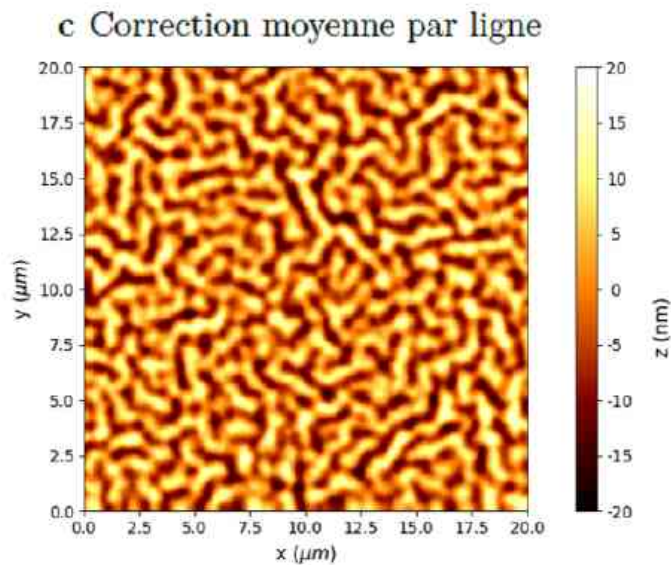
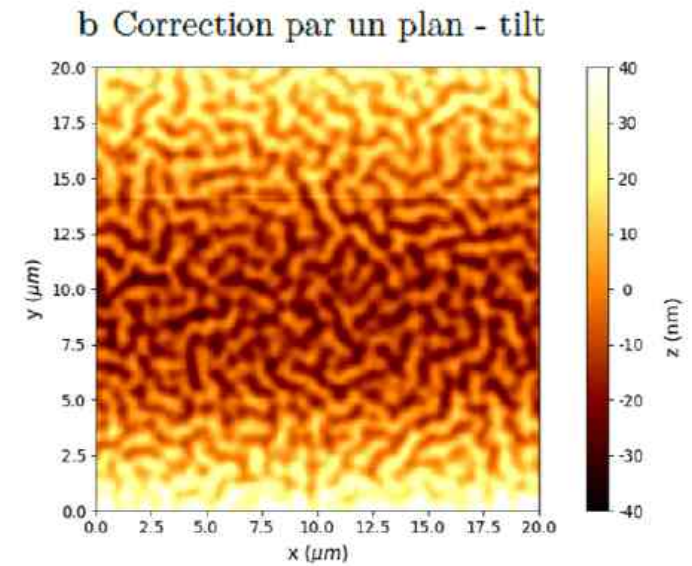
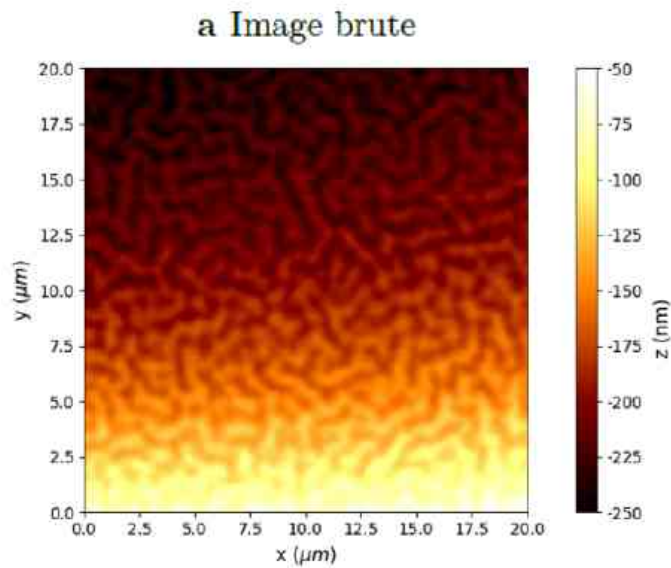
$$\sigma_z(\Delta x) \propto (\Delta x)^H, H \approx 0.78$$



Pente caractéristique :

$$S(\lambda) \approx 0.11 @ \lambda = 638.2 \text{ nm}$$

Rugosité : pré-traitement des données



More about roughness, local slopes and curvatures

IOP Publishing

Surf. Topogr.: Metrol. Prop. **11** (2023) 025018

<https://doi.org/10.1088/2051-672X/acd469>

Surface Topography: Metrology and Properties



CrossMark

RECEIVED
23 December 2021

REVISED
26 April 2023

ACCEPTED FOR PUBLICATION
11 May 2023

PUBLISHED
24 May 2023

PAPER

Statistically representative estimators of multi-scale surface topography: example of aluminum blasted rough samples

C Turbil¹, J Cabrero² , I Simonsen^{1,3} , D Vandembroucq⁴ and I Gozhyk¹

¹ SVI, UMR 125 CNRS/Saint-Gobain Research Paris, 39 quai Lucien Lefranc, F-93303 Aubervilliers, France

² Saint-Gobain Research Provence, 550 avenue Alphonse Jauffret, F-84306 Cavaillon, France

³ Department of Physics, NTNU—Norwegian University of Science and Technology, NO-7491 Trondheim, Norway

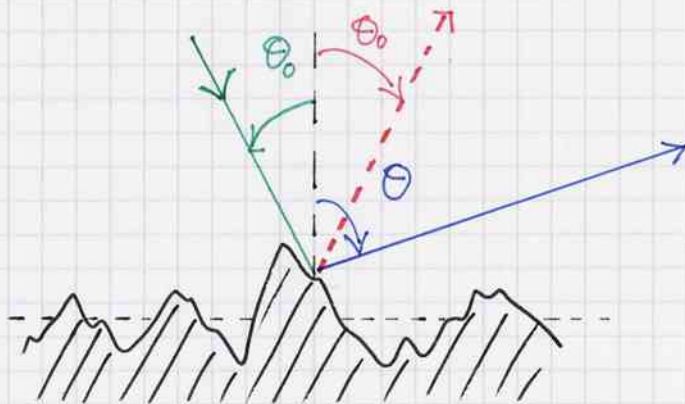
⁴ PMMH, CNRS, ESPCI Paris, PSL University, Sorbonne Université, Université de Paris, 10 rue Vauquelin, F-75231 Paris cedex 05, France

E-mail: iryna.gozhyk@saint-gobain.com

Keywords: multi-scale roughness, blasted aluminum, topography, surface slopes, mounded surface

Diffusion de la lumière par des interfaces rugueuses

Diffusion de la lumière par des interfaces rugueuses



θ_0 : angle incident

θ : angle de diffusion

$\theta = \theta_0$: direction spéculaire

Intensité diffusée : $I_d(\theta, \theta_0) = \langle |A|^2 \rangle$

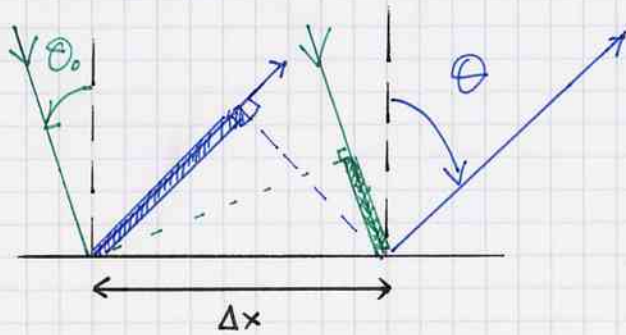
—— cohérente : $I_{coh}(\theta, \theta_0) = \langle A \rangle^2$

—— incohérente : $I_{inc}(\theta, \theta_0) = \langle |A|^2 \rangle - \langle A \rangle^2$

où $A = A_0 e^{i\varphi}$ est l'amplitude de l'onde

Rugosité et retard de phase

Décalage horizontal

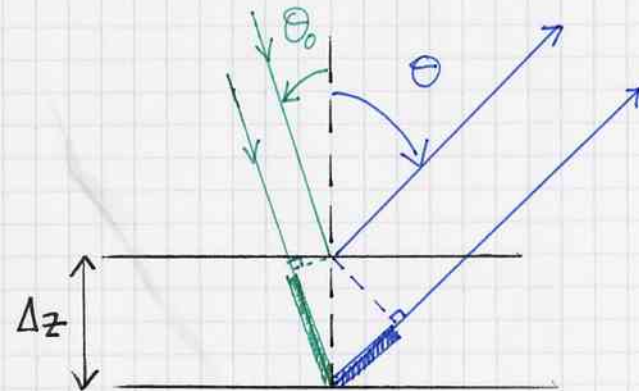


$$\Delta c_h = \Delta x (\sin \theta_0 - \sin \theta)$$

$$\delta_h \sim \frac{\lambda}{|\sin \theta_0 - \sin \theta|}$$

↑
longueur de cohérence
E.g. $\Delta c \sim \lambda$

Décalage vertical



$$\Delta c_v = \Delta z (\cos \theta + \cos \theta_0)$$

$$\begin{aligned} \Delta \varphi &= \frac{2\pi}{\lambda} (\Delta c_h + \Delta c_v) \\ &= \frac{2\pi}{\lambda} [\Delta x (\sin \theta_0 - \sin \theta) + \Delta z (\cos \theta + \cos \theta_0)] \end{aligned}$$

Diffusion cohérente et distribution de hauteurs

$$I_{\text{coh}}(\theta, \theta_0) \propto \int e^{i\varphi(\theta, \theta_0)} dx$$

□ $\theta \neq \theta_0$ $\Rightarrow$ $\left| \begin{array}{l} \delta_h = \frac{\lambda}{|\sin\theta - \sin\theta_0|} \ll L \\ \text{longueur surface} \\ \hline \underline{I_{\text{coh}}(\theta \neq \theta_0) = 0} \end{array} \right.$

□ $\theta = \theta_0$ Réflexion spéculaire

$$I_{\text{coh}}(\theta_0) = \int e^{\frac{2i\pi}{\lambda} \Delta z (\cos\theta + \cos\theta_0)} dx = \langle e^{i\varphi} \rangle$$

$$= \int e^{\frac{2i\pi}{\lambda} \Delta z \frac{2\cos\theta_0}{\lambda}} \underbrace{P(\Delta z)}_{\substack{\downarrow \\ \text{T.F.}}} d\Delta z$$

distribution des hauteurs

$$P(\Delta z) \propto e^{-\Delta z^2 / 4\sigma^2} \Rightarrow \underline{I_{\text{coh}}(\theta_0) \propto e^{-\frac{\sigma^2 \cos^2 \theta_0}{\lambda^2}}}$$

Diffusion incohérente et corrélations de hauteurs

deux longueurs de cohérence :

$$\delta_h \sim \frac{\lambda}{|\sin\theta - \sin\theta_0|} \quad \searrow \text{ quand l'écart angulaire } \nearrow$$

$$\delta_v \text{ [Gaussien ou self-affine]} \searrow \text{ quand la pente locale } \nearrow$$

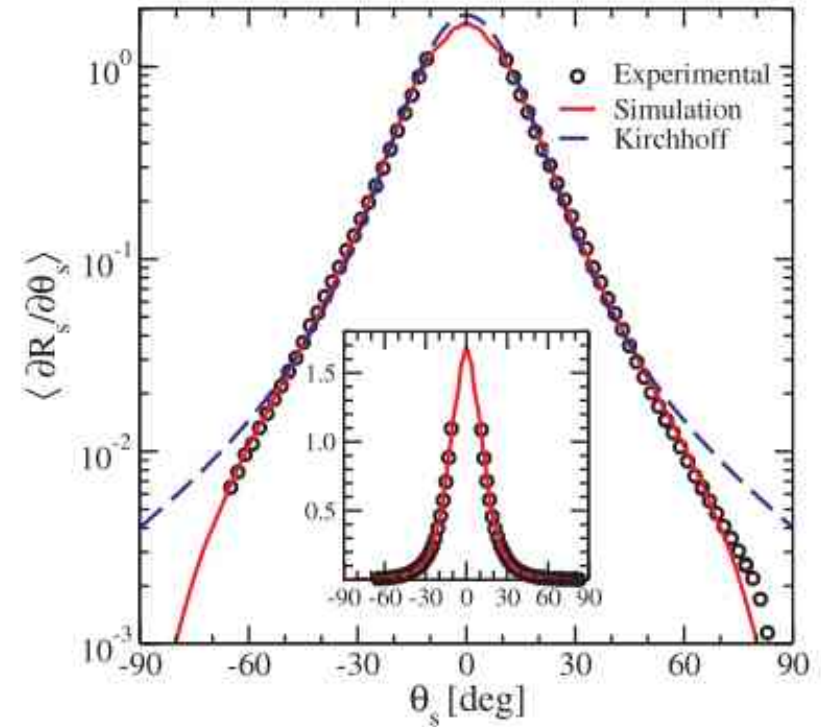
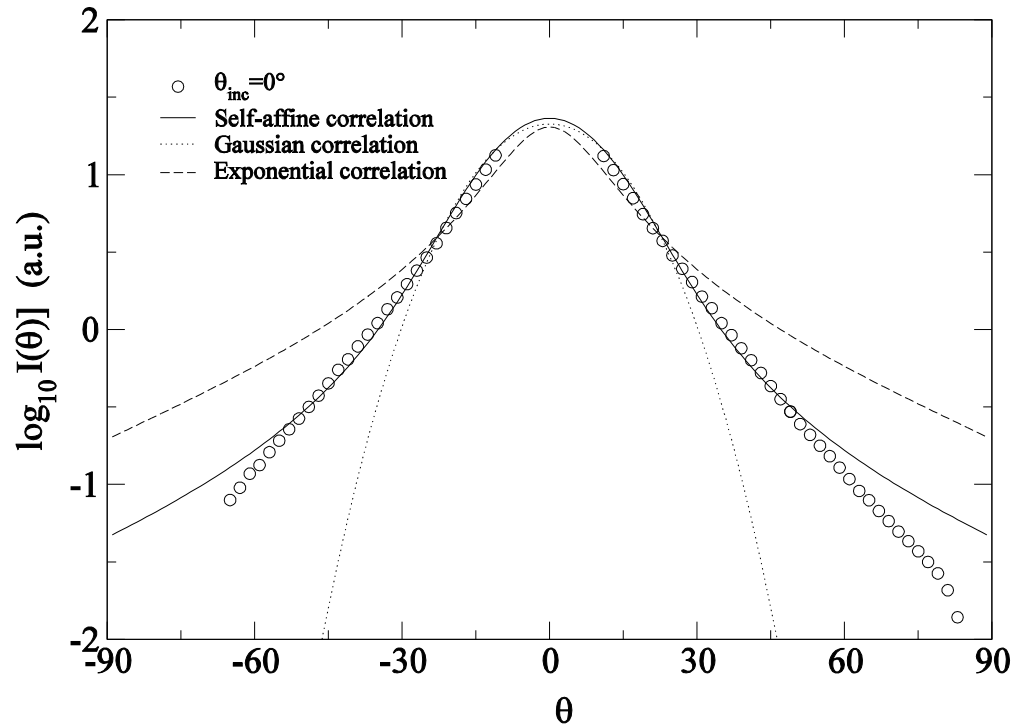
Aux petits angles $|\theta - \theta_0| \ll 1$: $\delta_v \ll \delta_h$

Aux grands angles : $\delta_h \ll \delta_v$

w largeur angulaire du pic de diffusion $\text{tg} \quad \delta_v \sim \delta_h$

$$w_G \sim 2 \frac{\sigma}{\lambda} ; \quad w_{SA} \sim [2s(\lambda)]^{-1/H}$$

Diffusion de la lumière par une surface d'aluminium

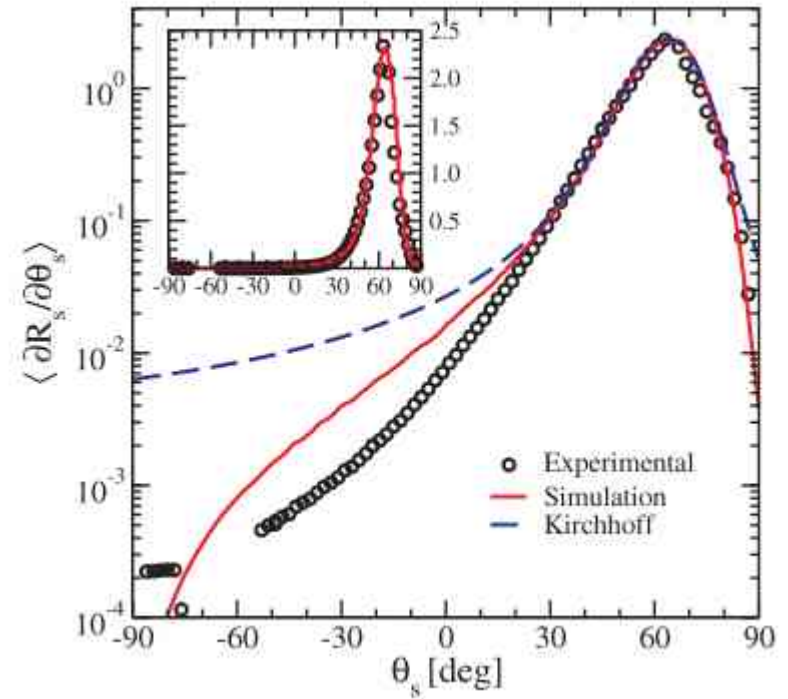
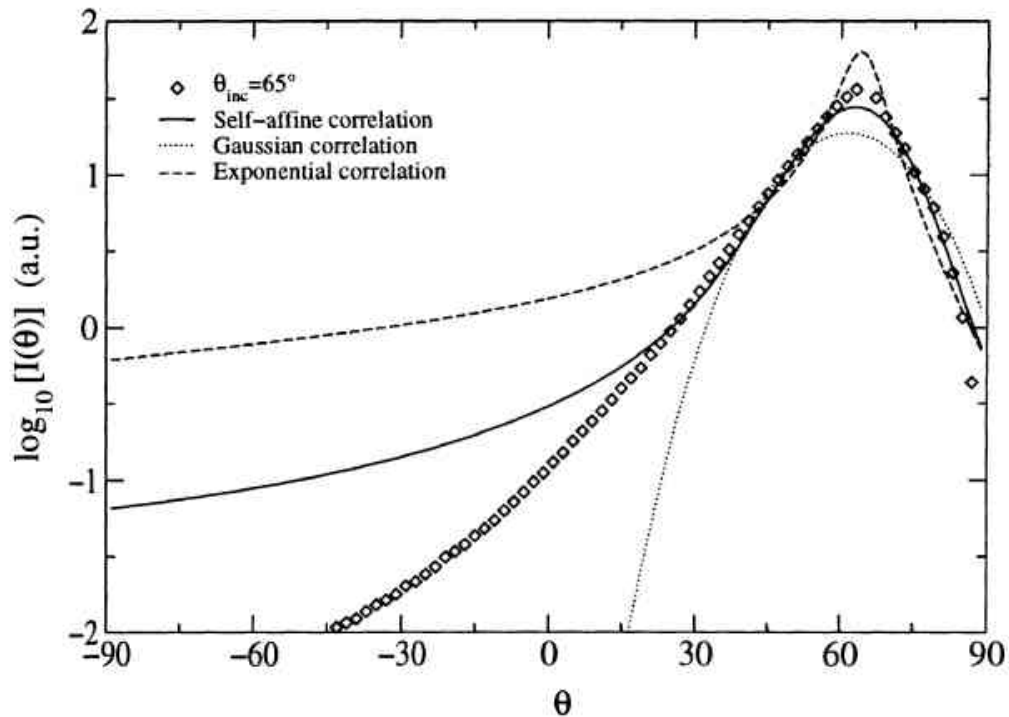


Résultats expérimentaux vs Approximation de Kirchhoff et Simulations avec corrélations Gaussiennes, Exponentielles ou Auto-Affines

Paramètres expérimentaux rugosité : $\sigma_z(\Delta x) \propto (\Delta x)^H$, $H \approx 0.78$

$s(\lambda) \approx 0.11$ @ $\lambda = 638.2$ nm

Diffusion de la lumière par une surface d'aluminium



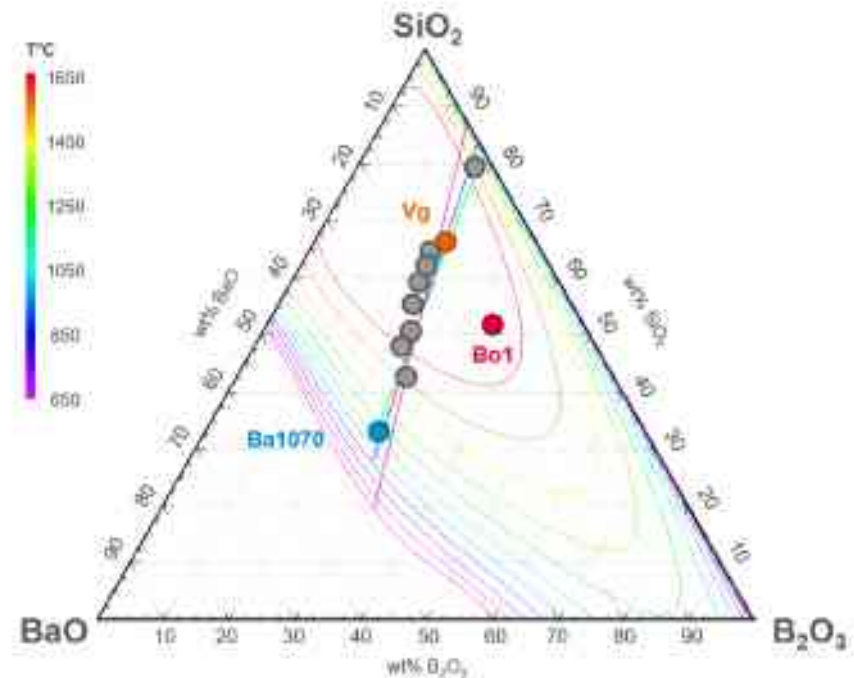
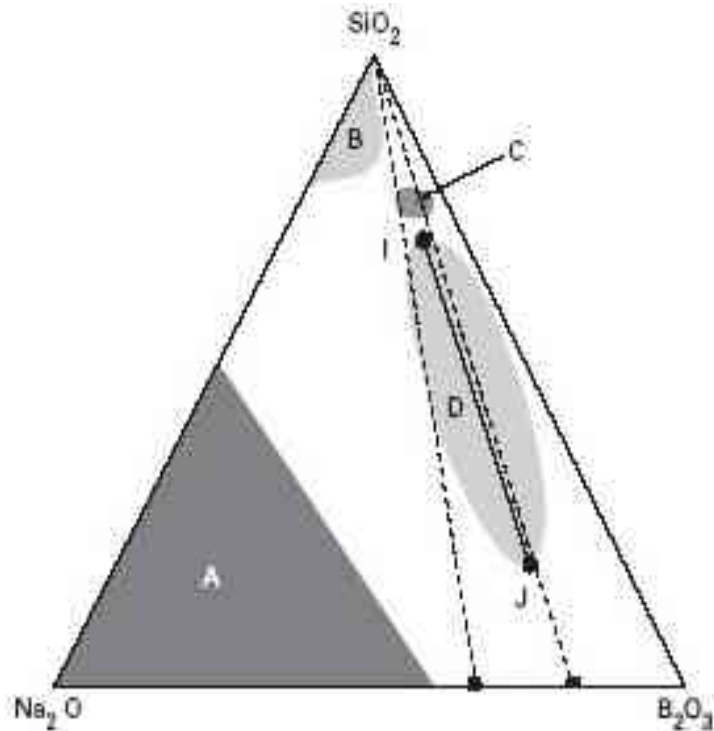
Résultats expérimentaux vs Approximation de Kirchhoff et Simulations avec corrélations Gaussiennes, Exponentielles ou Auto-Affines

Paramètres expérimentaux rugosité : $\sigma_z(\Delta x) \propto (\Delta x)^H$, $H \approx 0.78$

$s(\lambda) \approx 0.11$ @ $\lambda = 638.2$ nm

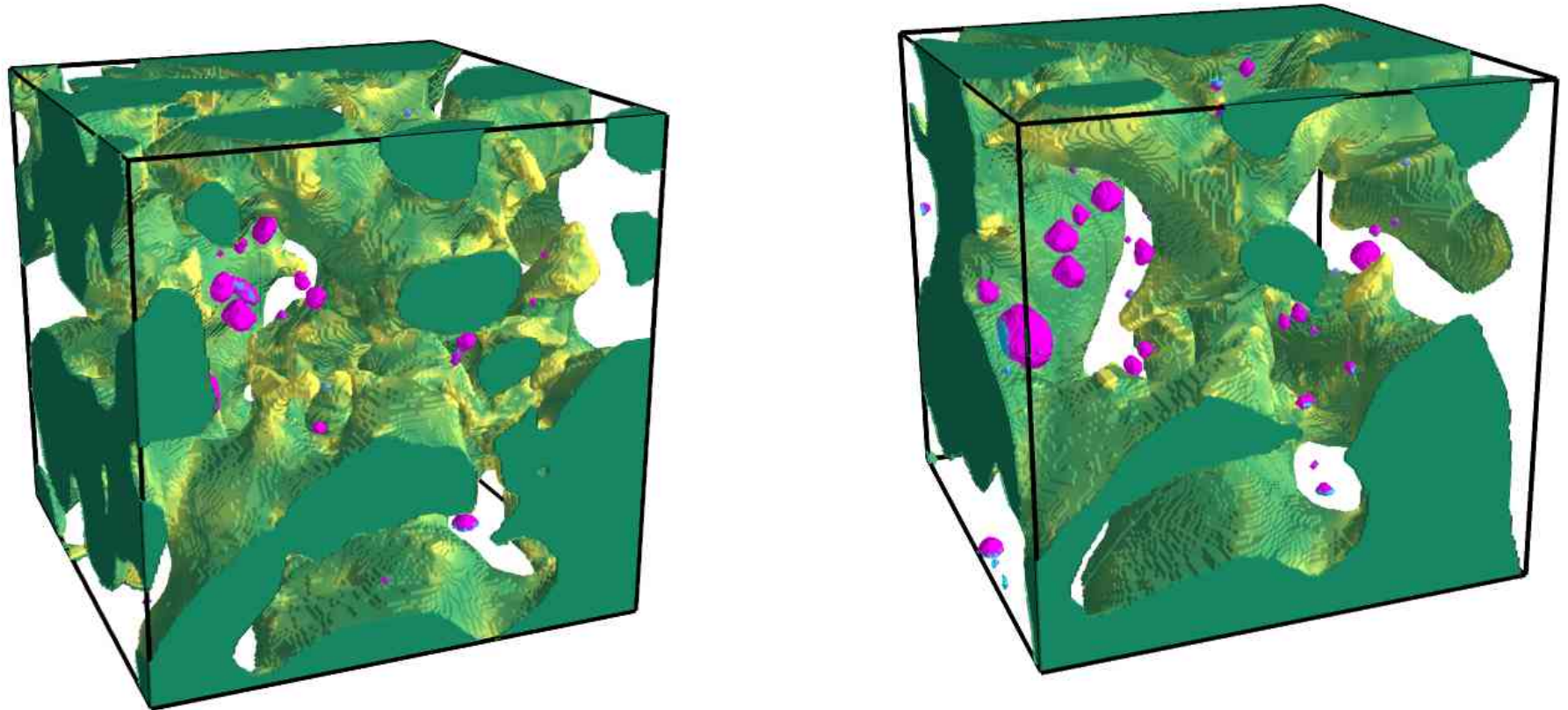
Application à l'étude de la séparation de phase dans les verres

Verres démixés

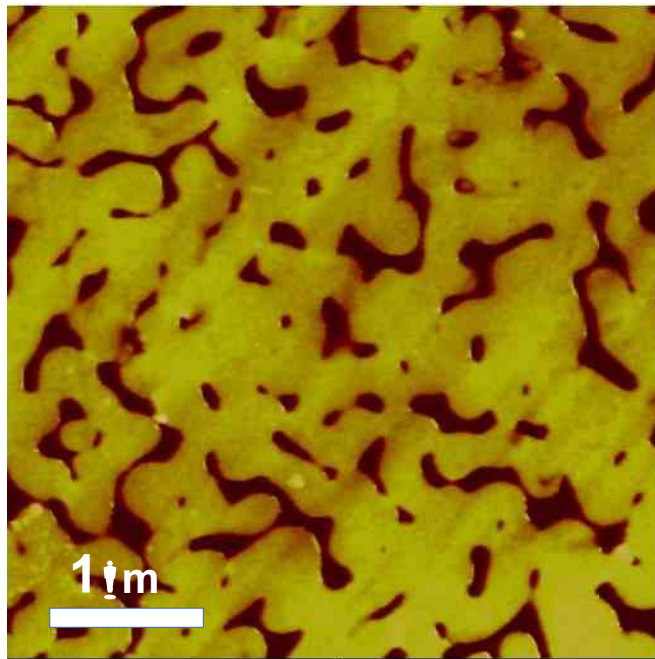


Séparation de phase dans de nombreuses compositions verrières binaires ou ternaires
Différentes tailles de domaines, morphologies variées, mûrissement hydrodynamique ou diffusif. Applications: pyrex, vycor, etc.

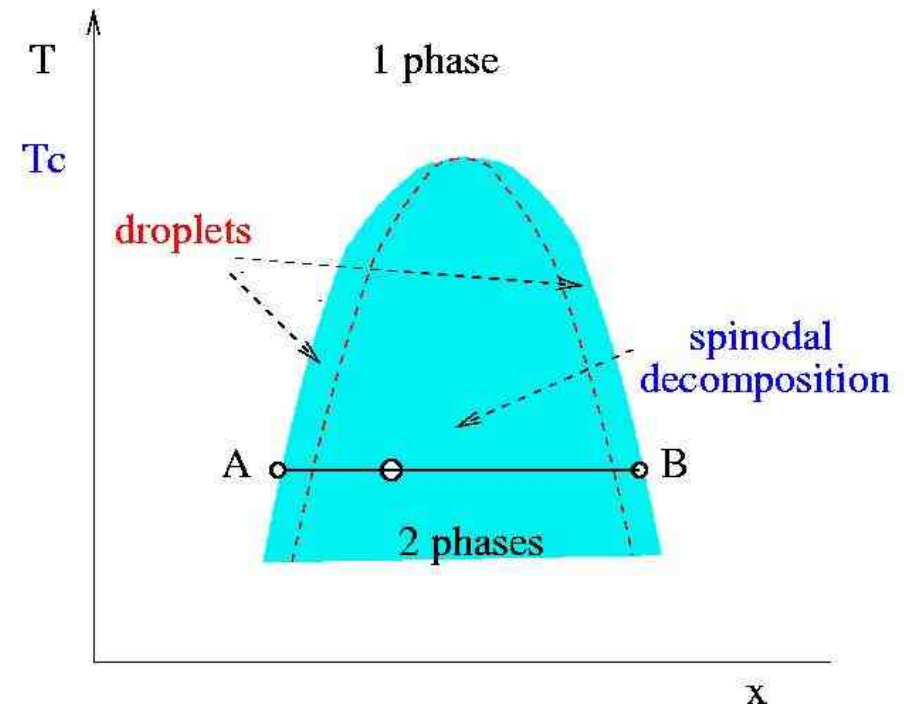
Suivi temps réel du mûrissement par tomographie X



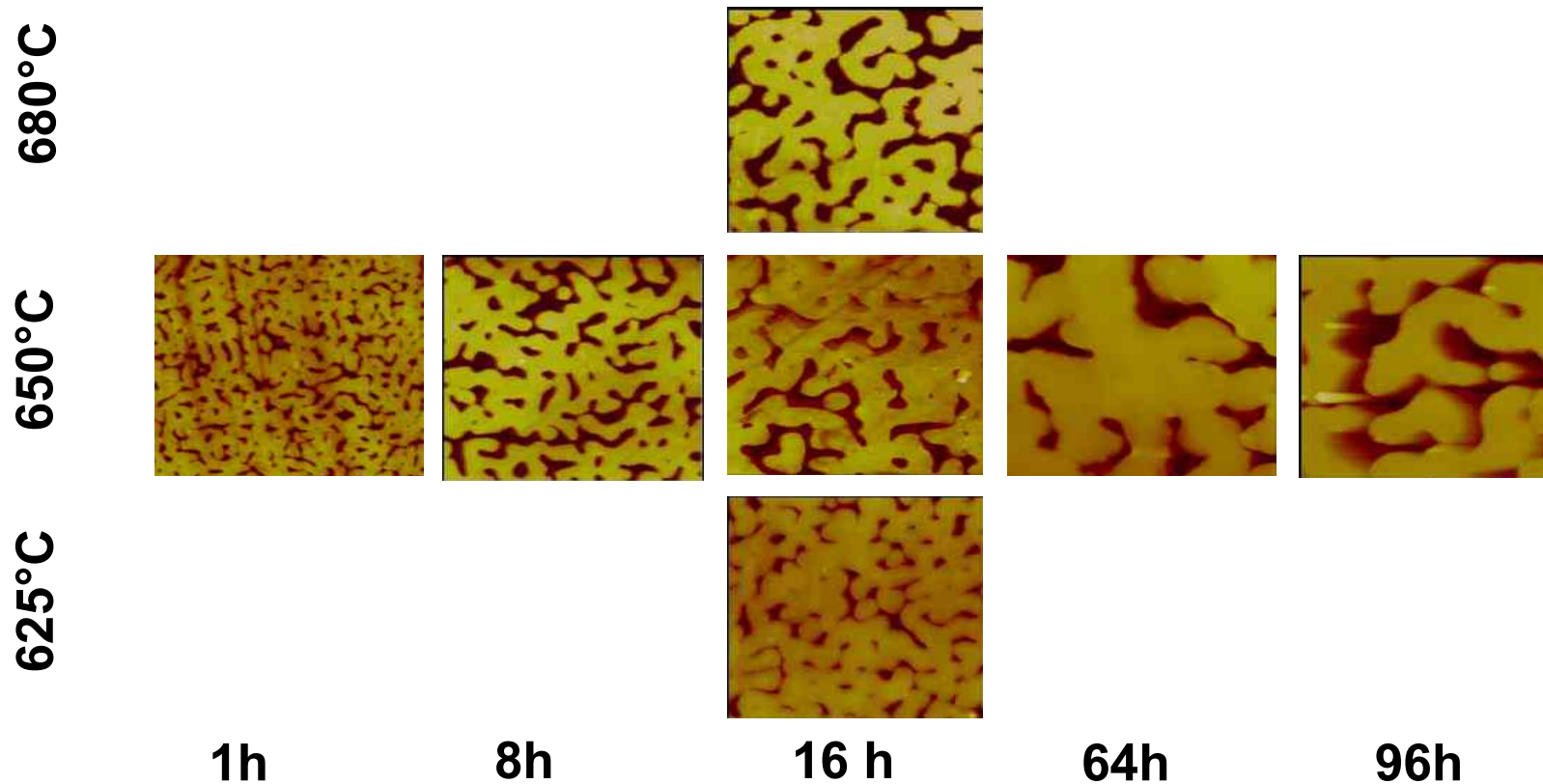
Séparation de phase dans les verres



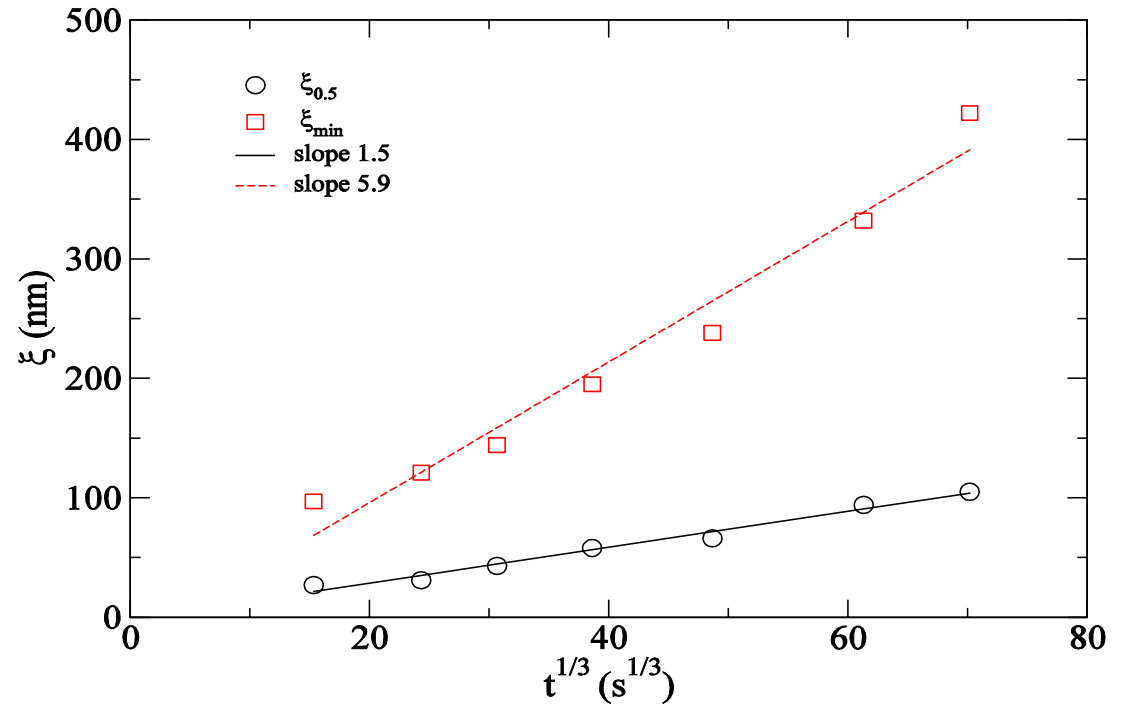
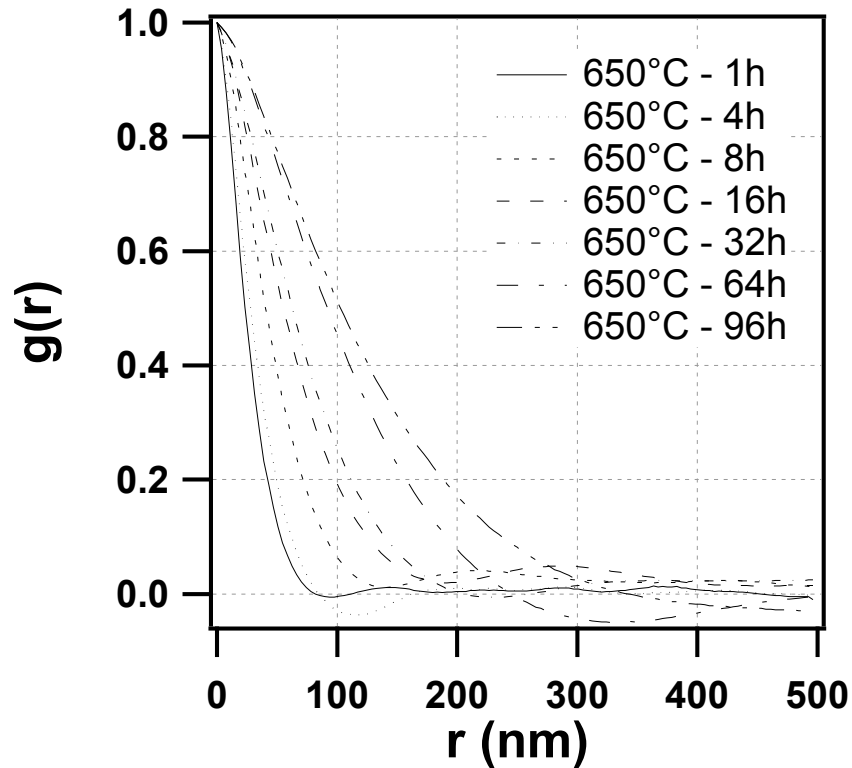
AFM image of a surface of a phase separated
alkaline borosilicate glass after selective etching
Lateral size: 4 μm, Z-scale: [-100:+100 nm]



Cinétique de croissance des domaines



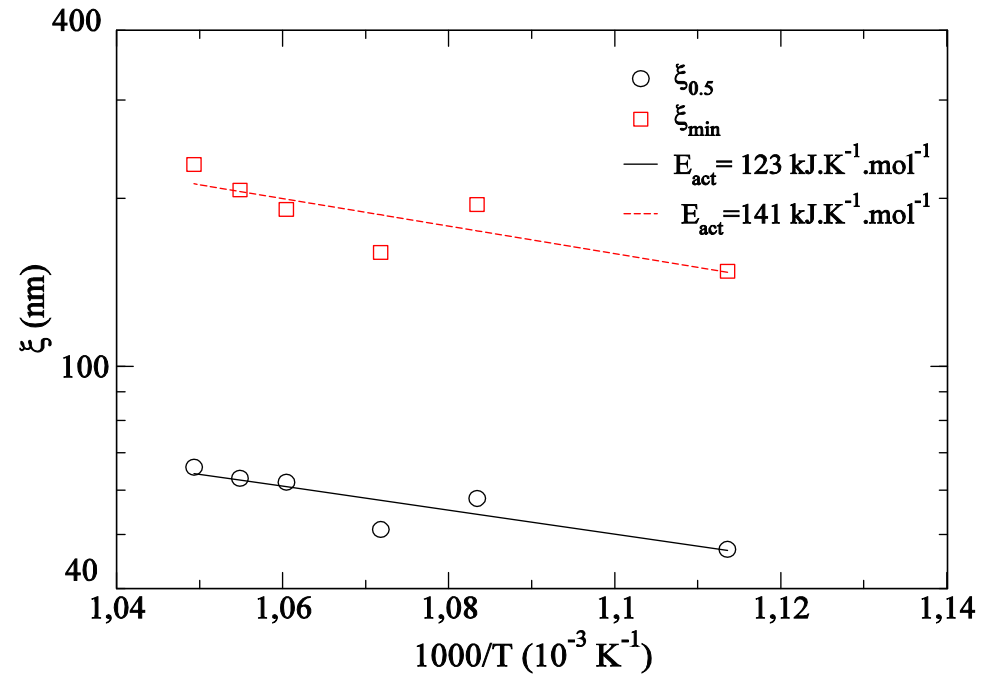
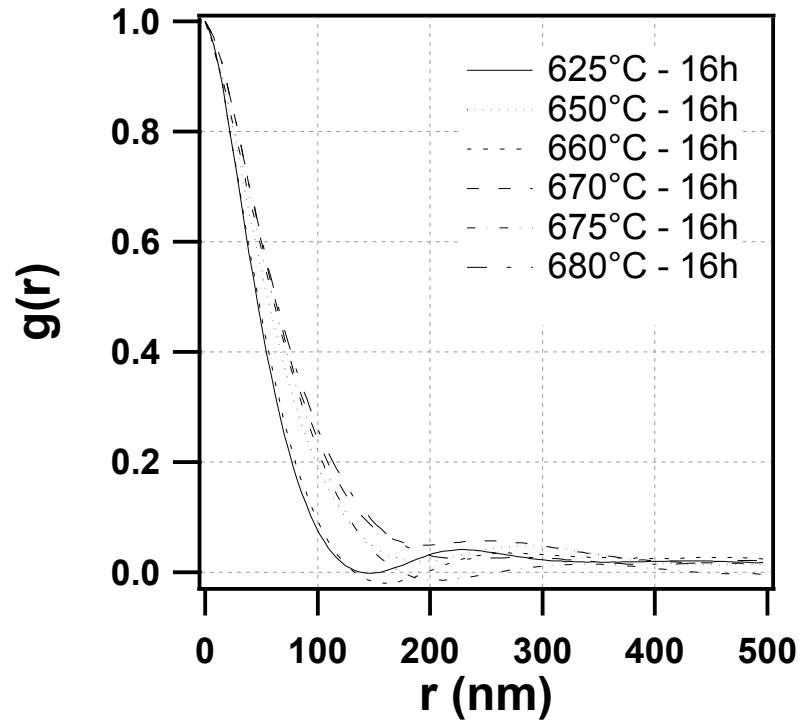
Loi d'échelle Lifshitz-Slyozhov-Wagner



$$R \approx (Kt)^{1/3}, \quad K \approx \frac{\gamma D v}{kT}$$

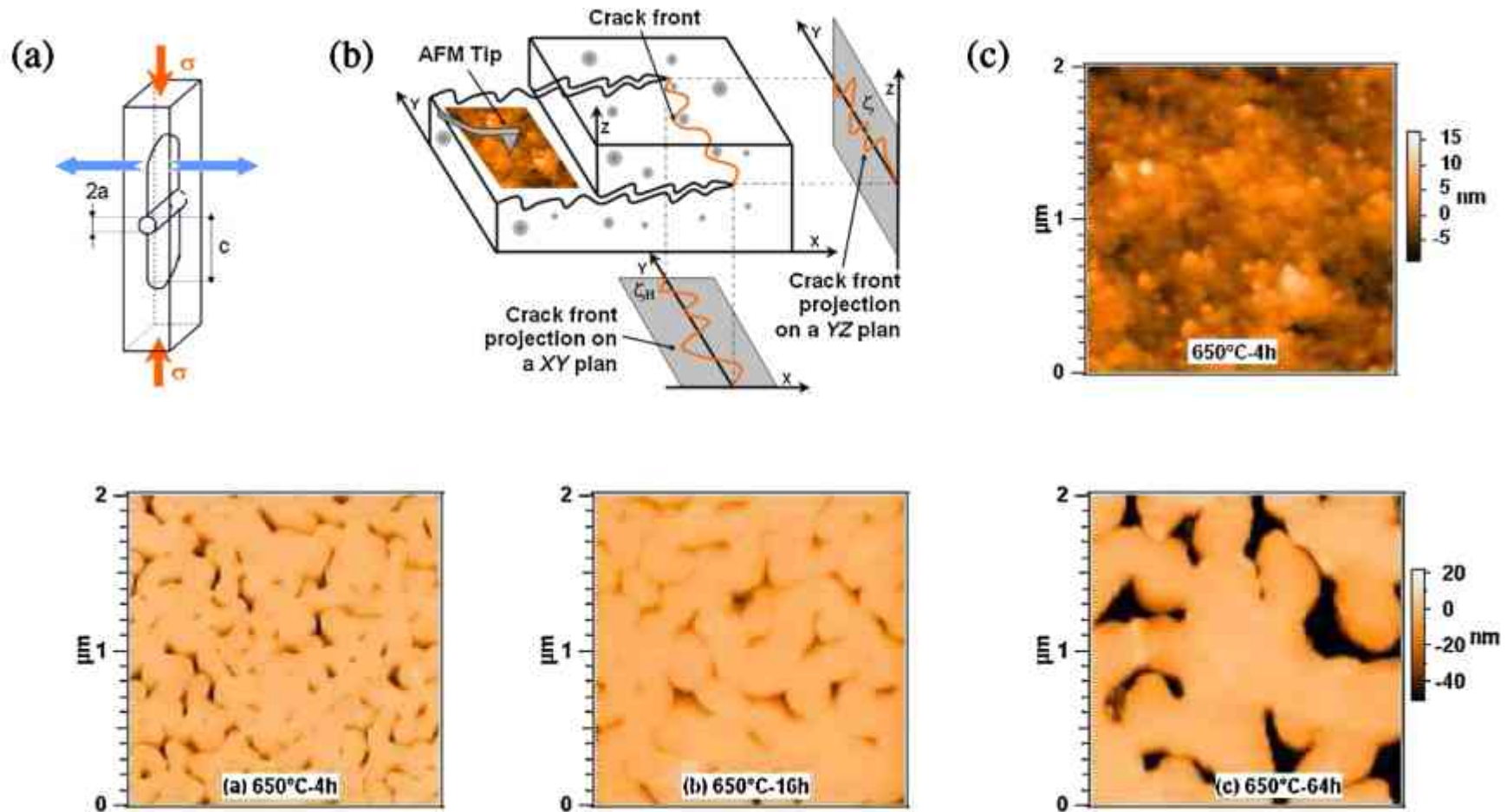
$$D \sim 10^{-16} \text{ cm s}^{-1}$$

Temperature dependence: Arrhenius behavior

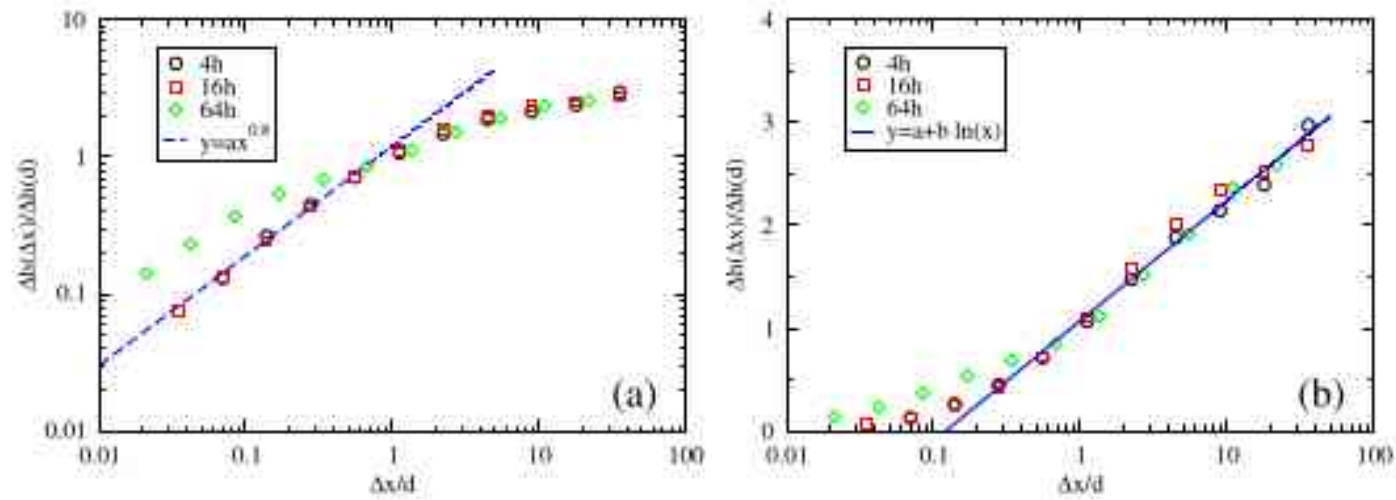


Estimate of activation energy from AFM measurements

Surface de fracture de verre démixé

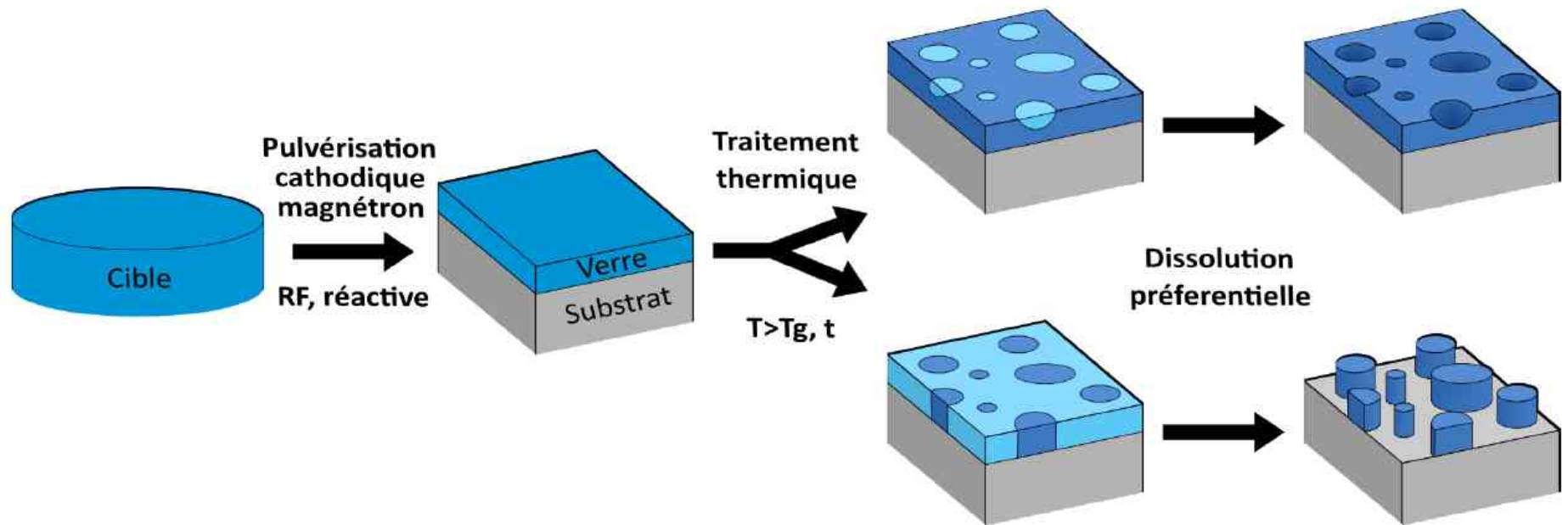


Rugosité de surface de fracture de verre

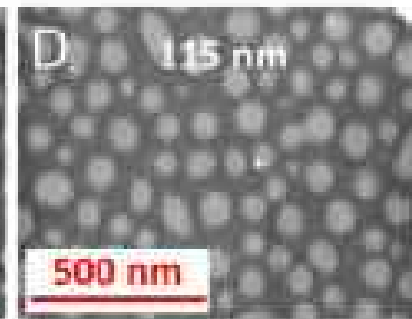
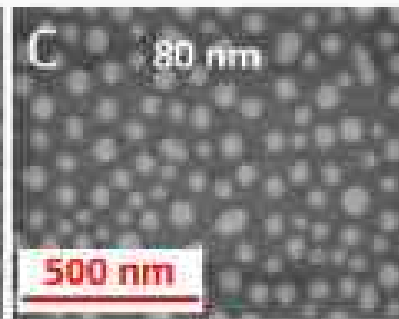
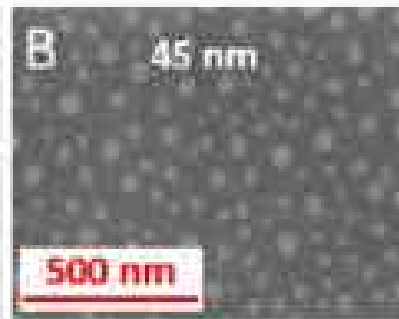
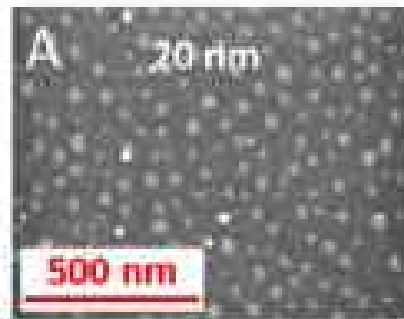
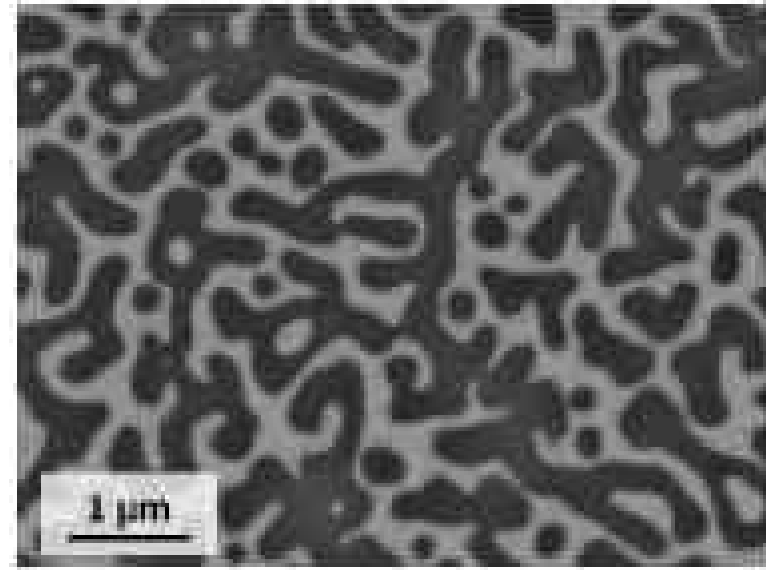
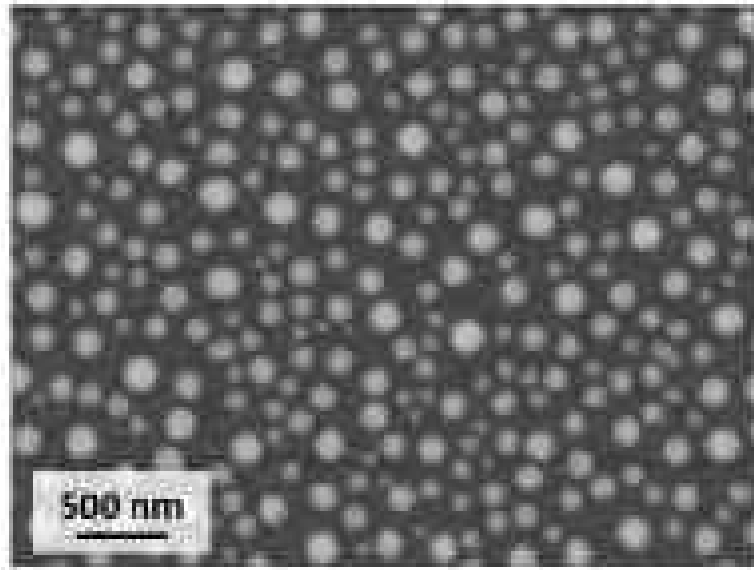


Démixion = 1 longueur de corrélation associée au mûrissement
Fracture : Corrélation de hauteurs logarithmiques aux grandes longueurs

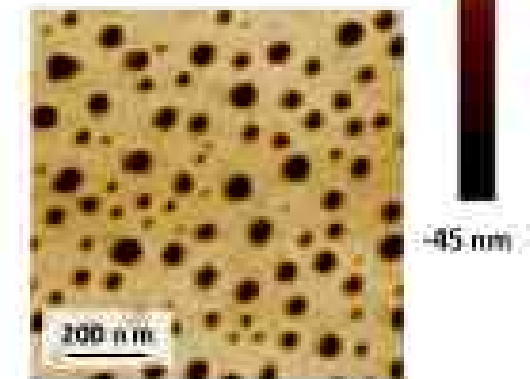
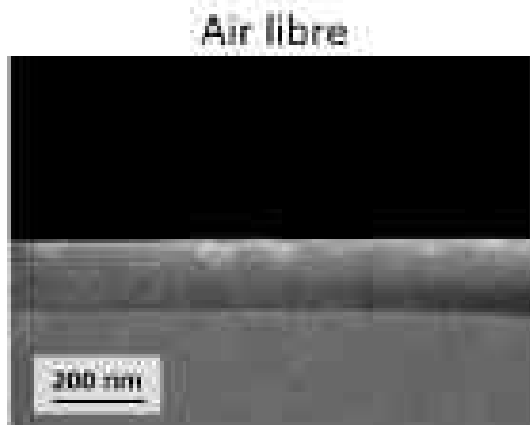
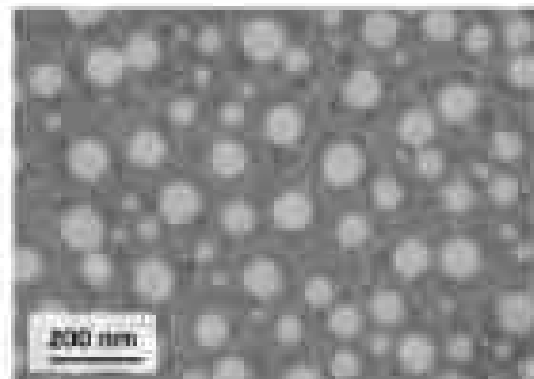
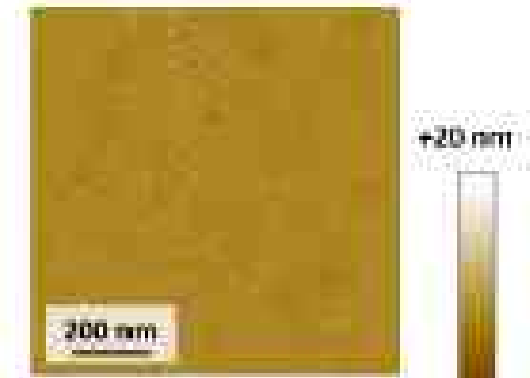
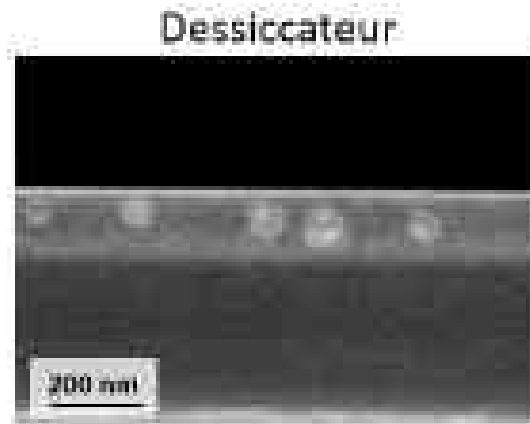
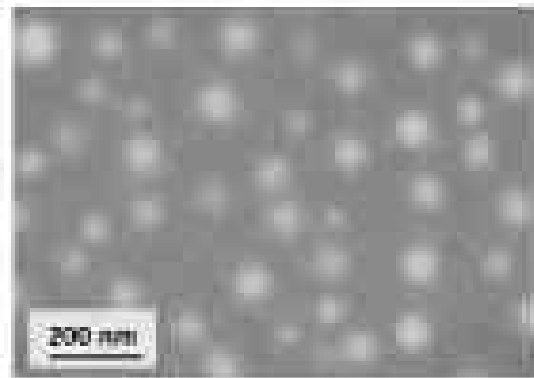
Texturation de surface par séparation de phase en couche mince



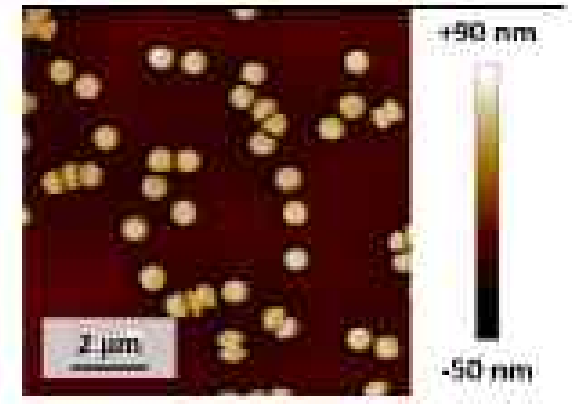
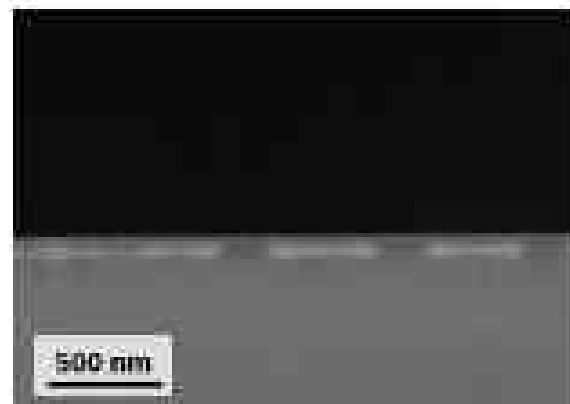
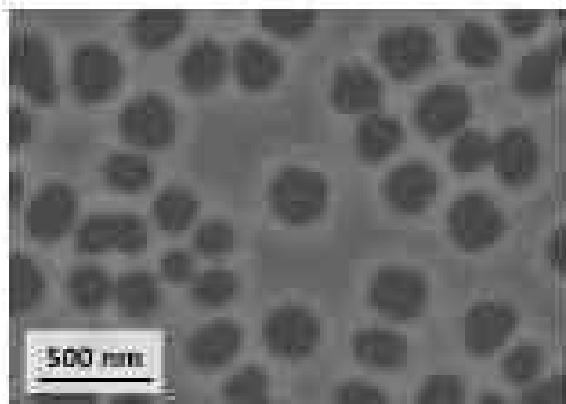
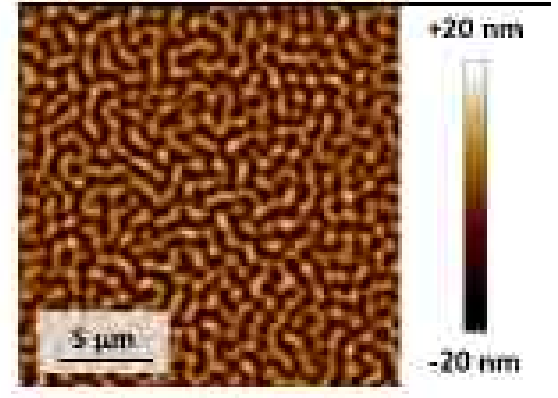
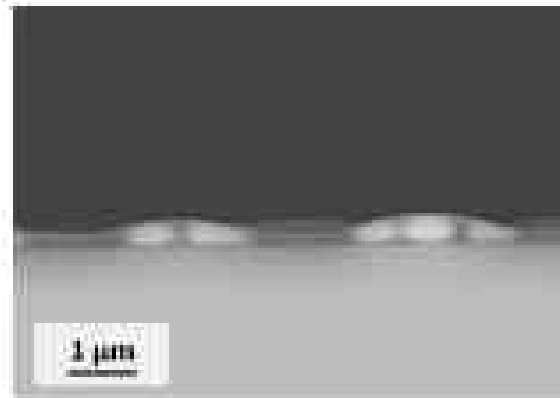
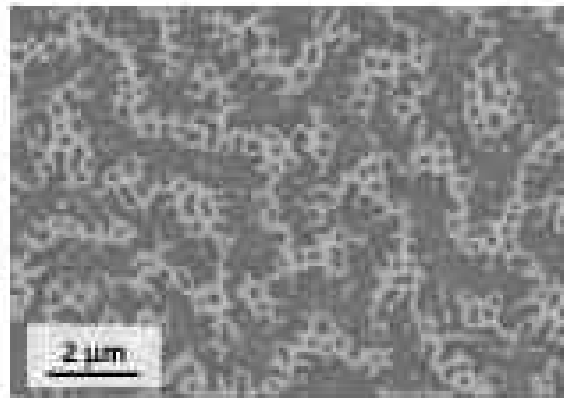
Variétés de tailles et de morphologie des domaines



MEB vs AFM

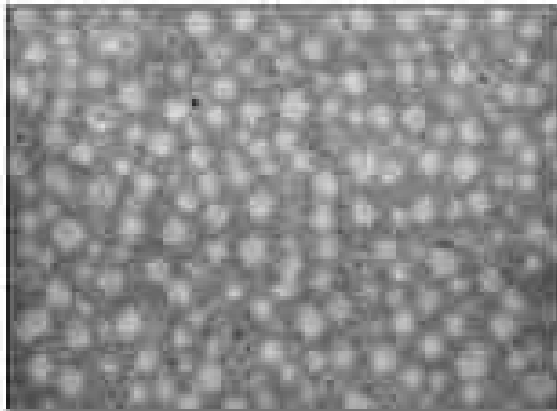


Différentes compositions, différentes texturations

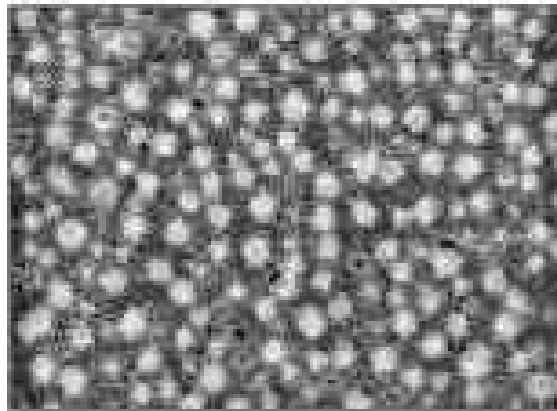


Traitement d'image

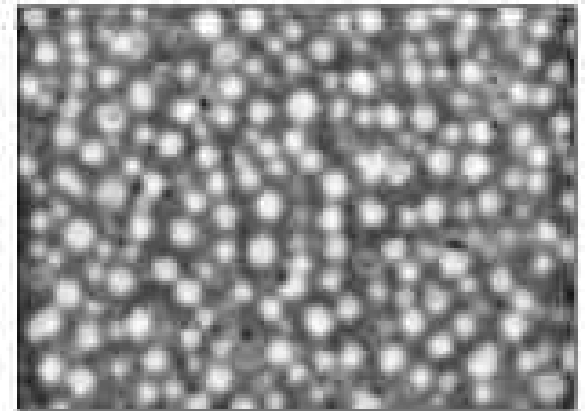
a Brut



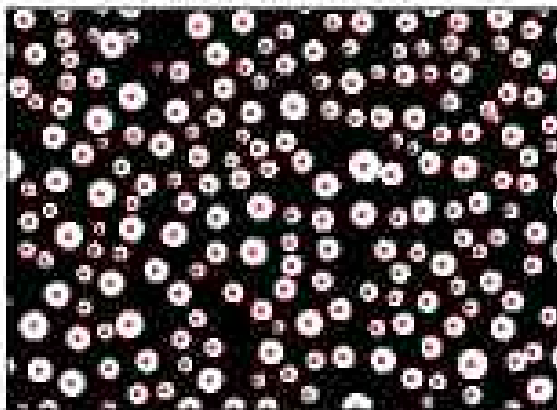
b Exposition



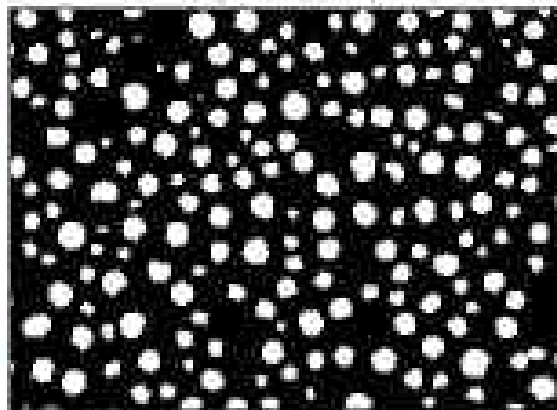
c Débruitage



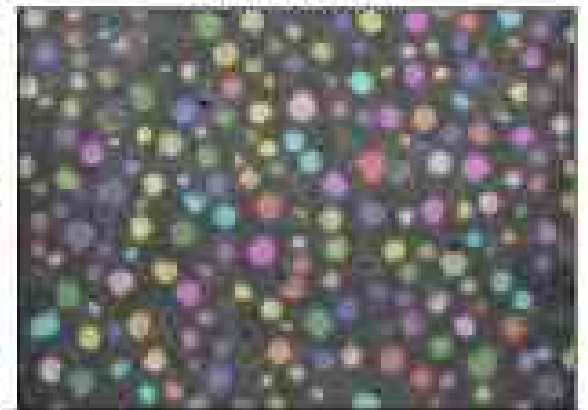
d Détection de blob



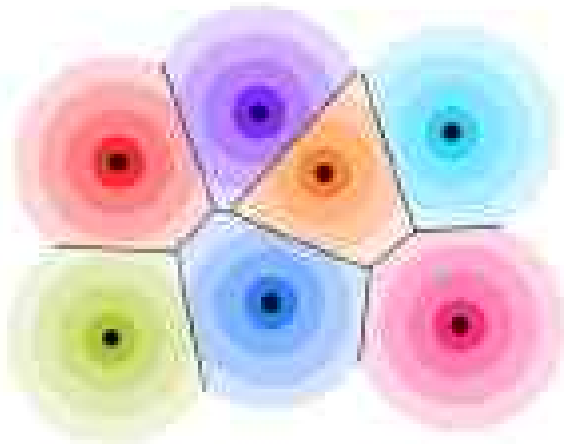
e Binarisation



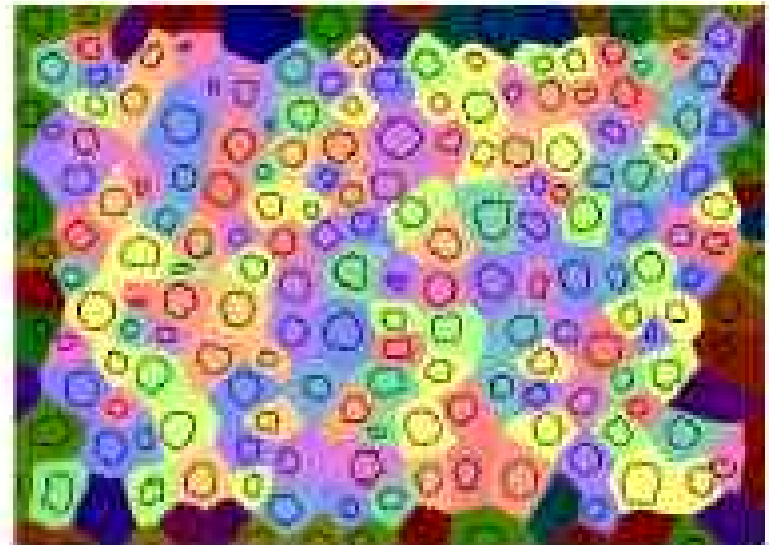
f Labélisation



Cellules de Voronoi

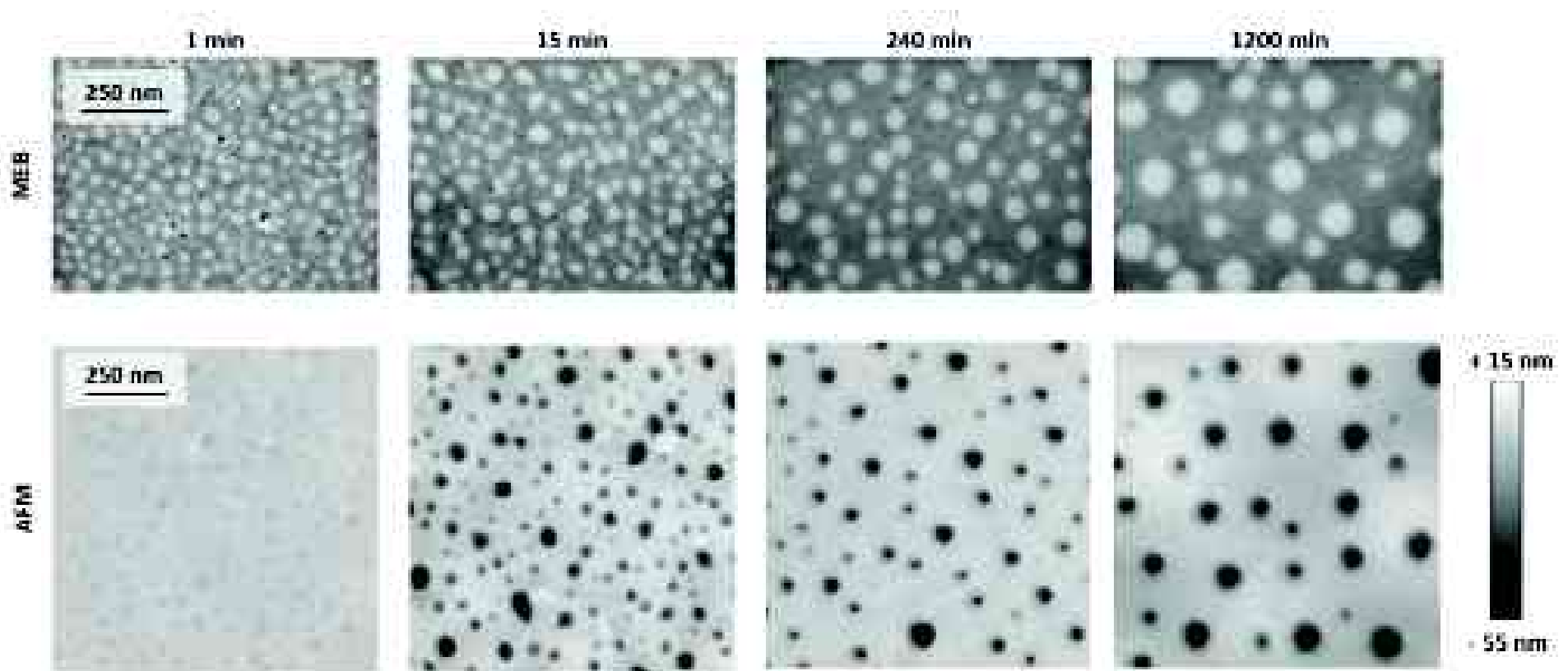


a Diagramme de Voronoï de centre à centre

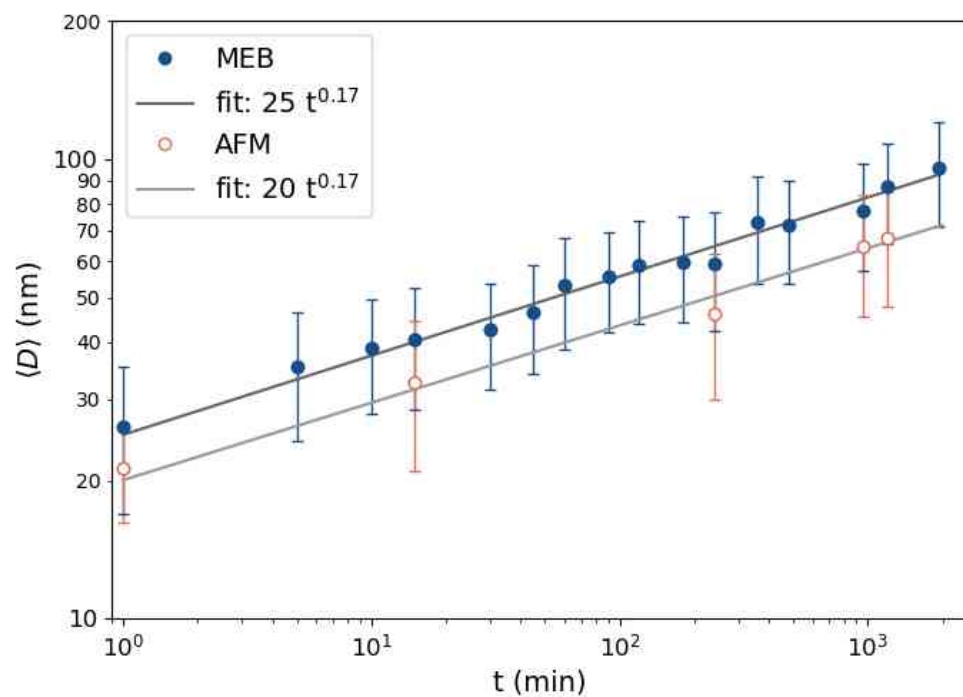


b Diagramme de Voronoï de bords à bords

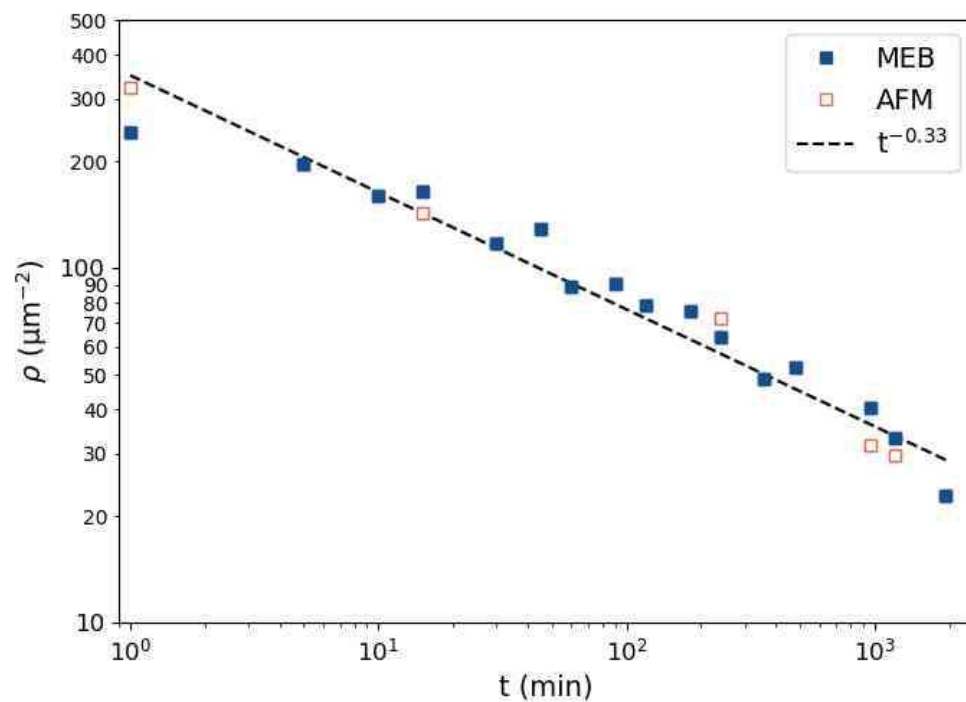
Croissance de domaines en couche mince



Cinétique (lente) de croissance

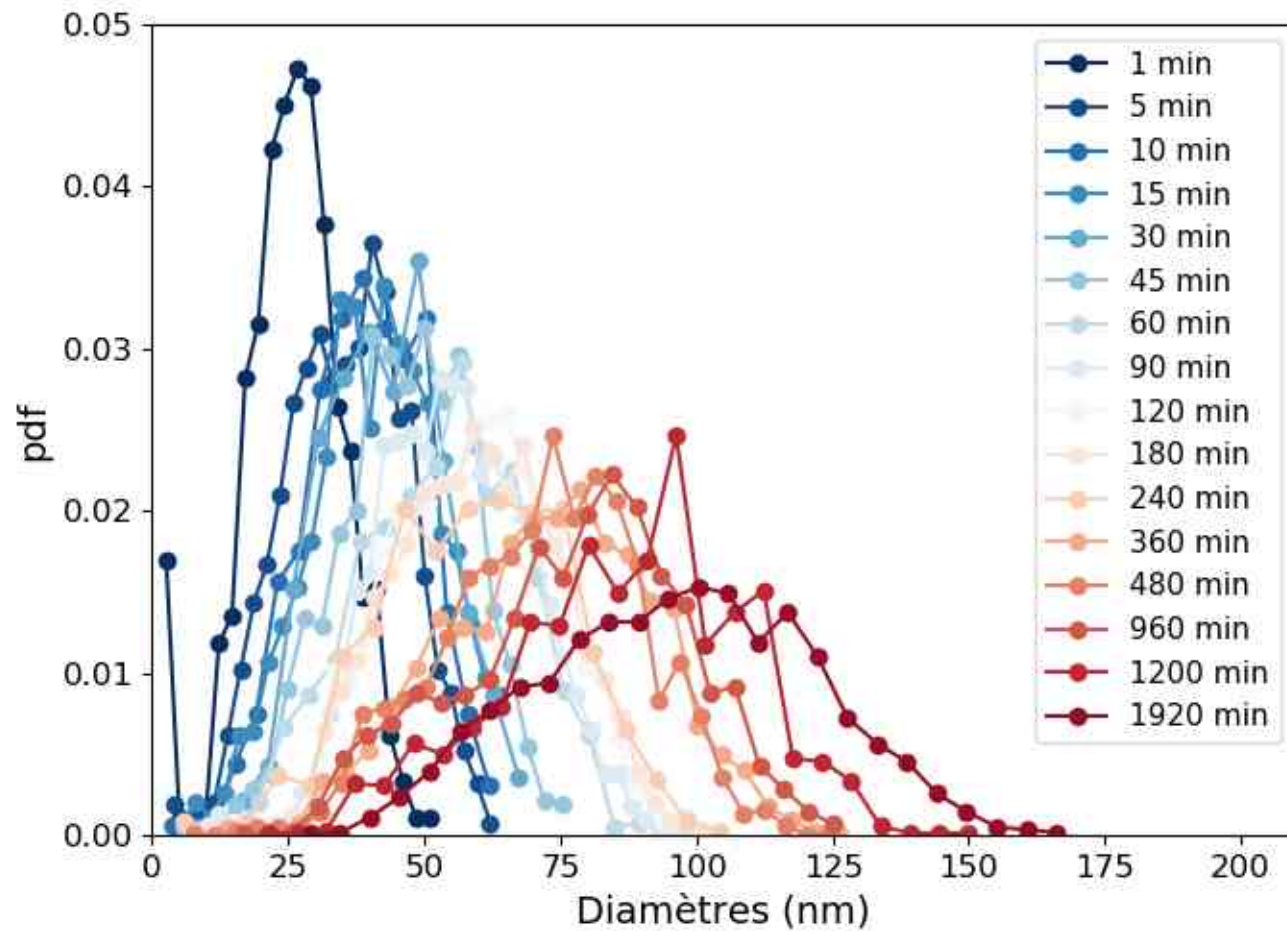


Diamètre Goutelettes

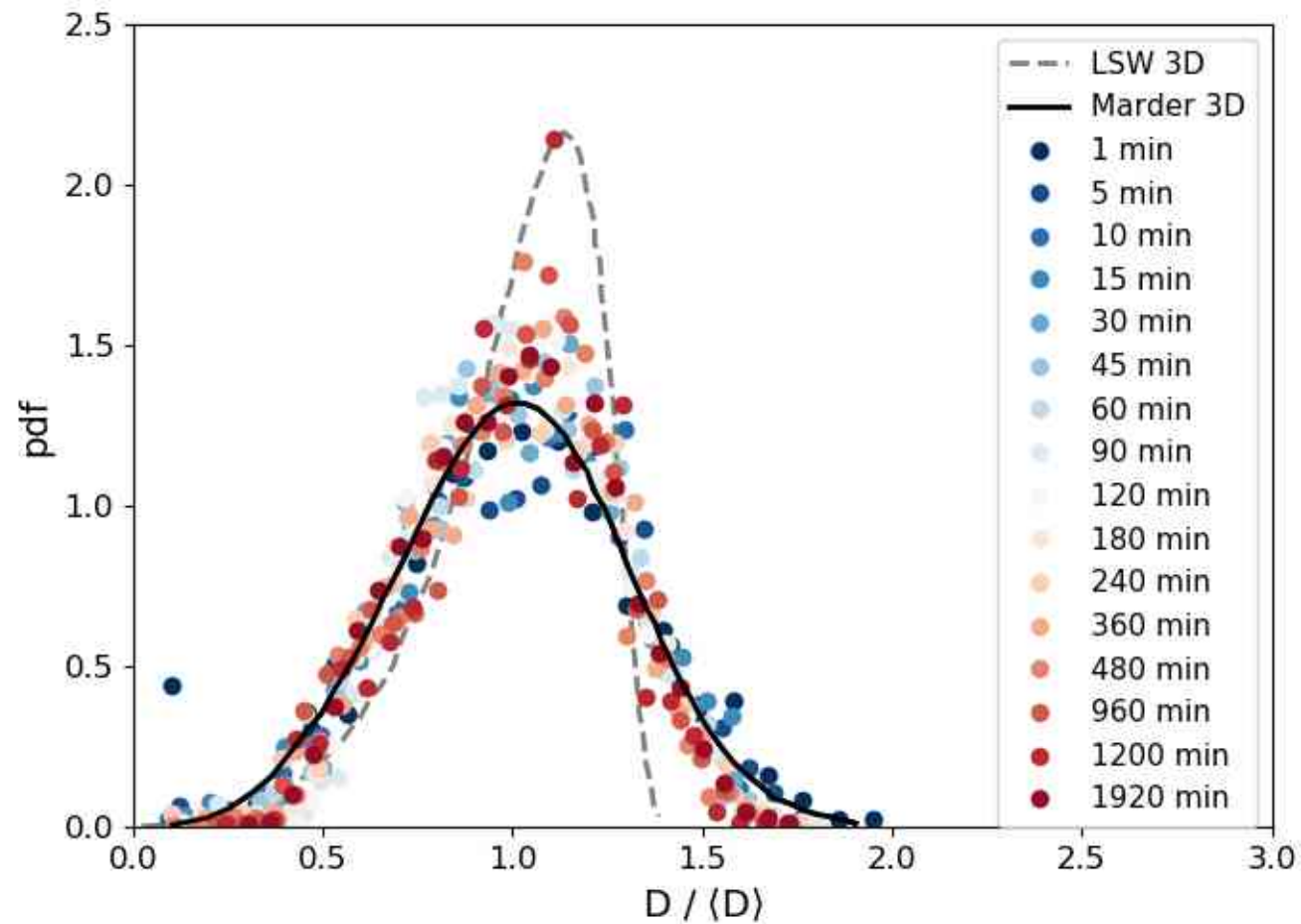


Densité Goutelettes

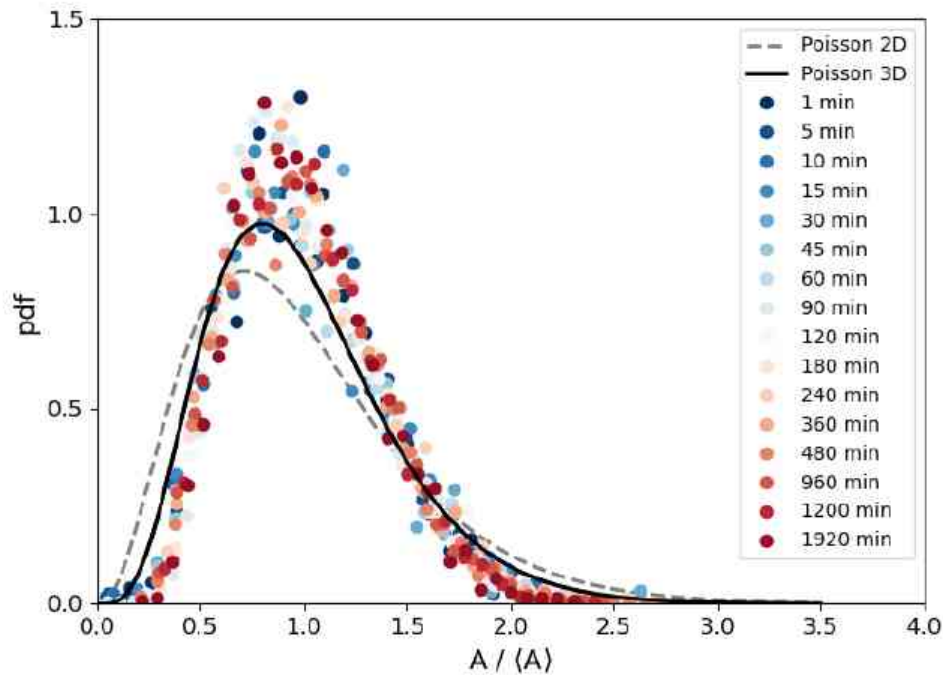
Evolution de la distribution de taille



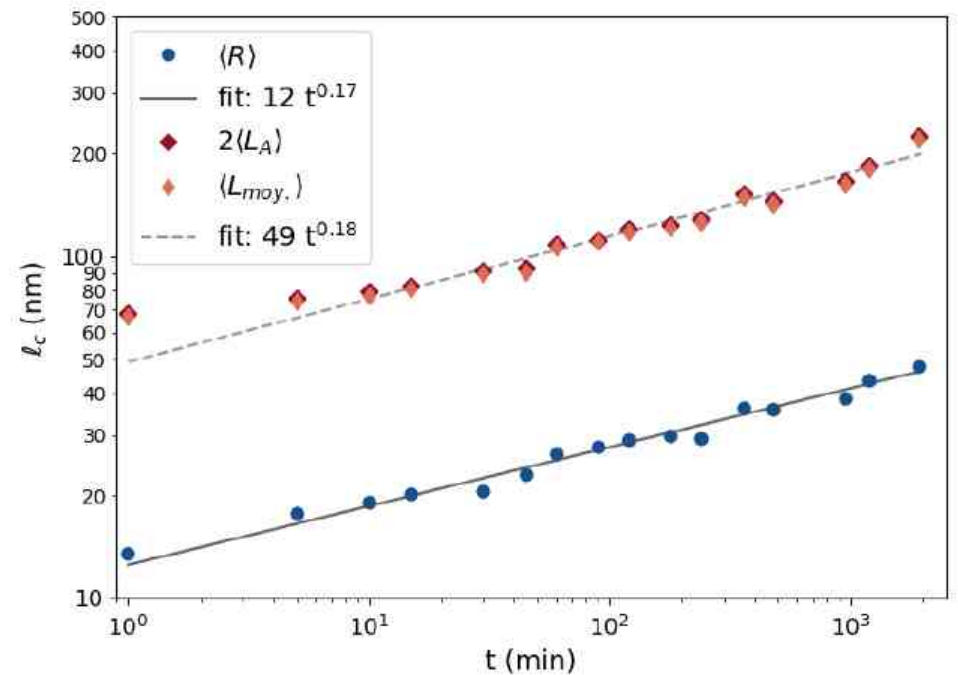
Distributions de tailles renormalisées



Cellules de Voronoi



Distribution renormalisée de l'aire des cellules de Voronoi



Evolution temporelle du rayon et de la distance inter-gouttelettes