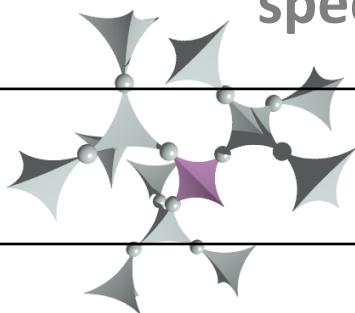


How to assess the glass structure

November 18-22, 2019

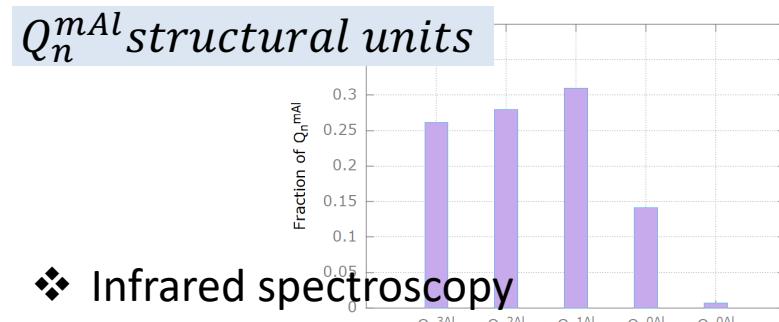
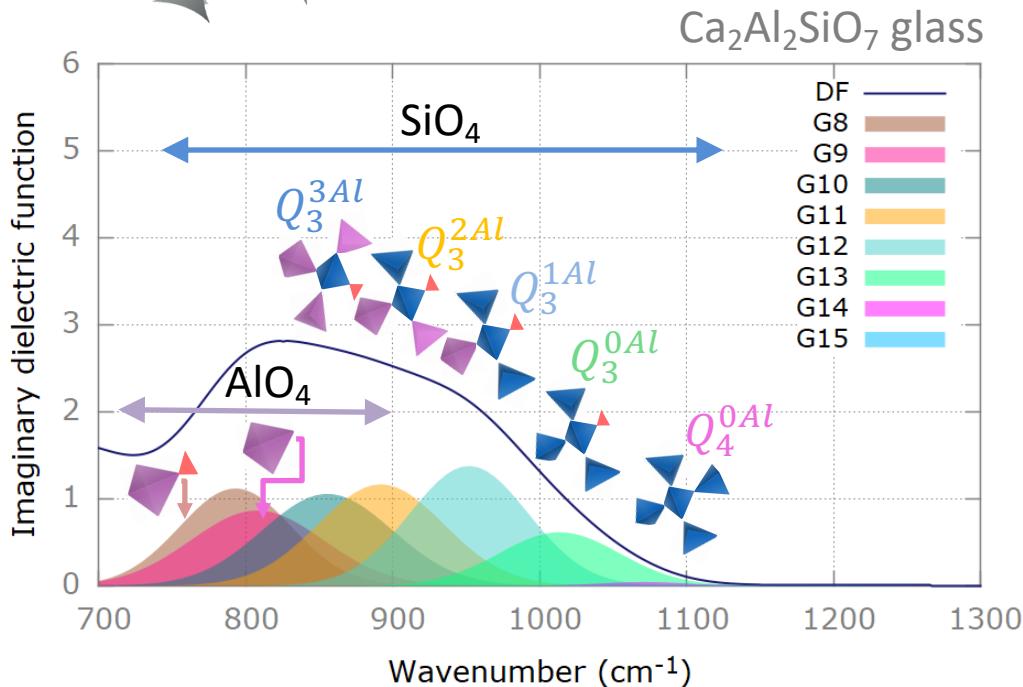


Contribution of infrared spectroscopy to the analysis of the glass structure

Domingos De Sousa Meneses

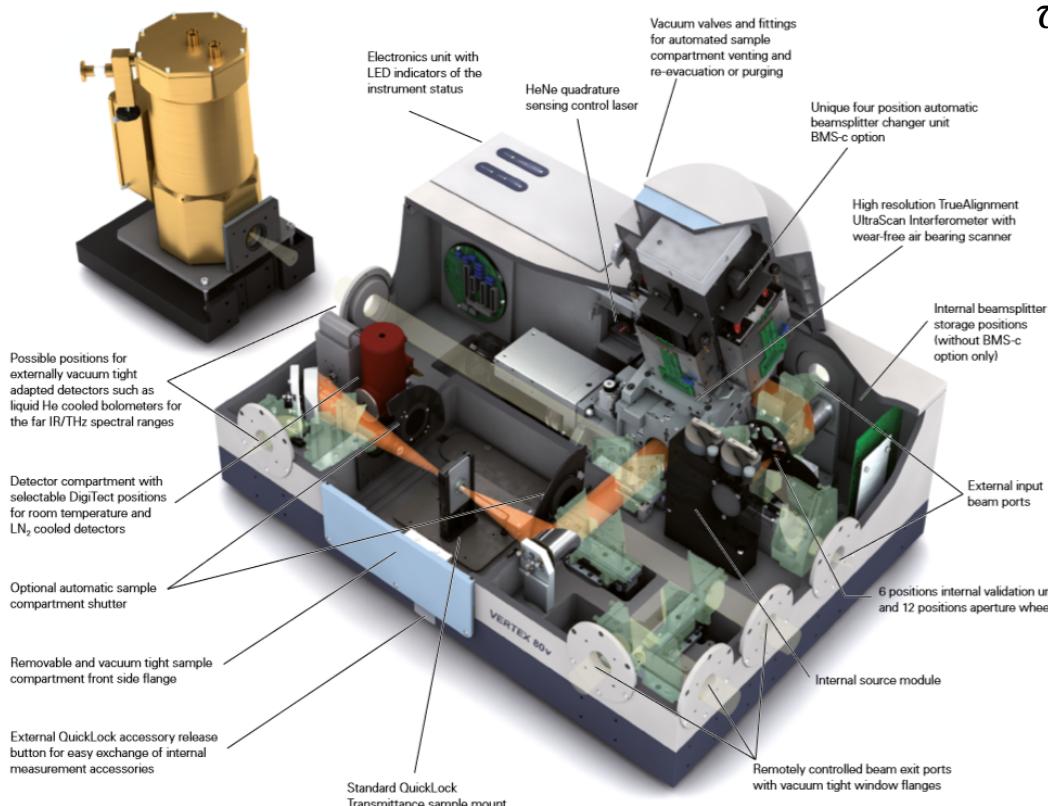
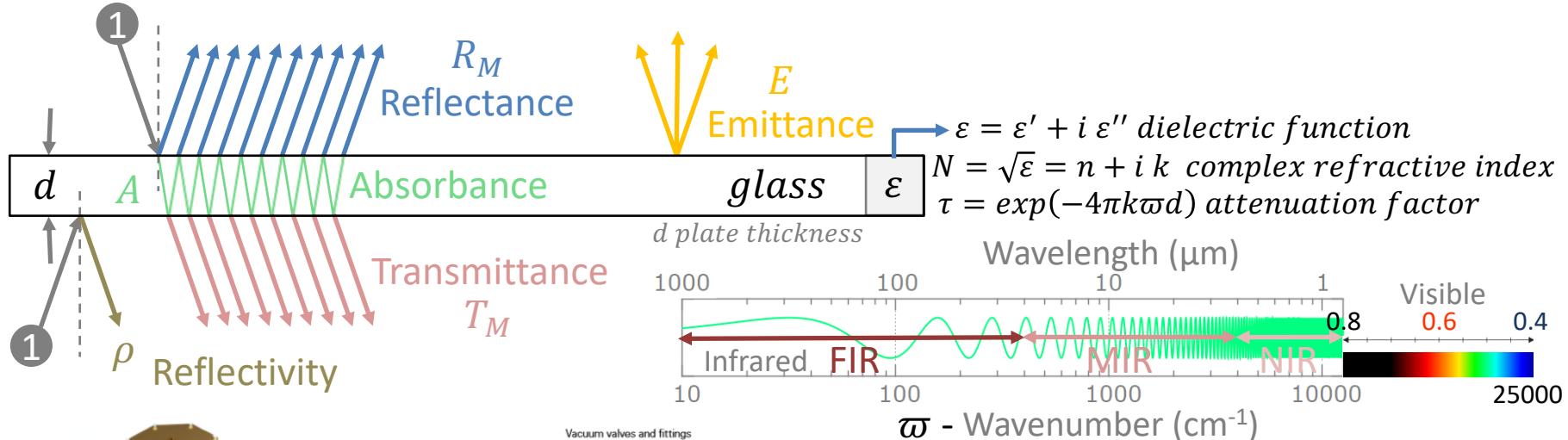
CEMHTI UPR3079 CNRS, Univ. Orléans, F-45071 Orléans, France

e-mail: desousa@cnrs-orleans.fr



- ❖ Infrared spectroscopy
- ❖ Retrieval of the optical functions
- ❖ Dielectric function models
- ❖ Focus software
- ❖ Origin of the vibrational modes
- ❖ Silicates glasses
- ❖ Aluminosilicate glasses
- ❖ Iron in silicate glasses and melts

Infrared spectroscopy



Experimental observables *

Parallel plate sufficiently thick to avoid the observation of interferences

$$\text{Reflectivity } \rho = \frac{(n - 1)^2 + k^2}{(n + 1)^2 + k^2}$$

$$\text{Reflectance } R_M = \rho \left[1 + \frac{(1 - \rho)^2 \tau^2}{1 - \rho^2 \tau^2} \right]$$

$$\text{Transmittance } T_M = \tau \frac{1 - \rho}{1 + \rho} \frac{1 - \rho^2}{1 - \rho^2 \tau^2}$$

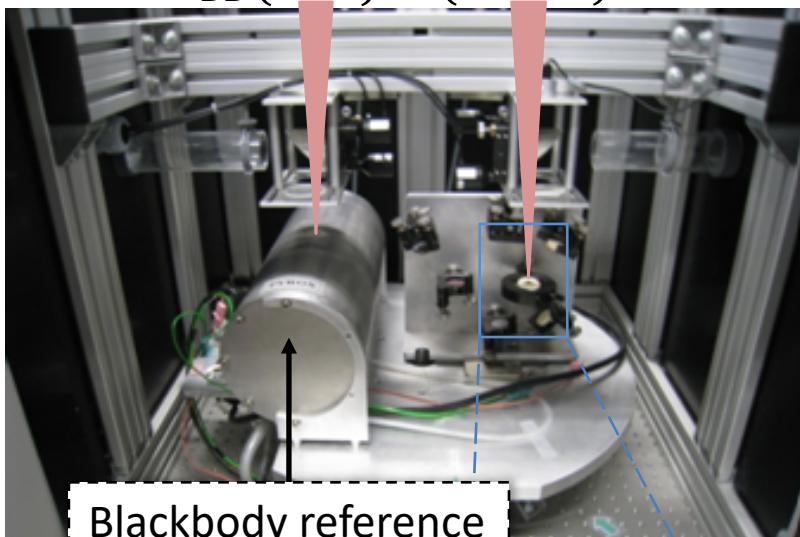
Absorbance and Emittance

$$E = A = 1 - R_M - T_M = \frac{(1 - \rho)(1 - \tau)}{1 - \rho \tau}$$

* Measurement at near-normal incidence

Emittance measurement

$$L_{BB}(\varpi, \hat{T}) \quad L(\varpi, \hat{T}, \theta)$$



Directional spectral emittance measurement

Ratio of the intensities emitted by the sample and a blackbody in the same conditions

$$E(\varpi, \hat{T}, \theta) = \frac{L(\varpi, \hat{T}, \theta)}{L_{BB}(\varpi, \hat{T})}$$

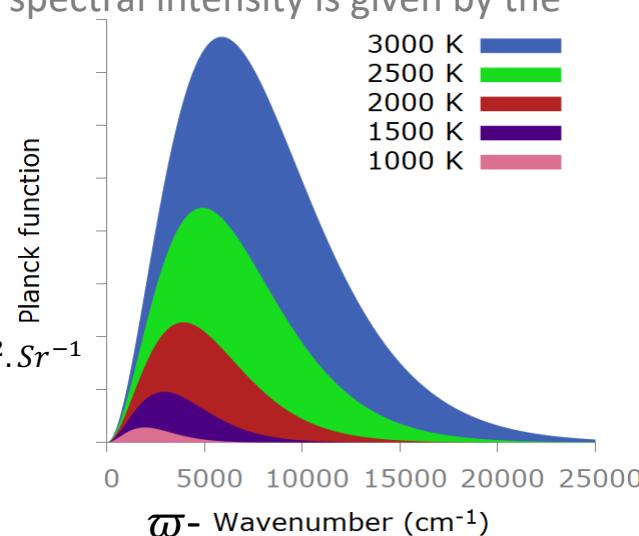


\hat{T} : temperature

Blackbody

Ideal radiator whose spectral intensity is given by the Planck's law

$$L_{BB}(\varpi, \hat{T}) = \frac{C_1 \varpi^3}{\exp\left(\frac{C_2 \varpi}{\hat{T}}\right) - 1}$$



$$C_1 = 1,191043 \cdot 10^{-16} \text{ W.m}^2.\text{Sr}^{-1}$$

$$C_2 = 0,01438777 \text{ mK}$$

Kirchhoff's law

At LTE, spectral absorptance A and emittance are equal

$$A(\varpi) = E(\varpi)$$

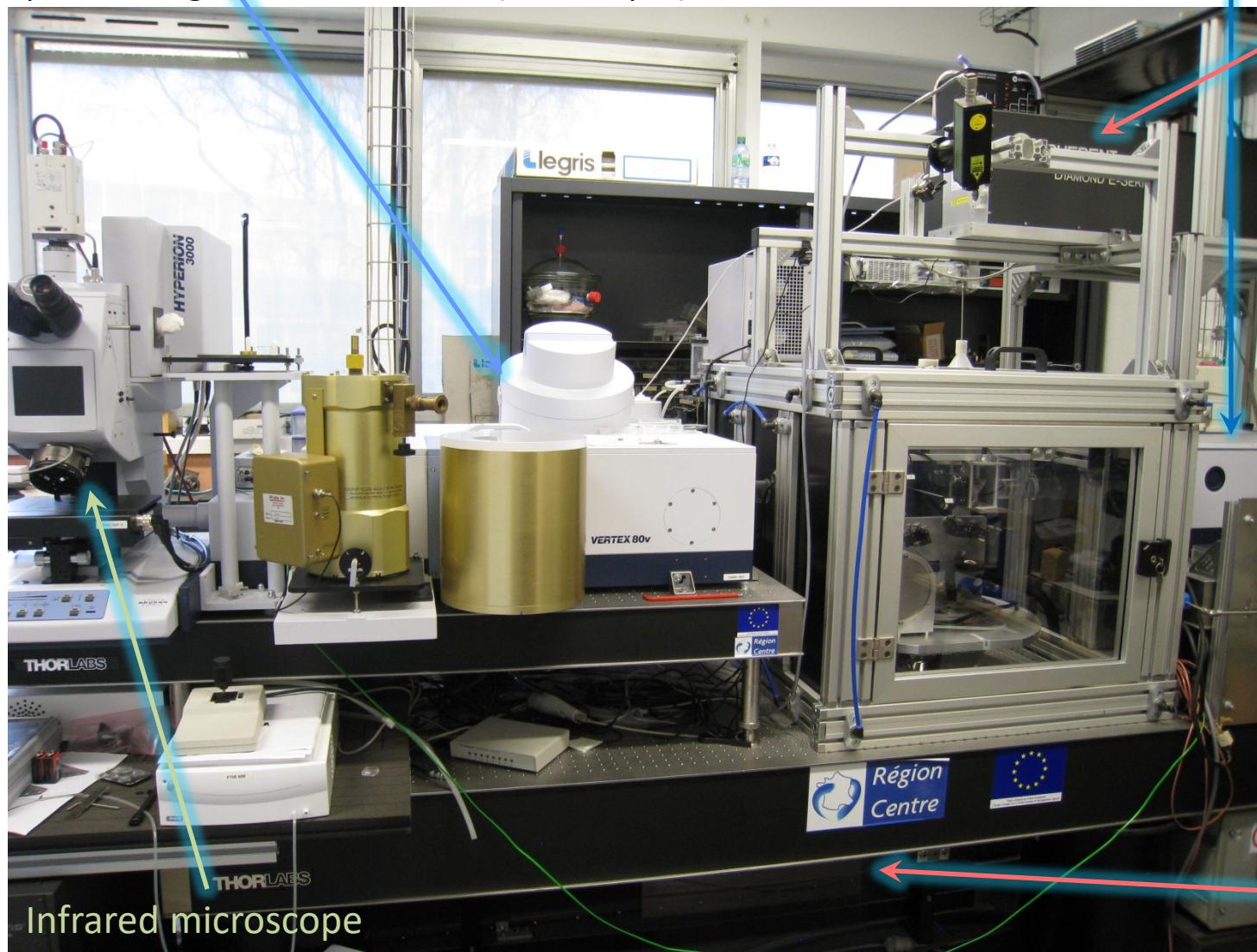
CO₂ laser



Infrared emission spectrometer

Bruker Vertex 80v and Vertex 70

Spectral range : [20-20 000 cm^{-1}](500-0.5 μm)

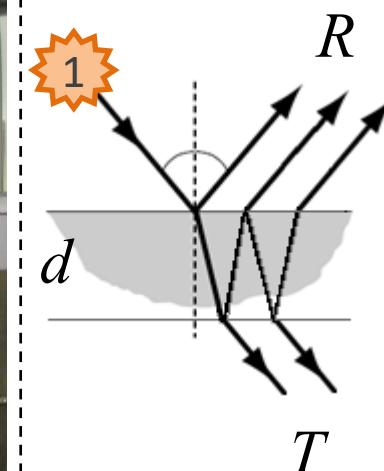


CO₂ laser (500W)
[400 - 3000 K]

Measurements

Reflection R

Transmission T



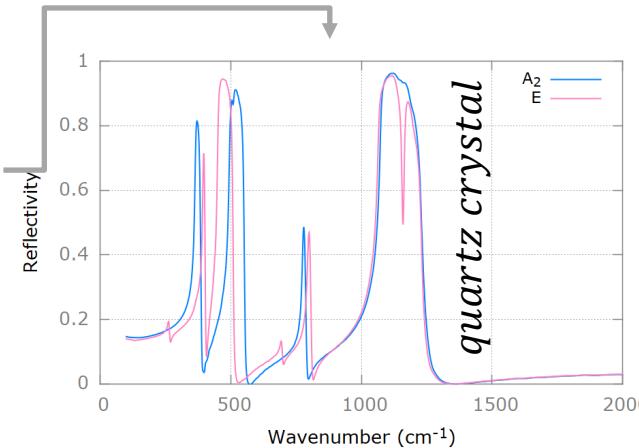
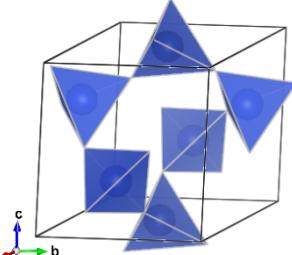
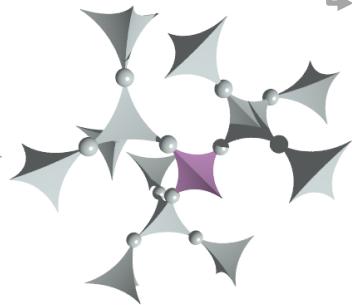
Emission E

CO₂ laser (500W)
[400 - 3000 K]

Infrared spectroscopy

SiO_2

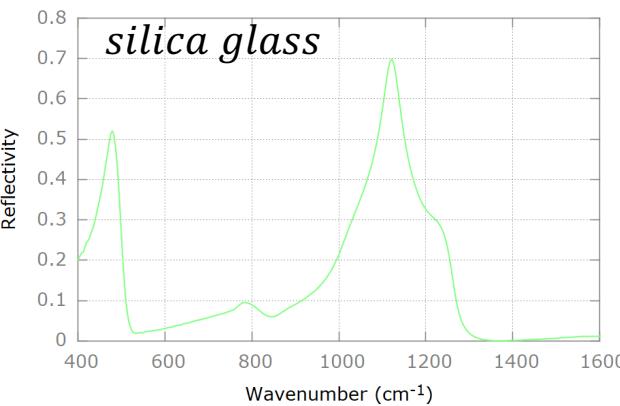
Reflectivity - ρ



Single crystal

Anisotropic infrared response.

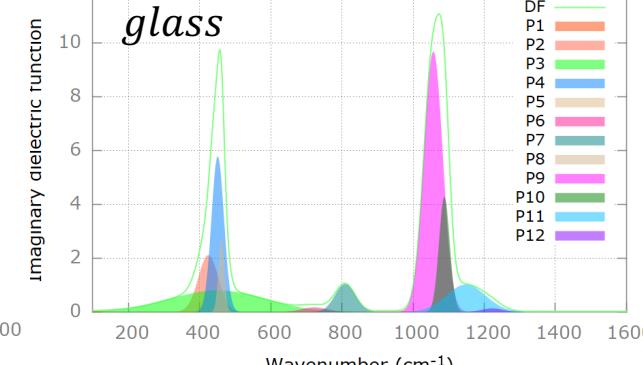
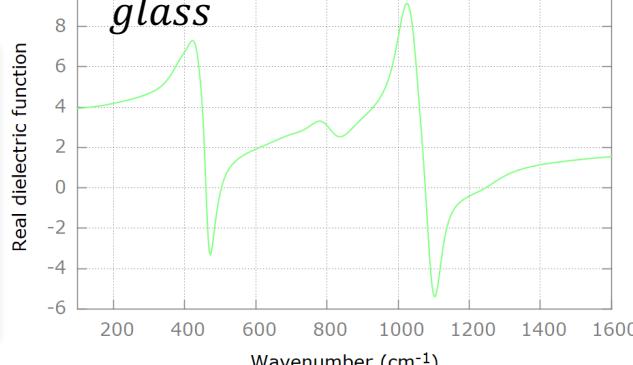
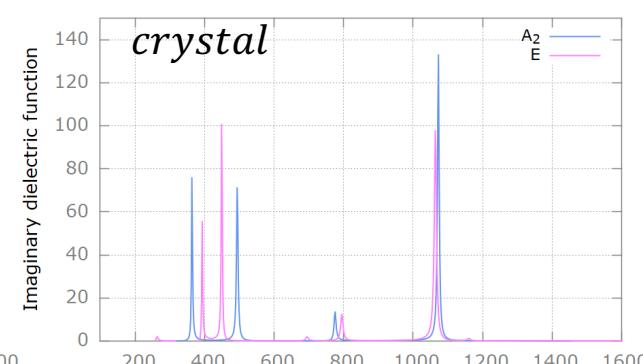
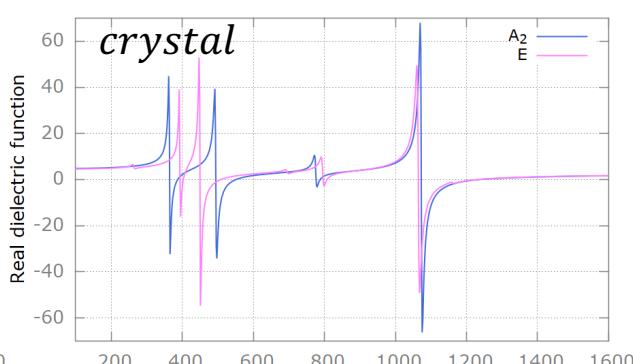
Activity of normal modes (phonons) fixed by crystal symmetry and infrared spectroscopy selection rules



Glass

Isotropic infrared response.

The complexity of the glass structure is revealed by its polar vibrational dynamics.



From experimental observables to physical properties

Complex refractive index extraction – inversion methods

IR-VISIBLE-UV **spectroscopies**

Ellipsometry

	R_p	R_s	ρ	R_M	T_M	E	ψ	Δ
R_p								
R_s								
ρ								
R_M								
T_M								
E								
ψ								
Δ								

Several inversion methods necessitates the knowledge of two experimental quantities.

Under certain conditions, 1 measure may be sufficient to determine the indices

Semi-transparent media

$$\begin{matrix} R_M \\ T_M \end{matrix}$$

$$\begin{matrix} R_M \\ E \end{matrix}$$

$$T_M = 1 - R_M \cdot E$$

$$\begin{matrix} T_M \\ E \end{matrix}$$

$$R_M = 1 - T_M \cdot E$$

$$\rho = \frac{R_M(R_M - 2) - T_M^2 - 1 + \sqrt{[1 + T_M^2 - R_M(R_M - 2)]^2 + 4R_M(R_M - 2)}}{2(R_M - 2)}$$

$$\tau = \frac{1}{T_M} \left(\frac{R_M}{\rho} - 1 \right)$$



$$n(\varpi) = \frac{1 + \rho(\varpi) + \sqrt{4\rho(\varpi) - (\rho(\varpi) - 1)^2 k(\varpi)^2}}{1 - \rho(\varpi)}$$

$$k(\varpi) = -\frac{\ln(\tau(\varpi))}{4\pi\varpi d}$$

Semi-infinite media

$$\begin{matrix} \psi, \Delta \end{matrix}$$

$$n(\varpi) + ik(\varpi) = \sin(\theta_0) \sqrt{1 + \left[\frac{1 + \tan(\Psi(\varpi))e^{i\Delta(\varpi)}}{1 - \tan(\Psi(\varpi))e^{i\Delta(\varpi)}} \right]^2} \tan^2(\theta_0)$$

θ_0 : angle of incidence

KK

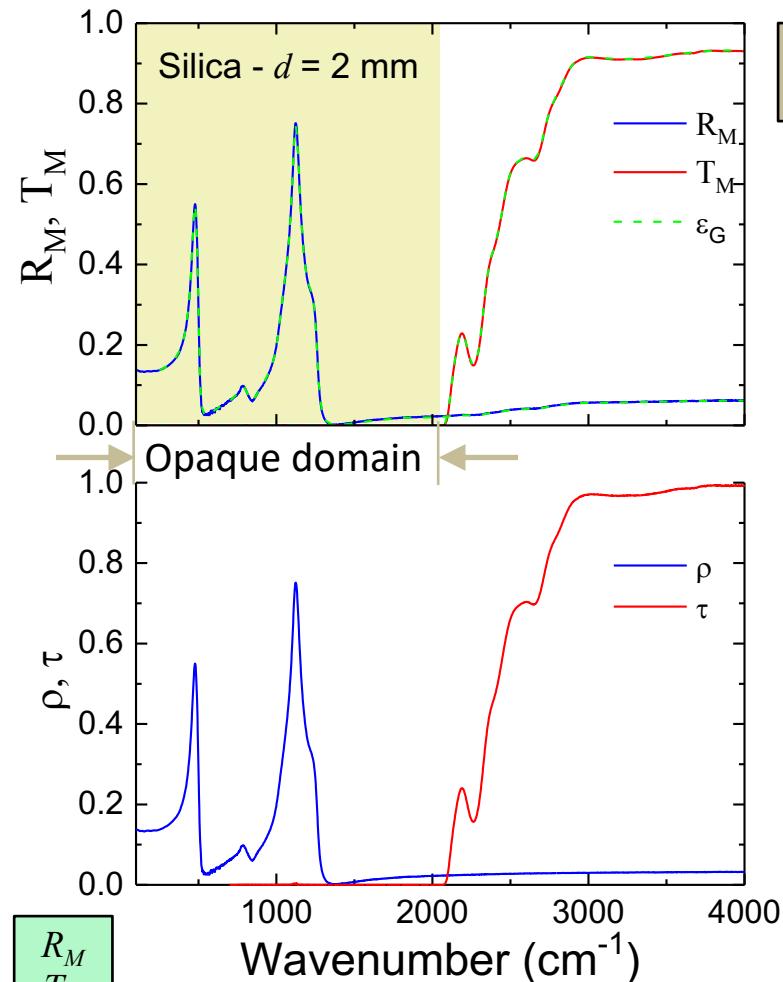
Inversion method using the Kramers-Kronig relations

$$\delta(\varpi_a) = \frac{1}{2\pi} \int_0^\infty \ln \left| \frac{\varpi - \varpi_a}{\varpi + \varpi_a} \right| \frac{d}{d\varpi} \ln[\rho(\varpi)] d\varpi \quad n(\varpi) = \frac{1 - \rho(\varpi)}{1 + \rho(\varpi) - 2\sqrt{\rho(\varpi)} \cdot \cos[\delta(\varpi)]} \quad k(\varpi) = \frac{2\sqrt{\rho(\varpi)} \cdot \sin[\delta(\varpi)]}{1 + \rho(\varpi) - 2\sqrt{\rho(\varpi)} \cdot \cos[\delta(\varpi)]}$$

D. De Sousa Meneses, J-F. Brun, P. Echegut, P. Simon Applied Spectroscopy 58 (2004) 969-974

Kramers-Kronig Relations in Optical Materials Research, Lucarini, V., Saarinen, J.J., Peiponen, K.-E., Vartiainen, E.M. Springer Series in Optical Sciences, Vol. 110 (2005)

Complex refractive index extraction – inversion methods



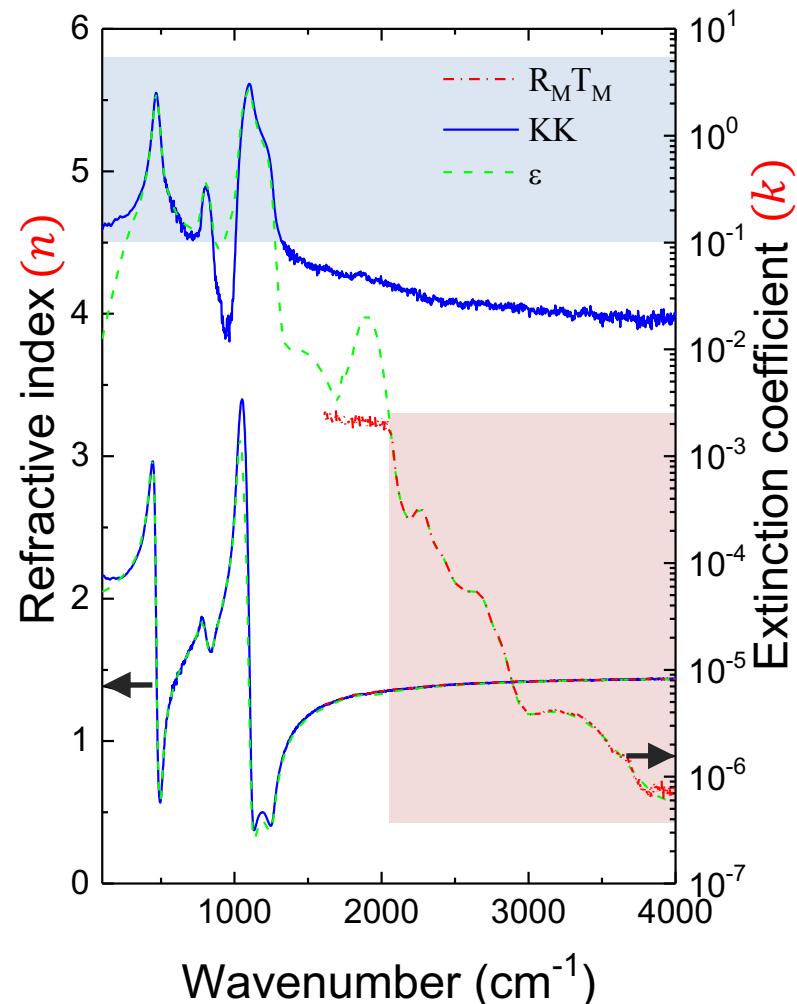
$$\rho = \frac{R_M(R_M - 2) - T_M^2 - 1 + \sqrt{[1 + T_M^2 - R_M(R_M - 2)]^2 + 4R_M(R_M - 2)}}{2(R_M - 2)}$$

$$\tau = \frac{1}{T_M} \left(\frac{R_M}{\rho} - 1 \right)$$

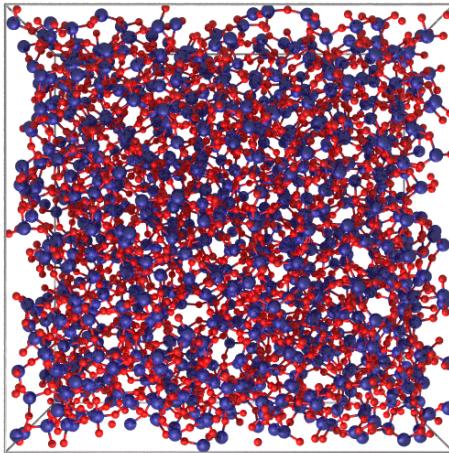
$$n(\omega) = \frac{1 + \rho(\omega) + \sqrt{4\rho(\omega) - (\rho(\omega) - 1)^2 k(\omega)^2}}{1 - \rho(\omega)} \quad k(\omega) = -\frac{\ln(\tau(\omega))}{4\pi\omega d}$$

$$\delta(\omega_a) = \frac{1}{2\pi} \int_0^\infty \ln \left| \frac{\omega - \omega_a}{\omega + \omega_a} \right| \frac{d}{d\omega} \ln[\rho(\omega)] d\omega$$

$$n(\omega) = \frac{1 - \rho(\omega)}{1 + \rho(\omega) - 2\sqrt{\rho(\omega)} \cdot \cos[\delta(\omega)]} \quad k(\omega) = \frac{2\sqrt{\rho(\omega)} \cdot \sin[\delta(\omega)]}{1 + \rho(\omega) - 2\sqrt{\rho(\omega)} \cdot \cos[\delta(\omega)]}$$



Dielectric function models – disordered media



Lorentz model

Single crystals

$$\varepsilon(\omega) = \varepsilon_{\infty} + \sum_j \frac{S_j \omega_j^2}{\omega_j^2 - \omega^2 - i\gamma_j \omega}$$

The Lorentz dielectric function model (DHO - Damped Harmonic Oscillator) used for the adjustment of crystal spectra is not suitable for glasses.

Causal Voigt model

Allows to account for a Gaussian (G) broadening of a Lorentzian absorption profile (L).

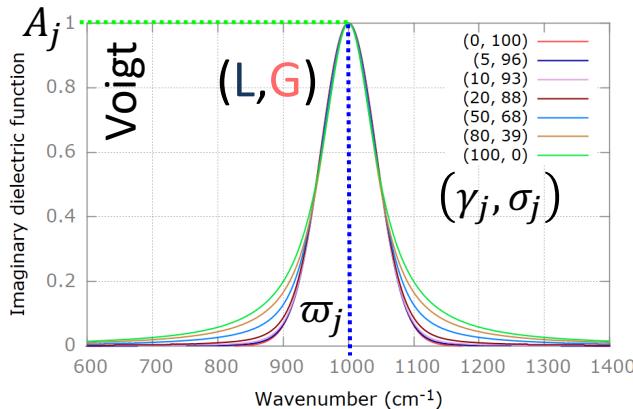
$$\varepsilon_V(\omega) = \varepsilon_{\infty} + \sum_j \hat{V}_j(\omega) = \varepsilon_{\infty} + \sum_j \hat{V}(\omega; A_j, \omega_j, \gamma_j, \sigma_j)$$

$$\hat{V}_j(\omega) = \hat{V}_j(x, y)$$

$$= A_j \left[-\frac{\Im(w(x - x_j + iy) + w(x + x_j + iy))}{\Re(w(iy))} + i \frac{\Re(w(x - x_j + iy) - w(x + x_j + iy))}{\Re(w(iy))} \right]$$

$$x = \frac{2\sqrt{\ln 2}}{\sigma_j} \omega \quad x_j = \frac{2\sqrt{\ln 2}}{\sigma_j} \omega_j \quad y = \frac{\gamma_j}{\sigma_j} \sqrt{\ln 2}$$

Faddeeva function: $w(z) = \frac{i}{\pi} \int_{-\infty}^{+\infty} \frac{e^{-t^2}}{z - t} dt = K(x, y) + i J(x, y)$



D. De Sousa Meneses et al. J. Non-Cryst. Solids 351 (2005) 124-129.

Dielectric function models – disordered media

Convolution model

Expression based on a Gaussian distribution of damped harmonic oscillators

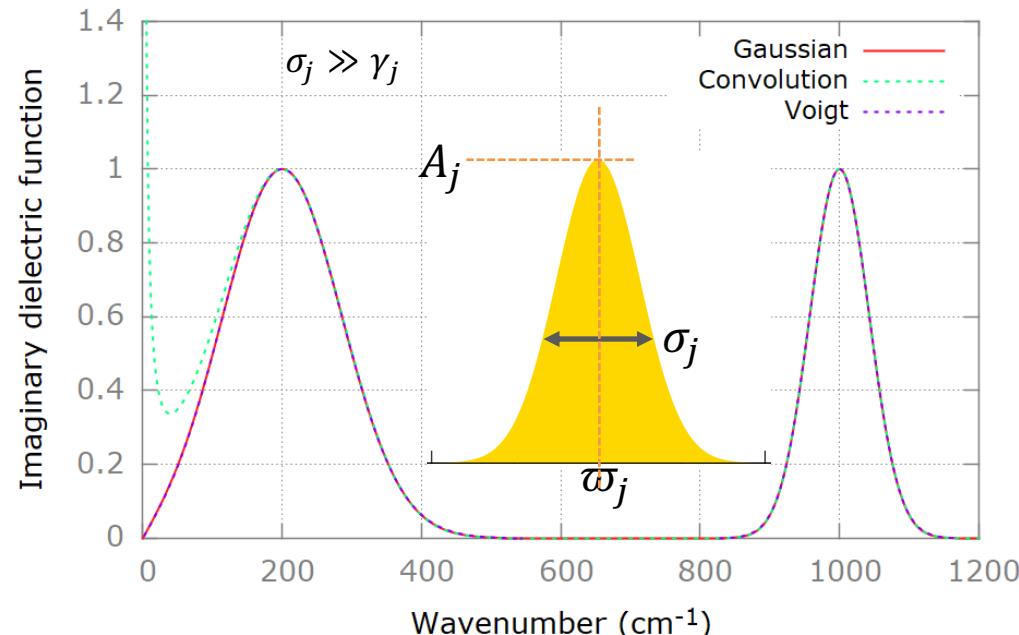
$$\varepsilon(\omega) = \varepsilon_\infty + \sum_j \frac{S_j}{\sqrt{2\pi}\sigma_j} \int_{-\infty}^{+\infty} \frac{\exp\left[-\frac{1}{2}\left(\frac{x - \bar{\omega}_j}{\sigma_j}\right)^2\right]}{x^2 - \omega^2 - i\gamma_j\omega} dx$$

H. Hobert, H. H. Dunken J. Non-Cryst. Solids 195 (1996) 64-71

A. M. Efimov, J. Non-Cryst. Solids 203 (1996) 1.

T. G. Mayerhofer et al. J. Non-Cryst. Solids 333 (2004) 172–181.

The Voigt and convolution models have close absorption profiles for high frequency modes with low inhomogeneous broadening. The difference can be large at low frequency.



Causal Gaussian model

Allows to take into account several components having a Gaussian absorption profile respecting the causality principle.

$$\varepsilon(\omega) = \varepsilon_\infty + \sum_j \frac{2A_j}{\sqrt{\pi}} \left[D\left(2\sqrt{\ln 2} \frac{\omega + \bar{\omega}_j}{\sigma_j}\right) - D\left(2\sqrt{\ln 2} \frac{\omega - \bar{\omega}_j}{\sigma_j}\right) \right] + i A_j \left[\exp\left(-4\ln 2 \left(\frac{\omega - \bar{\omega}_j}{\sigma_j}\right)^2\right) - \exp\left(-4\ln 2 \left(\frac{\omega + \bar{\omega}_j}{\sigma_j}\right)^2\right) \right]$$

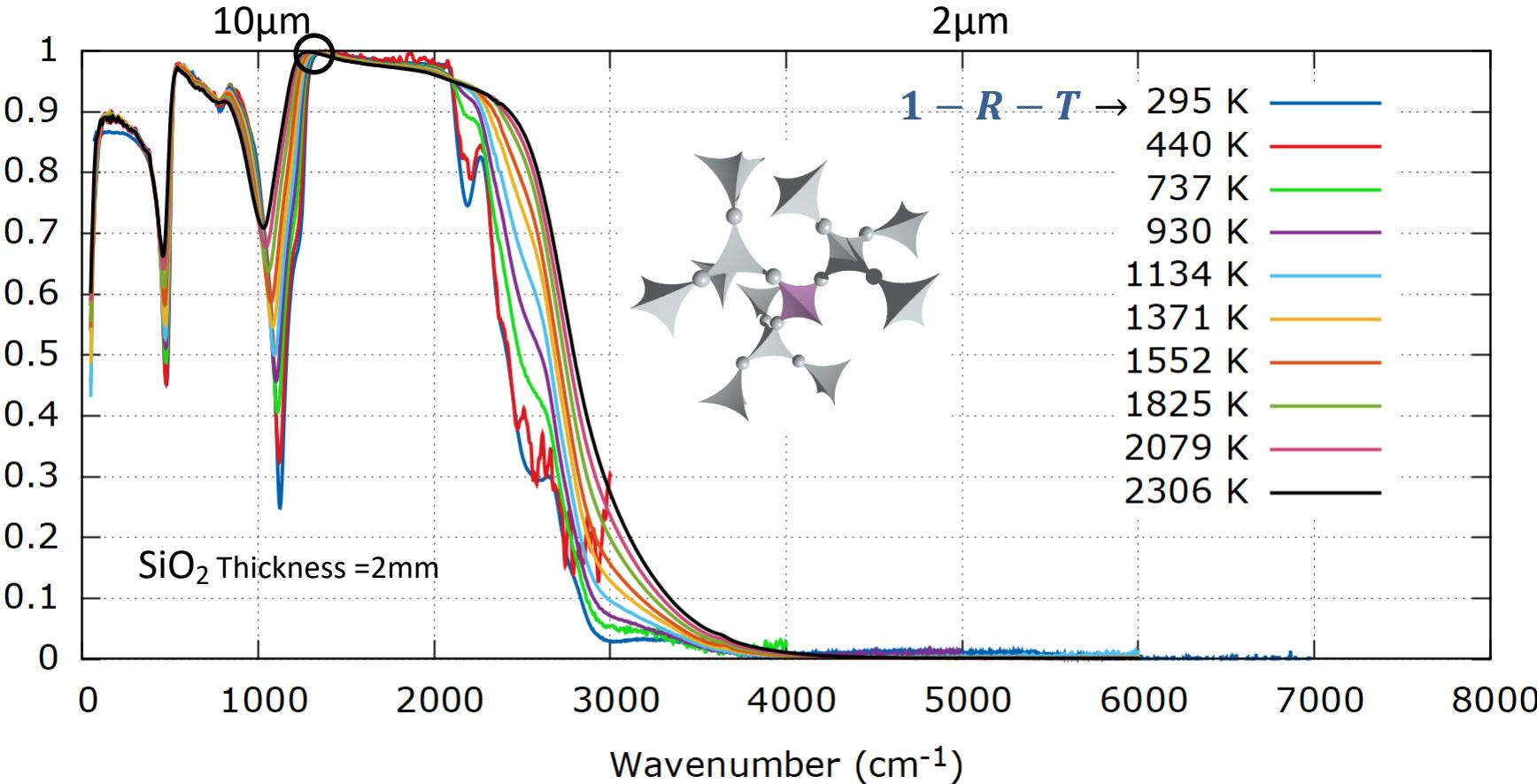
Dawson function: $D(x) = \exp(-x^2) \int_0^x \exp(t^2) dt$

D. De Sousa Meneses, M. Malki, P. Echegut, J. Non-Cryst. Solids 351 (2006) 769-776.

USTV SCHOOL ON THE CHARACTERIZATION OF GLASS STRUCTURE/ November 18-22 2019

Normal spectral emittance of a silica glass

Normal spectral emittance



Temperature measurement at the Christiansen point ○ $n = 1, k \ll 1 \rightarrow E \cong 1$

Retrieval of the complex refractive index $N(\omega) = n(\omega) + i k(\omega)$

Fit of the data with the following parallel plate model of emittance (E):

$$E = \frac{(1 - \rho)(1 - \tau)}{1 - \rho\tau} \quad \rho = \frac{(n - 1)^2 + k^2}{(n + 1)^2 + k^2} \quad \tau = \exp(-4\pi k\omega d)$$

d : sample thickness

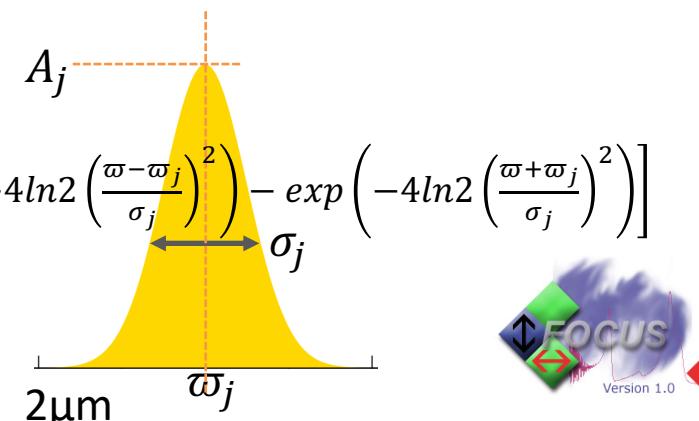
Fit with a dielectric function model

Dielectric function : $\epsilon(\omega) = [N(\omega)]^2$

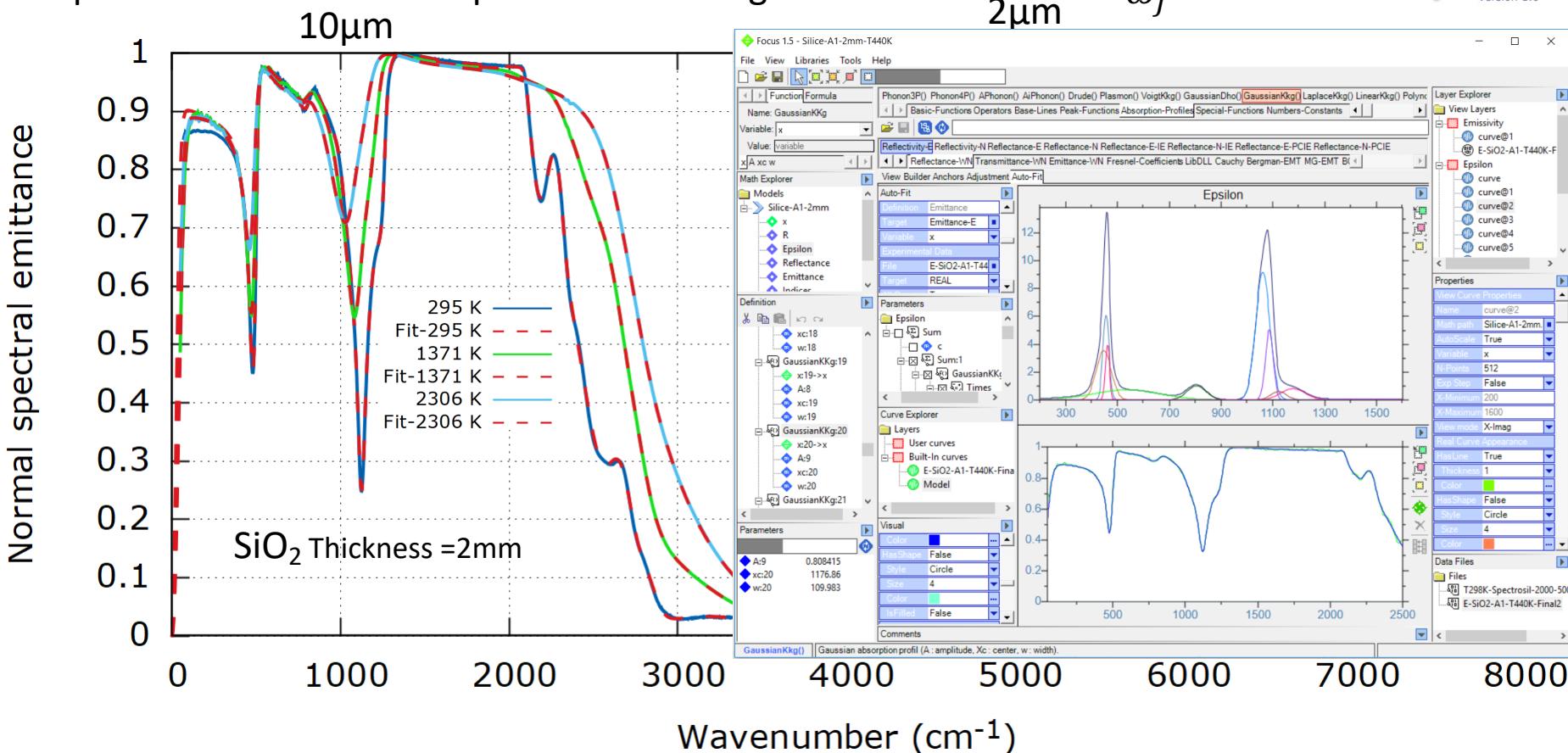
Causal Gaussian dielectric function model for glasses

$$\epsilon(\omega) = \epsilon_{\infty} + \sum_j \frac{2A_j}{\sqrt{\pi}} \left[D\left(2\sqrt{\ln 2} \frac{\omega + \omega_j}{\sigma_j}\right) - D\left(2\sqrt{\ln 2} \frac{\omega - \omega_j}{\sigma_j}\right) \right] + i A_j \left[\exp\left(-4\ln 2 \left(\frac{\omega - \omega_j}{\sigma_j}\right)^2\right) - \exp\left(-4\ln 2 \left(\frac{\omega + \omega_j}{\sigma_j}\right)^2\right) \right]$$

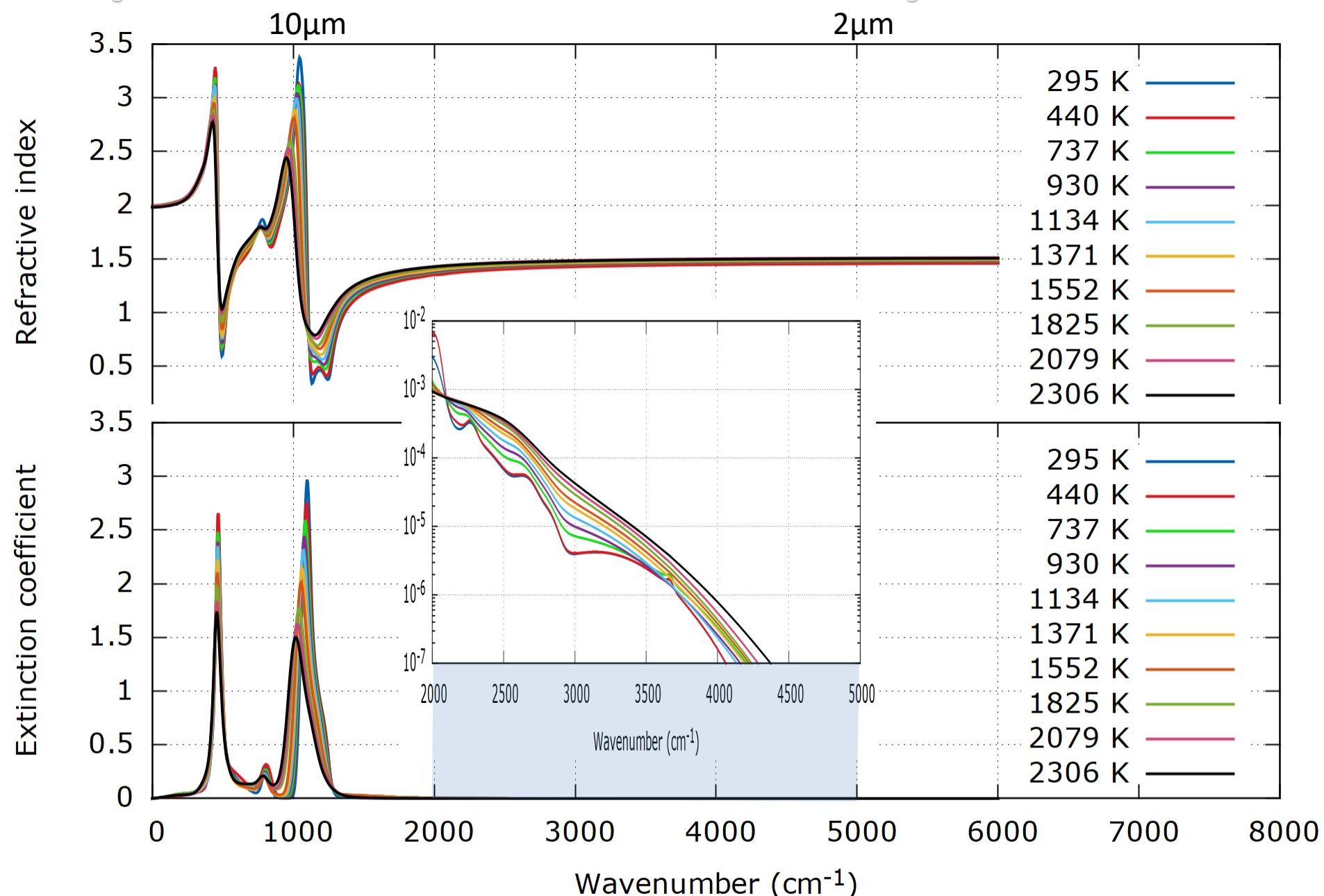
D is the Dawson function



Examples of fit of emittance spectra of a silica glass



Complex refractive index of the silica sample

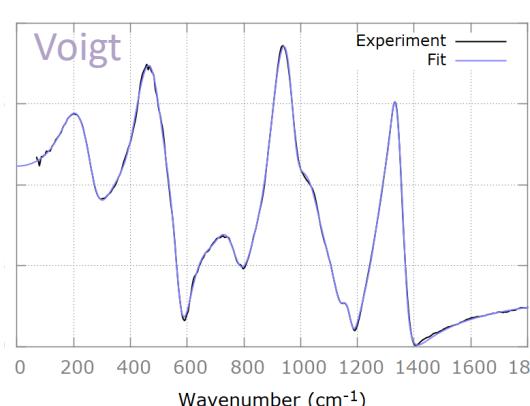
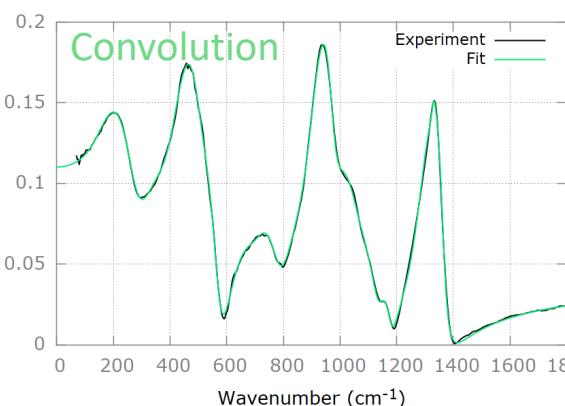
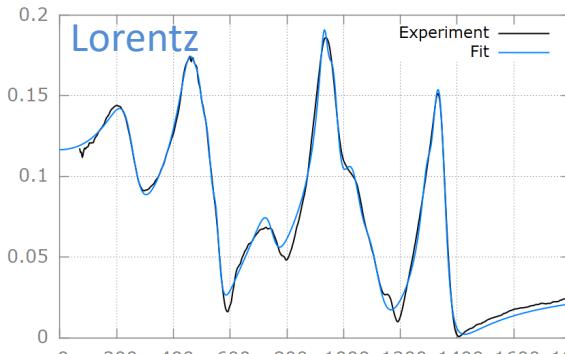


Fit of the reflectivity of a glass with different models

Lorentz model

Gaussian model

$(\text{CaO})_x(\text{P}_2\text{O}_5)_{1-x}$ glass

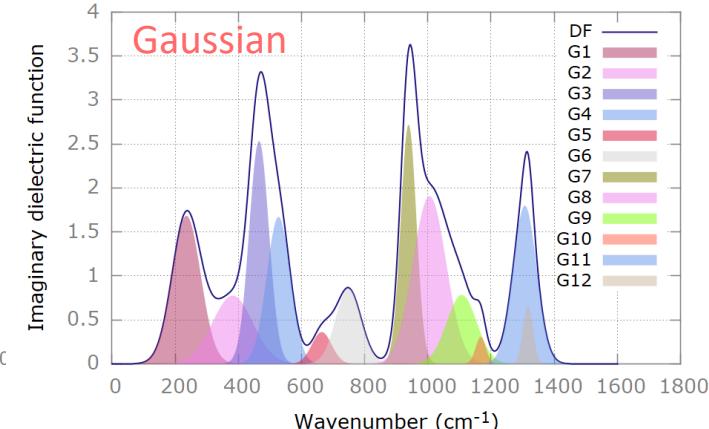


Convolution model

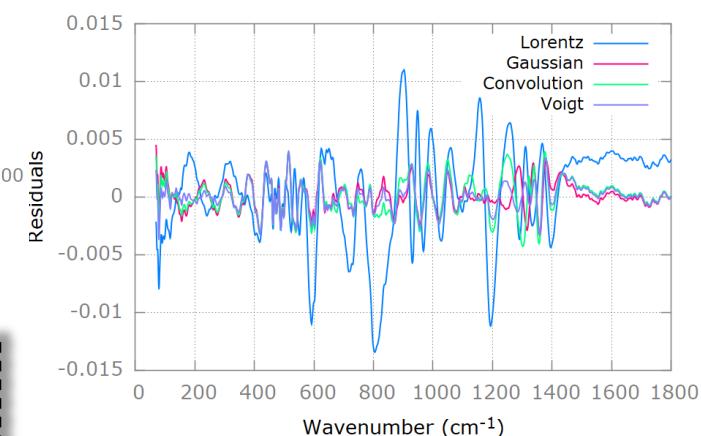
Voigt model

The causal Gaussian dielectric function model represents a good compromise in terms of quality of fit and simplicity for the analysis of the infrared response of most of glasses

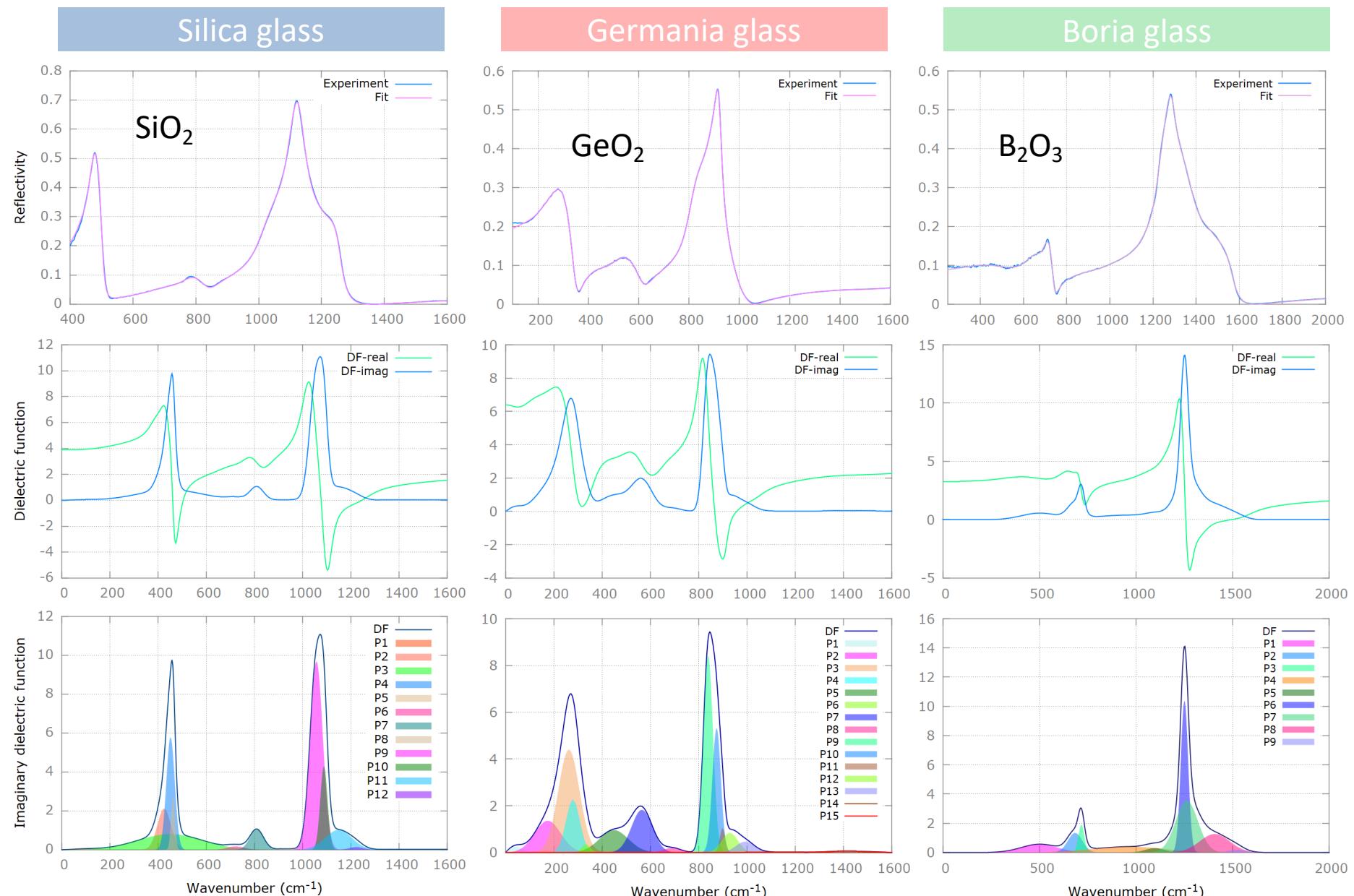
Imaginary dielectric function



Fit residuals

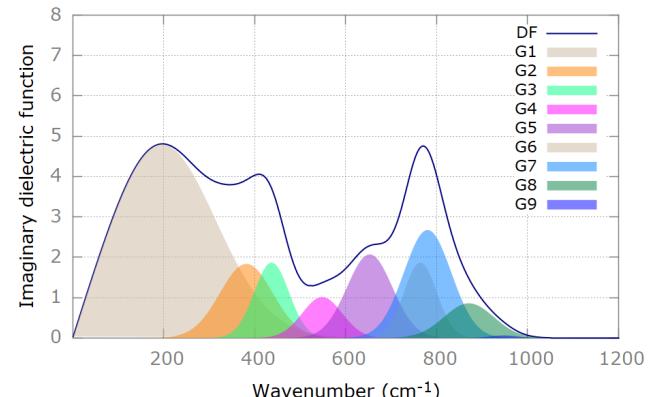
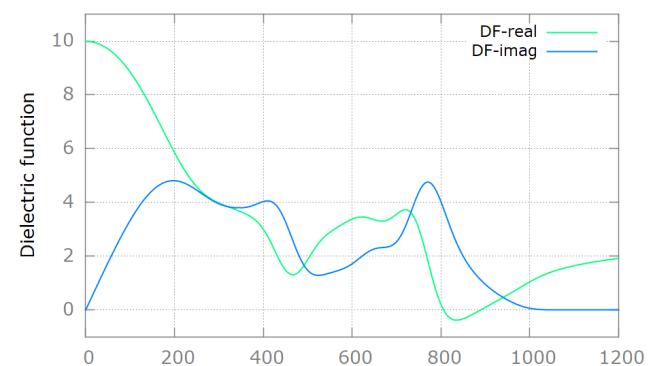
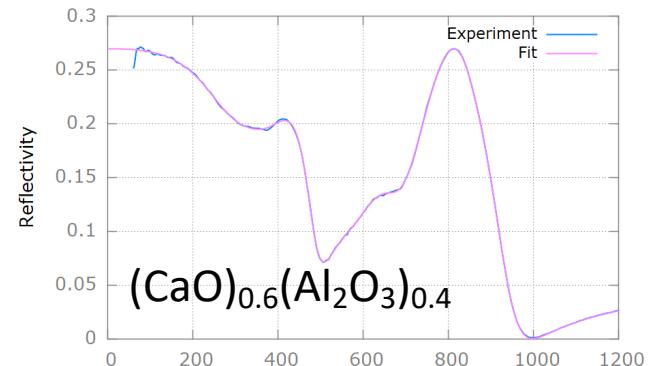


Fits of reflectivity with a Gaussian dielectric function model

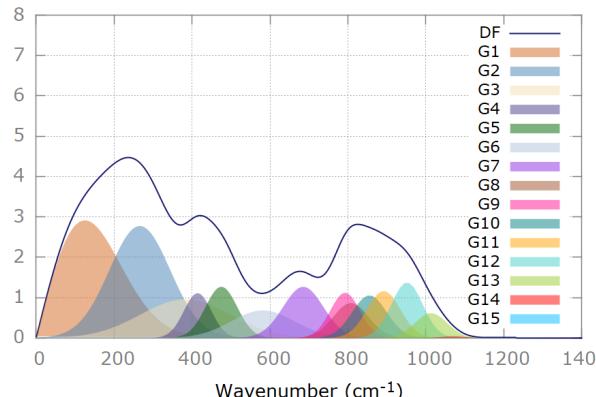
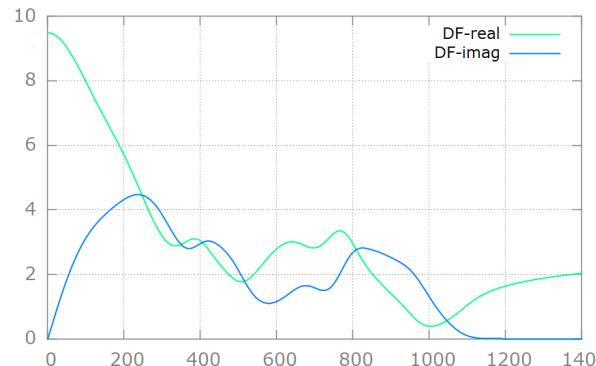
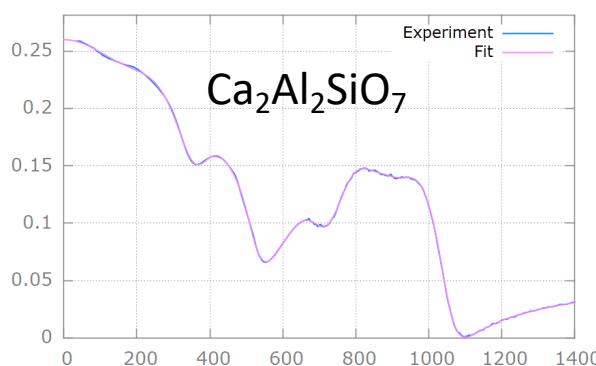


Fits of reflectivity with a Gaussian dielectric function model

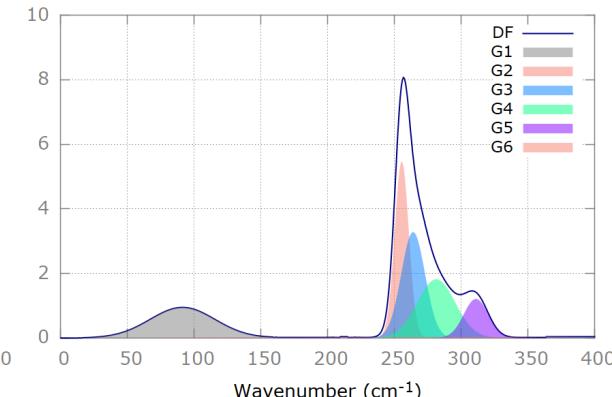
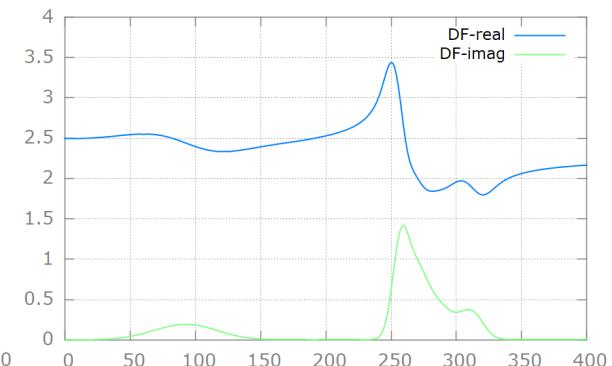
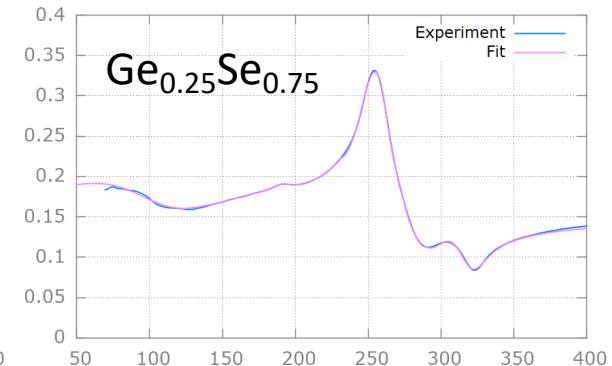
Aluminate glass



Aluminosilicate glass

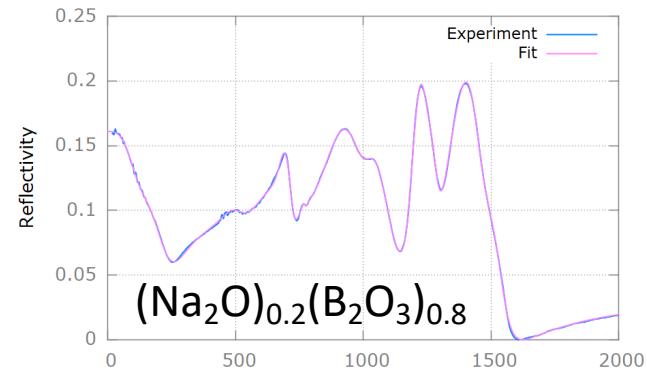


Chalcogenide glass

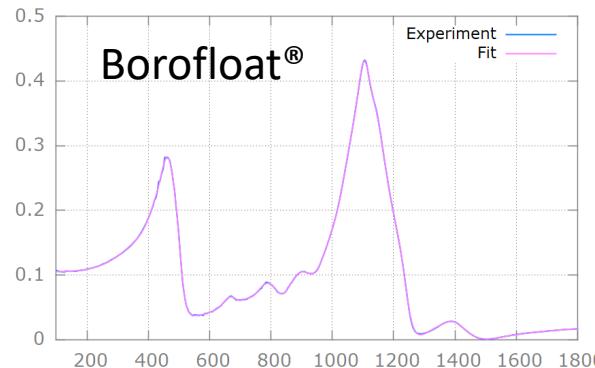


Fits of reflectivity with a Gaussian dielectric function model

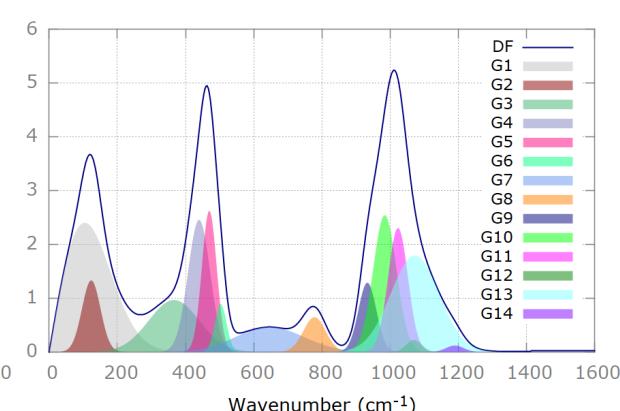
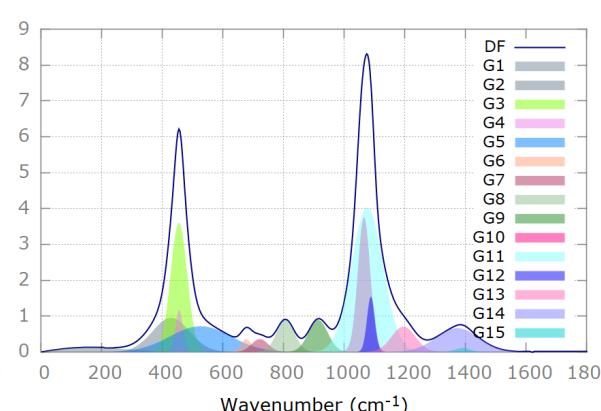
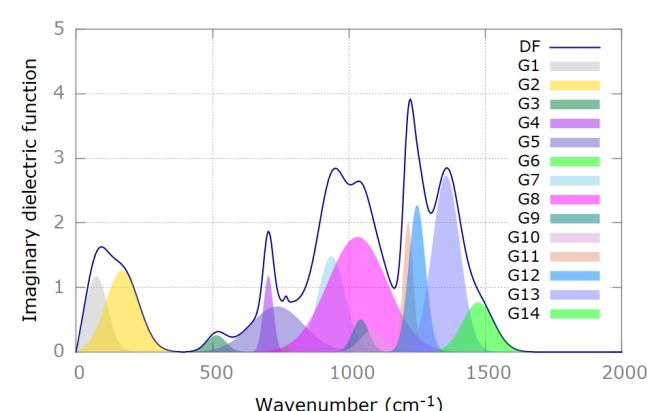
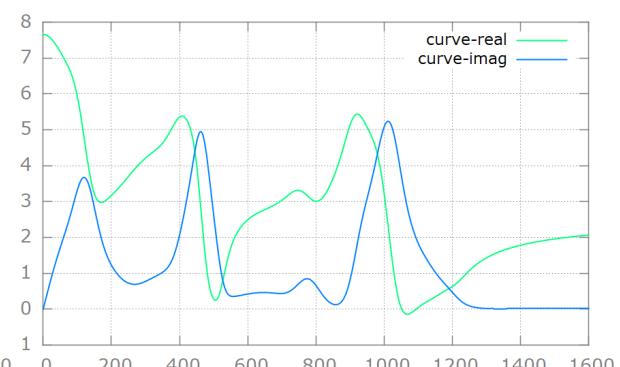
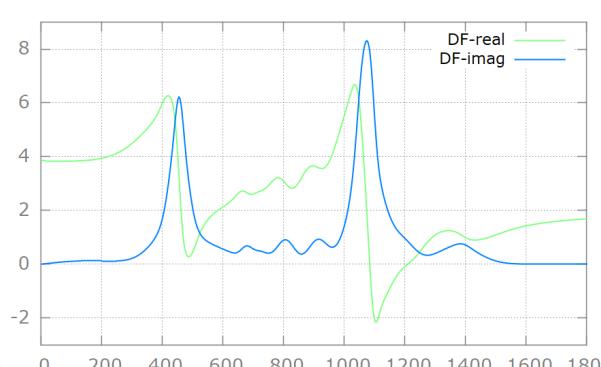
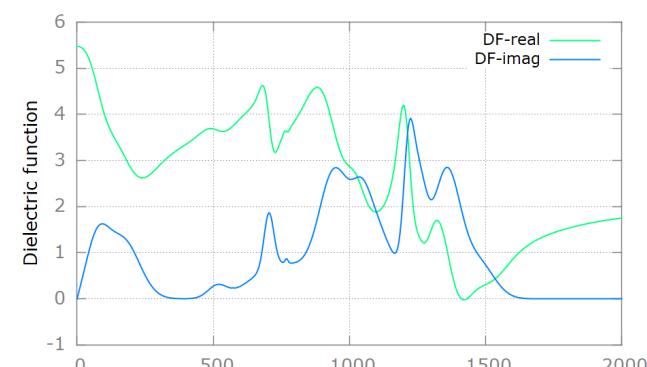
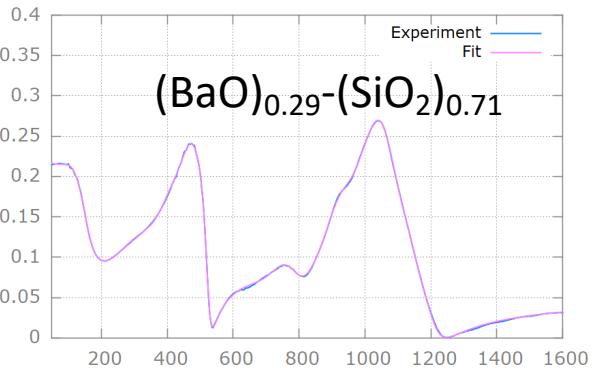
Borate glass



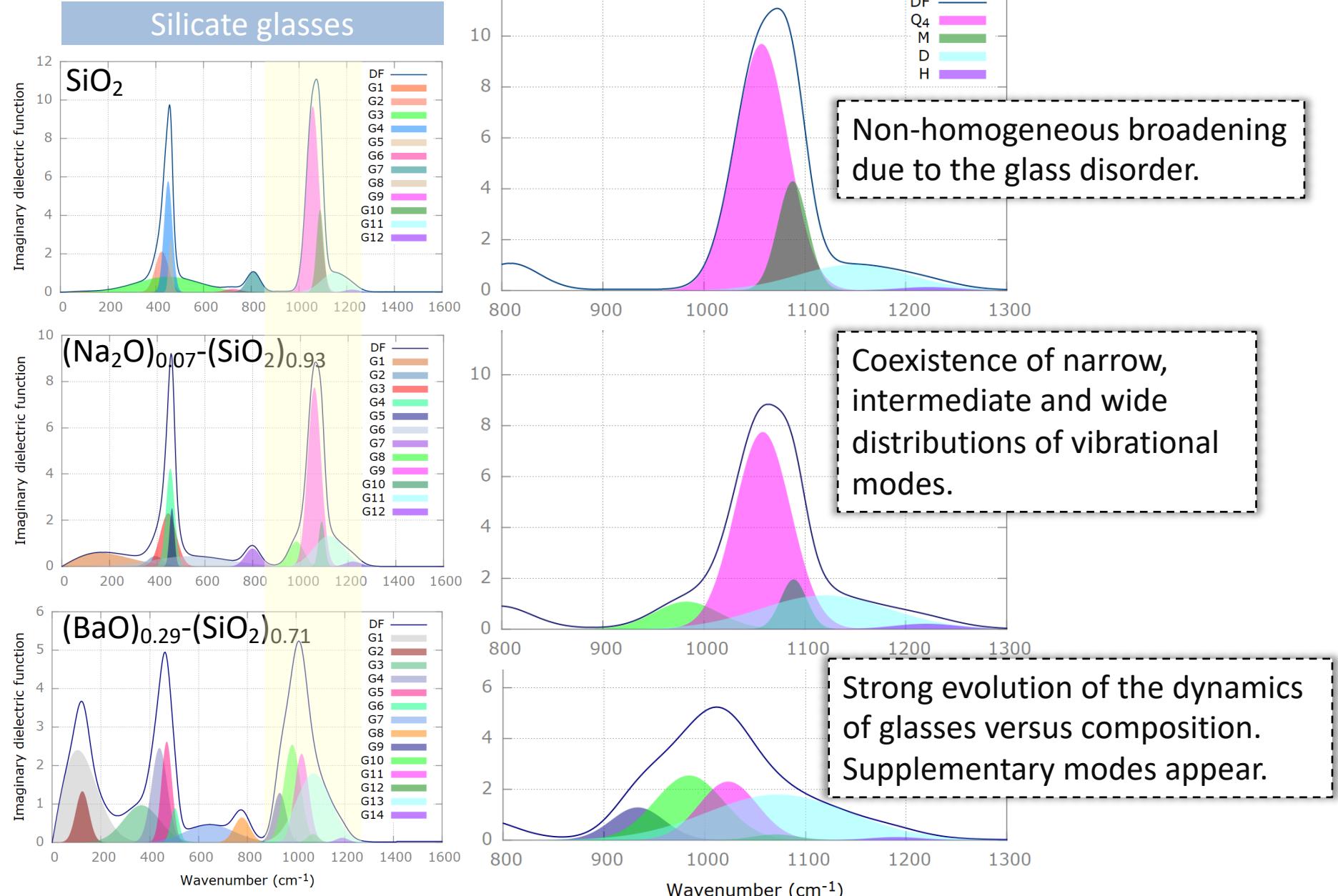
Borosilicate glass



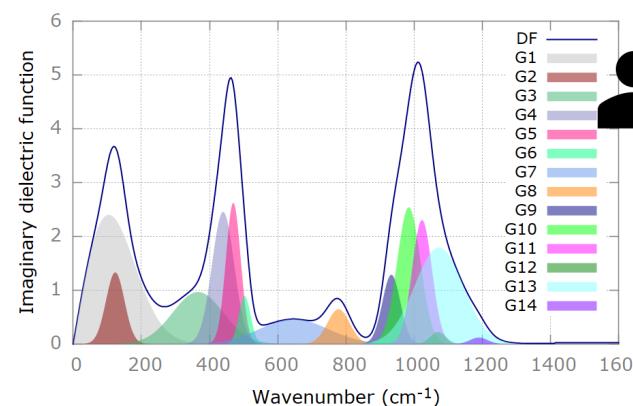
Silicate glass



Infrared response of silicate glasses

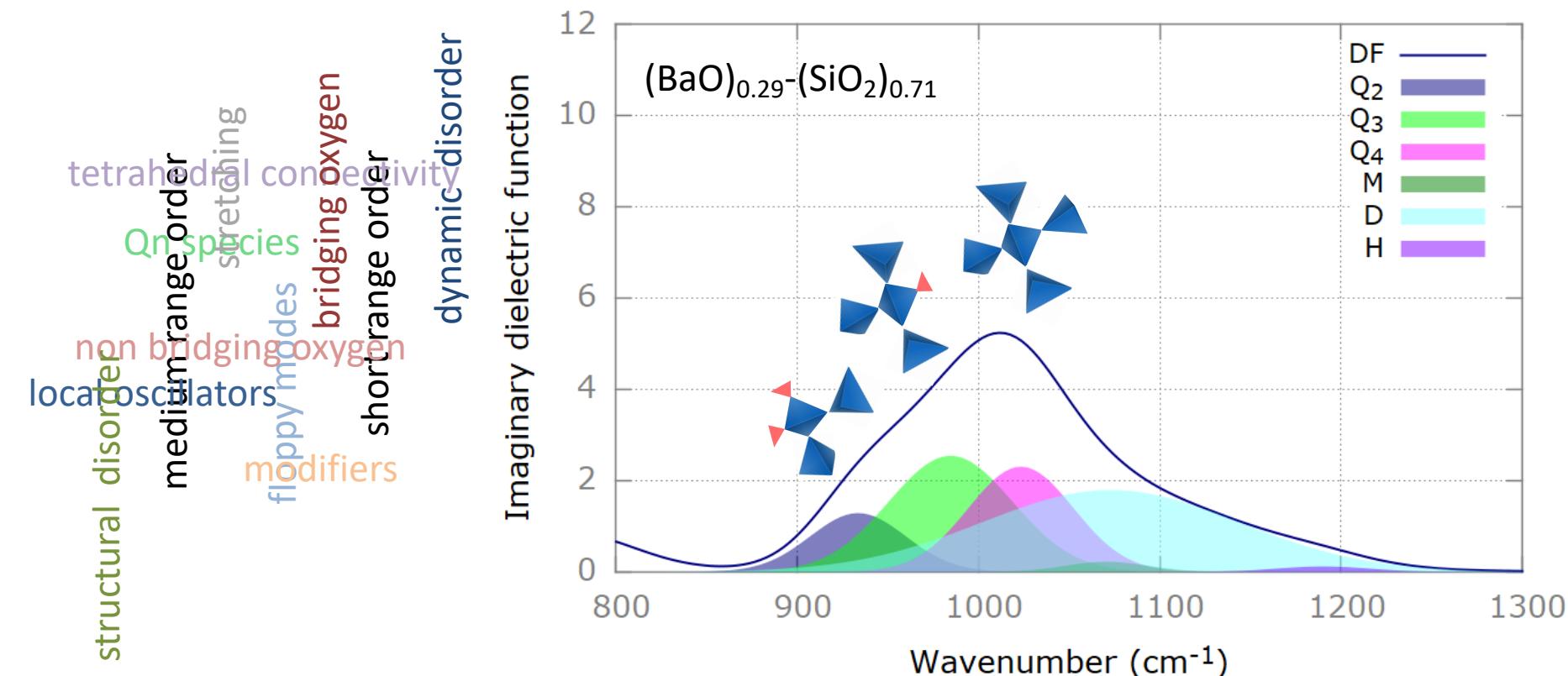


Infrared response of silicate glasses

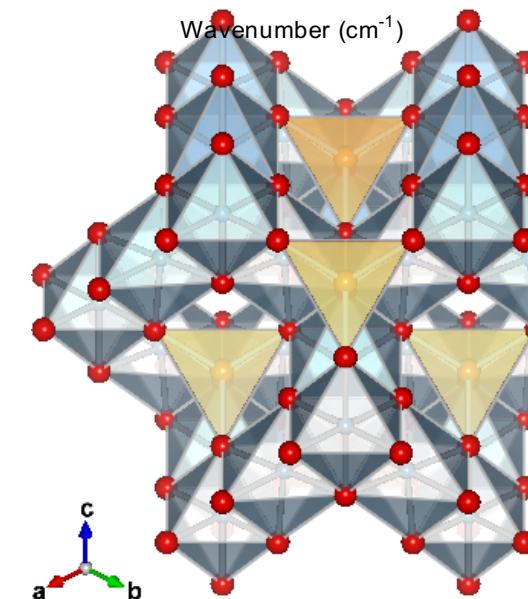
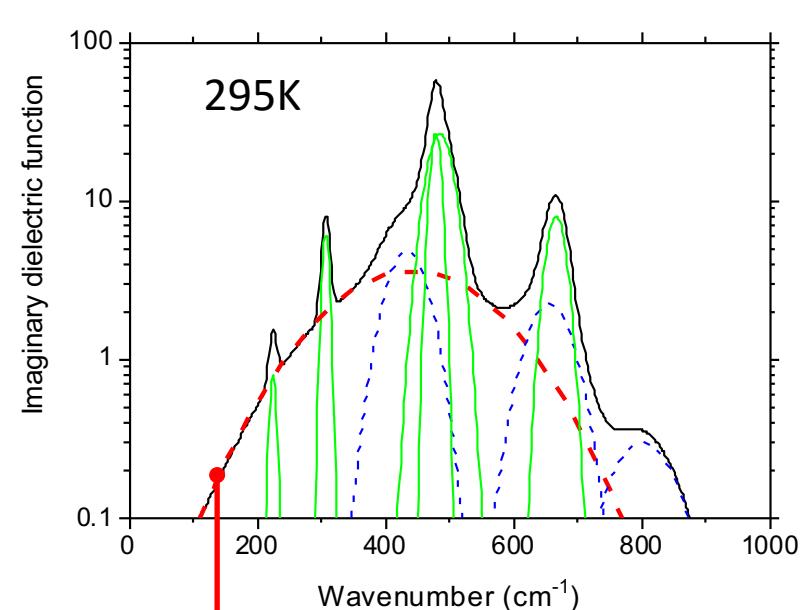
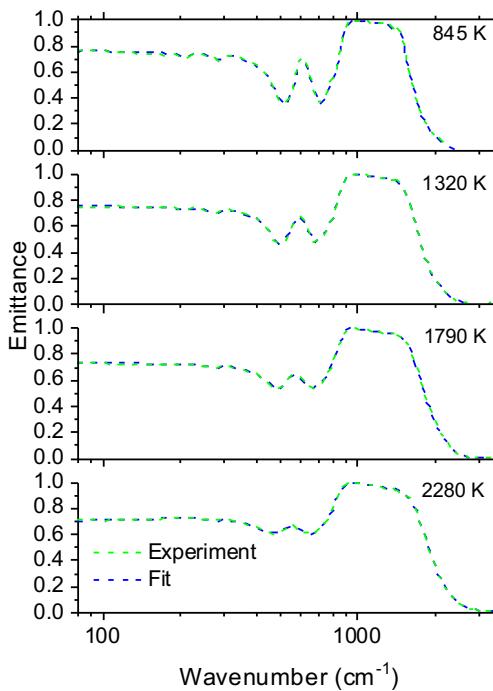
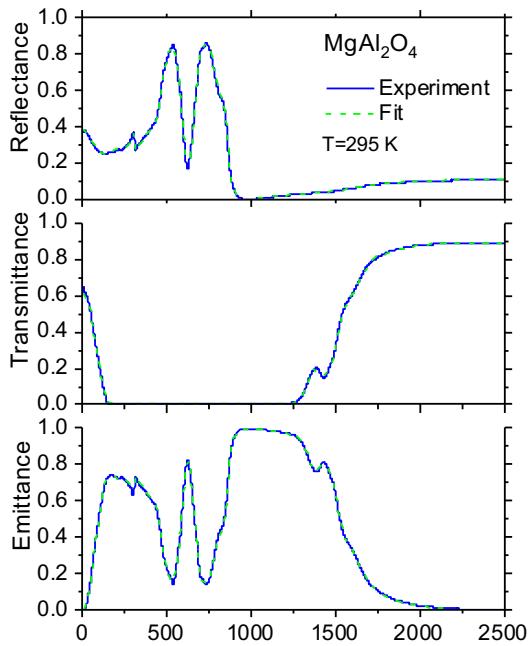


Why such a high number of Gaussian components?
Do they have a physical meaning?
What about the fidelity of the dielectric function model?
Does it include information on the glass network?
Can I probe cation modifiers?

...



Inversion rate in MgAl_2O_4 versus temperature

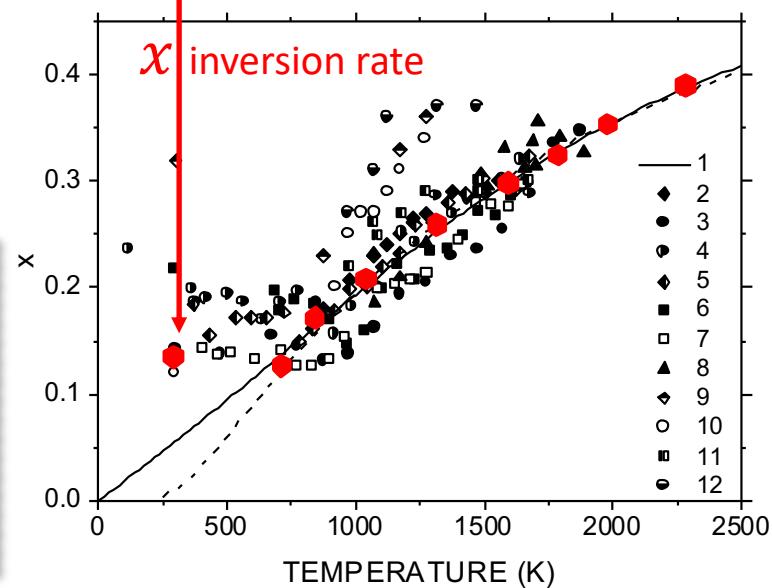


Site occupation disorder

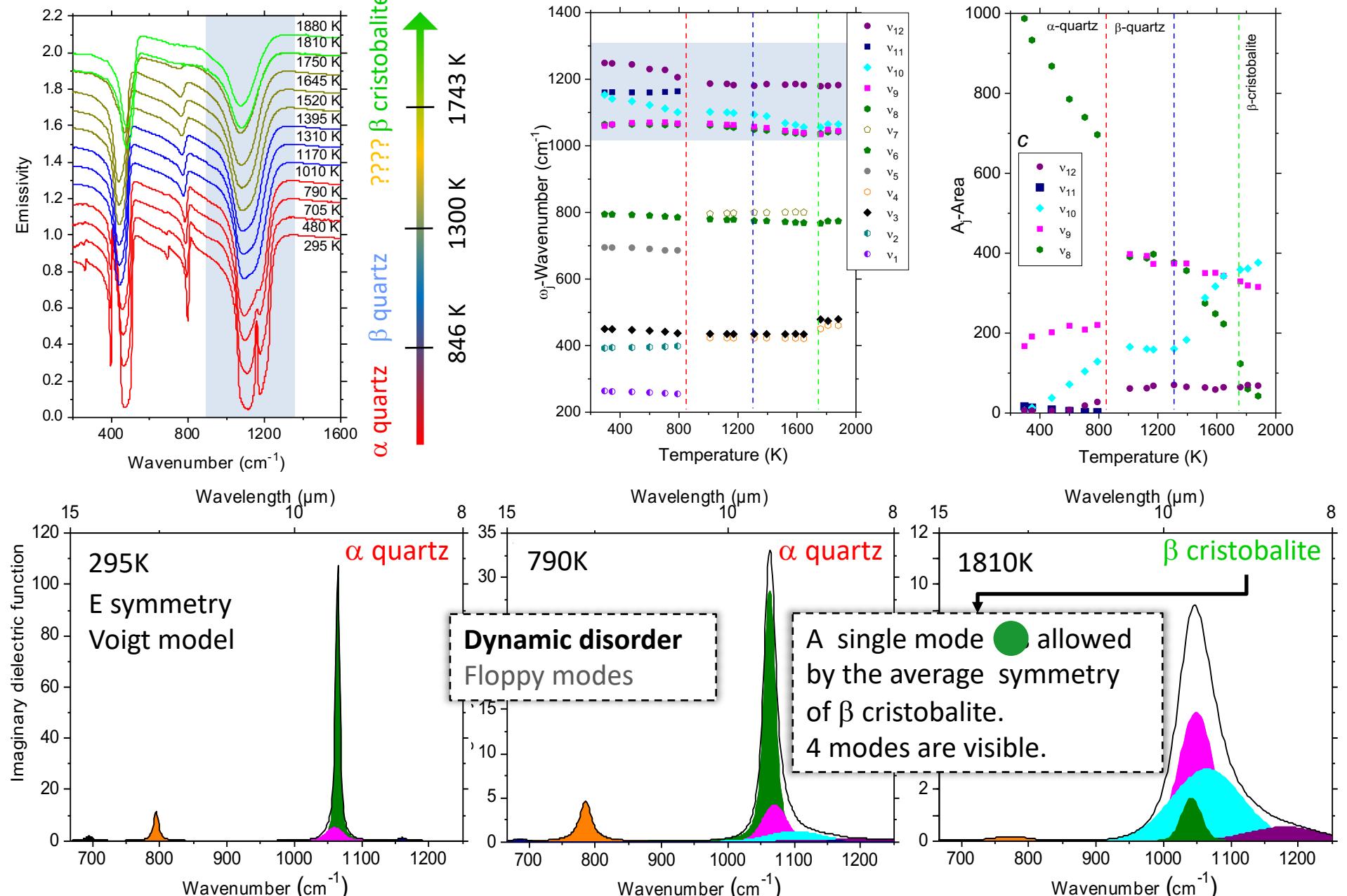
Al/Mg disorder



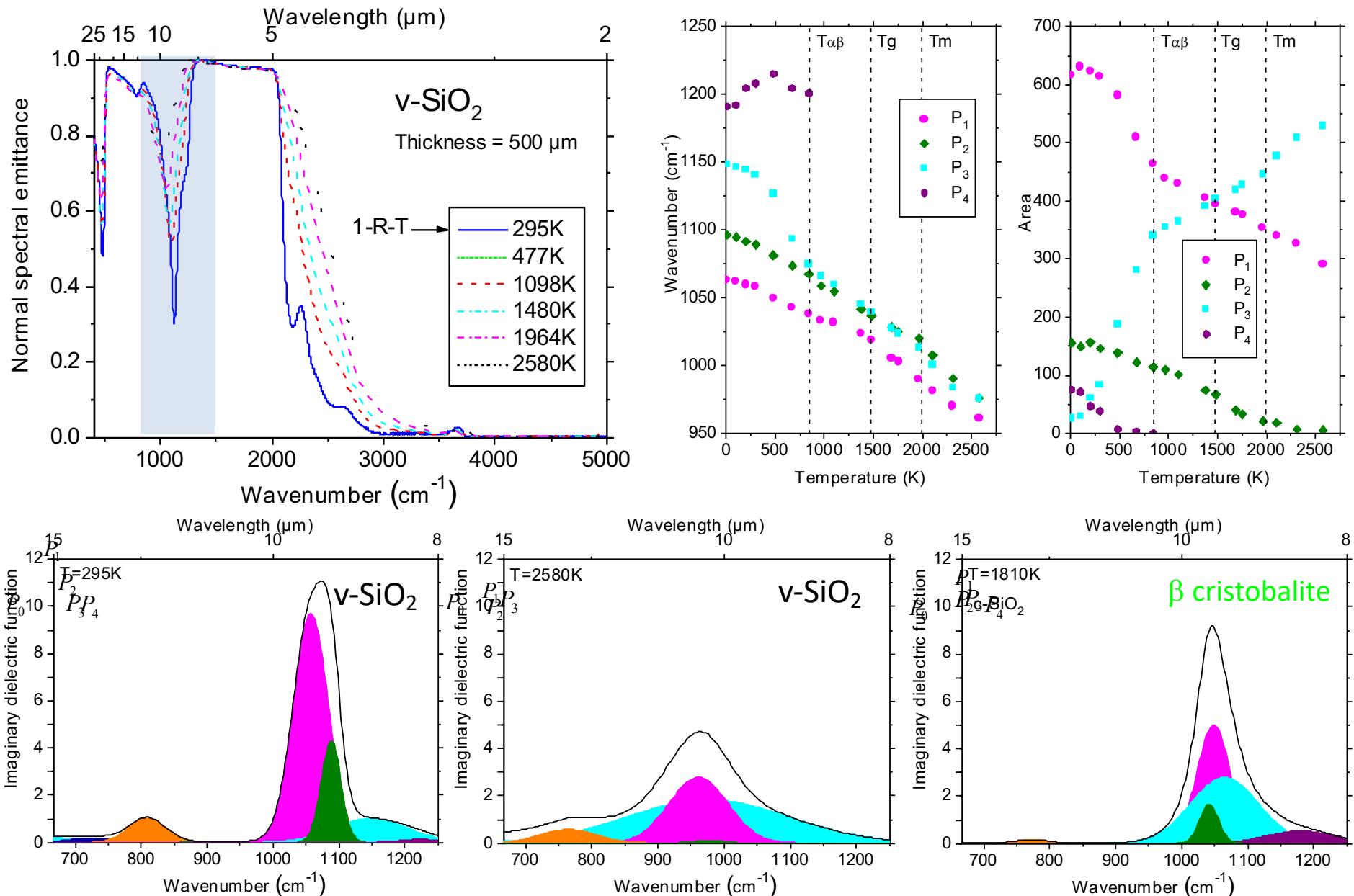
Coexistence of allowed modes and modes forbidden by symmetry.
Intensity of the widest absorption component linked to the inversion rate x .



Dynamics and phase transitions of crystalline SiO₂

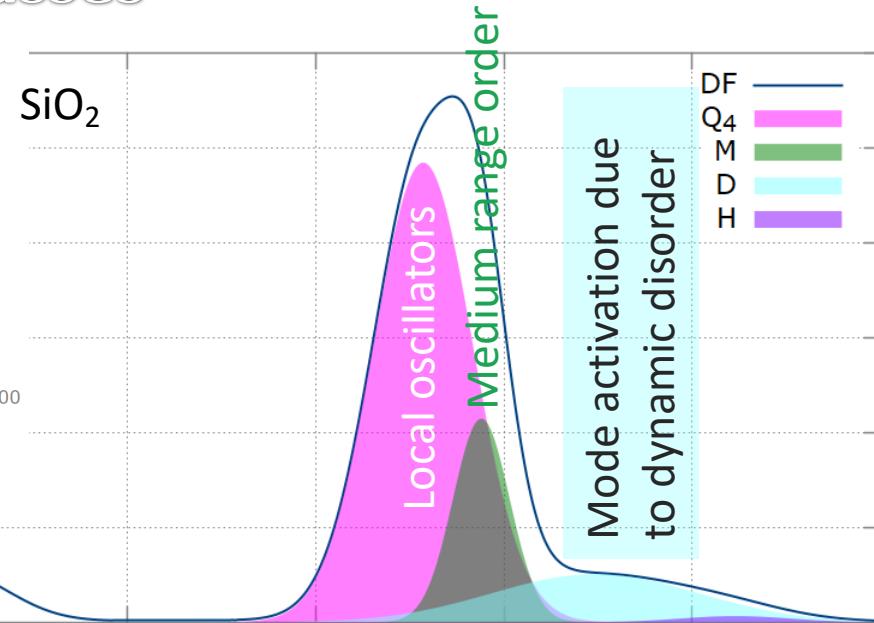
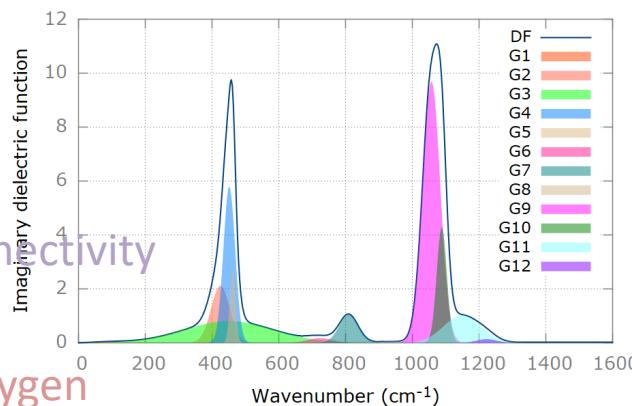


Dynamics of a silica glass versus temperature

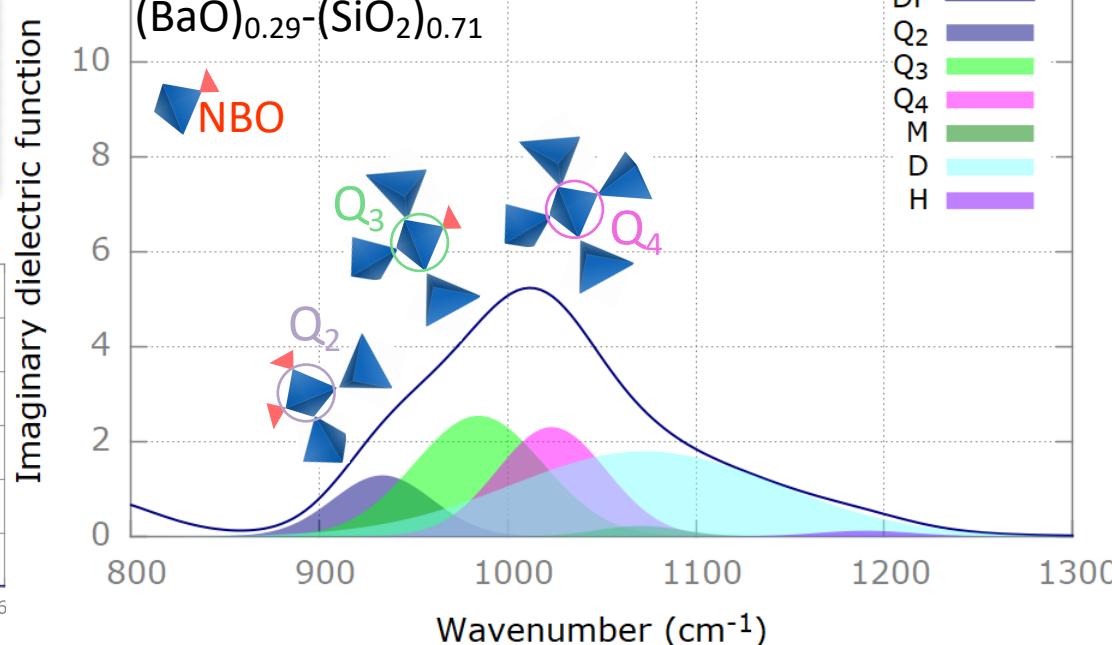
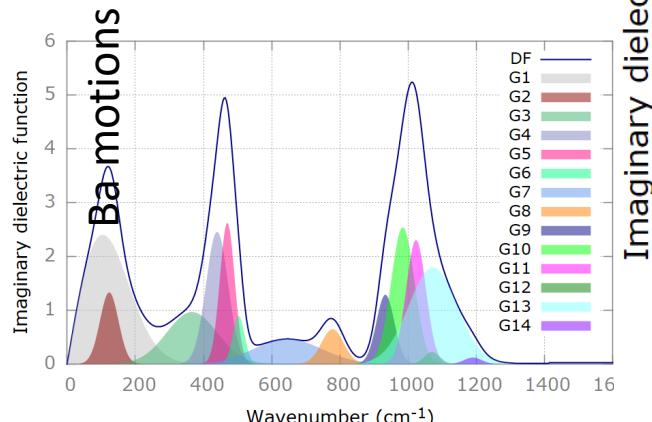


Infrared response of silicate glasses

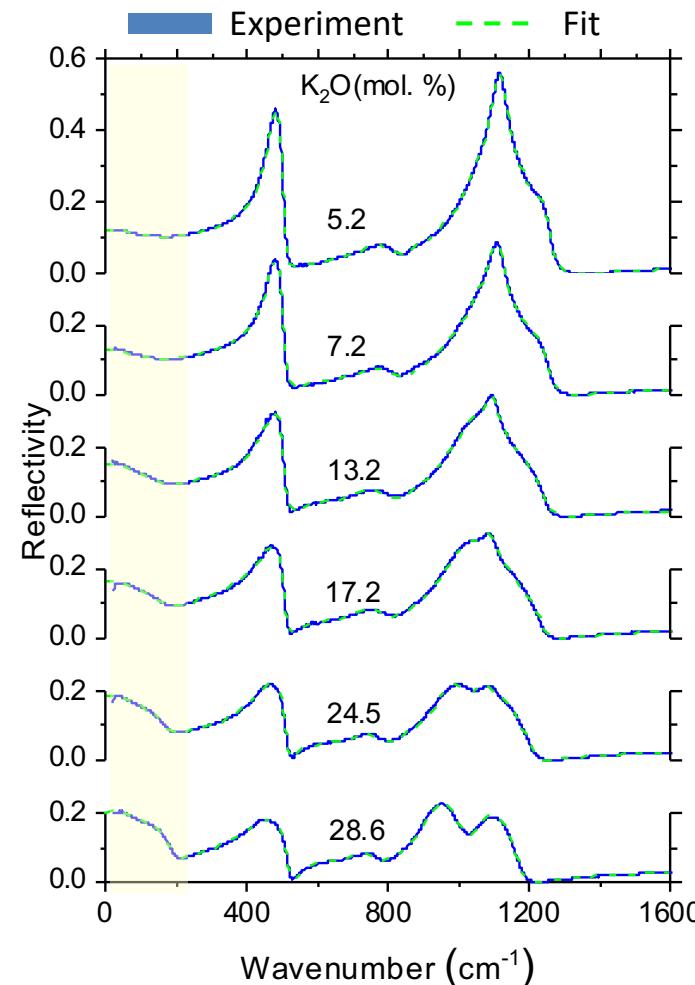
tetrahedral
disorder
medium range order
stretching
spectra
non bridging oxygen
local oscillators
short range order
dynamic disorder
modifiers



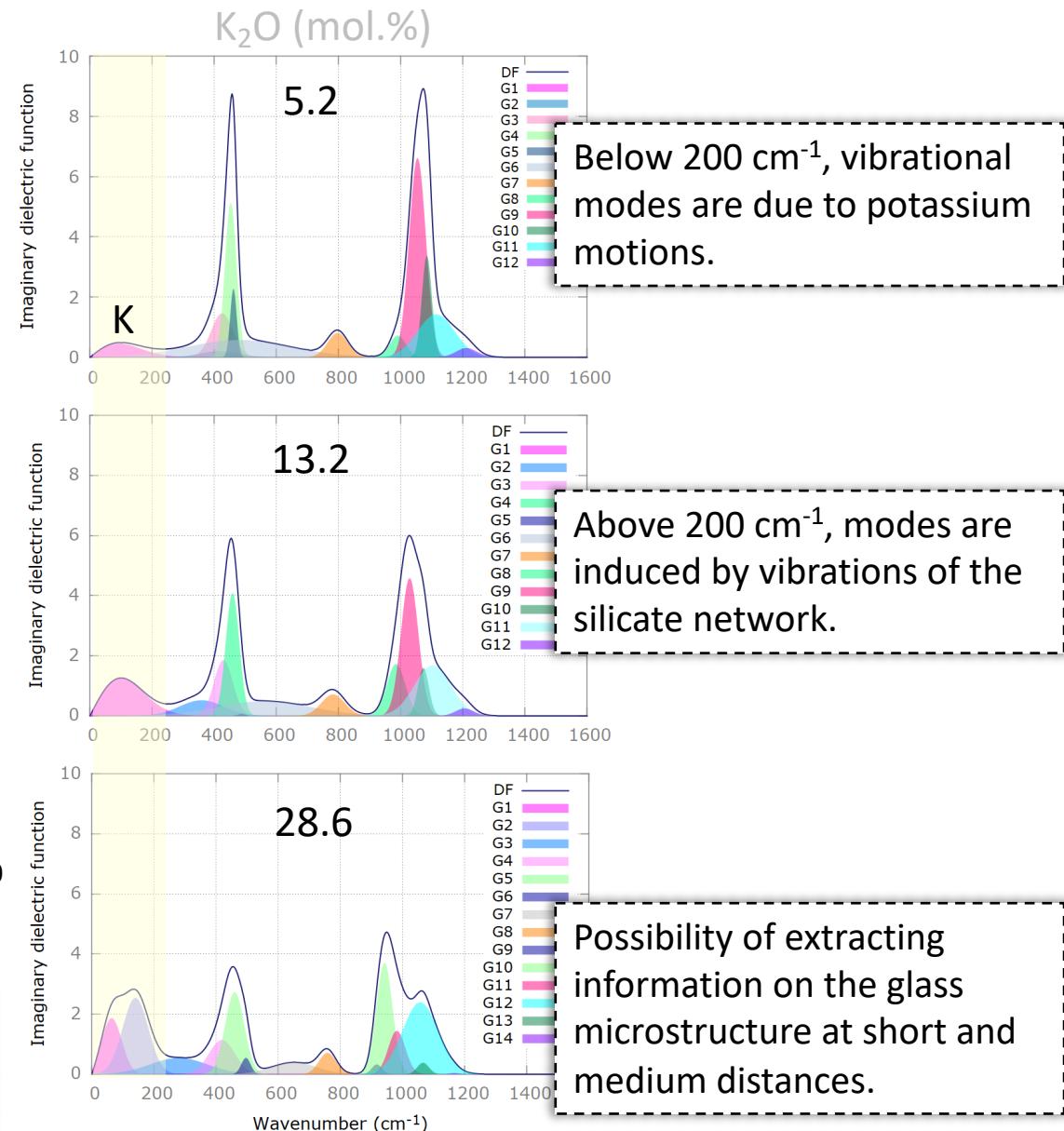
Gaussian components give information on the silicate network dynamics, cation motions, network connectivity, short and medium range order....



K_2O - SiO_2 glass system



Strong evolution of the reflection spectrum with the increase of the K_2O content.

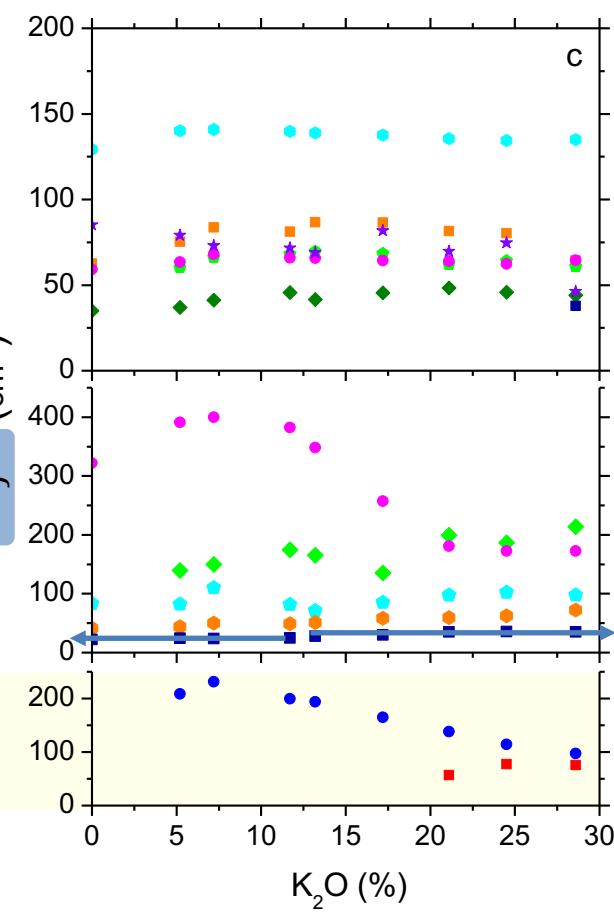
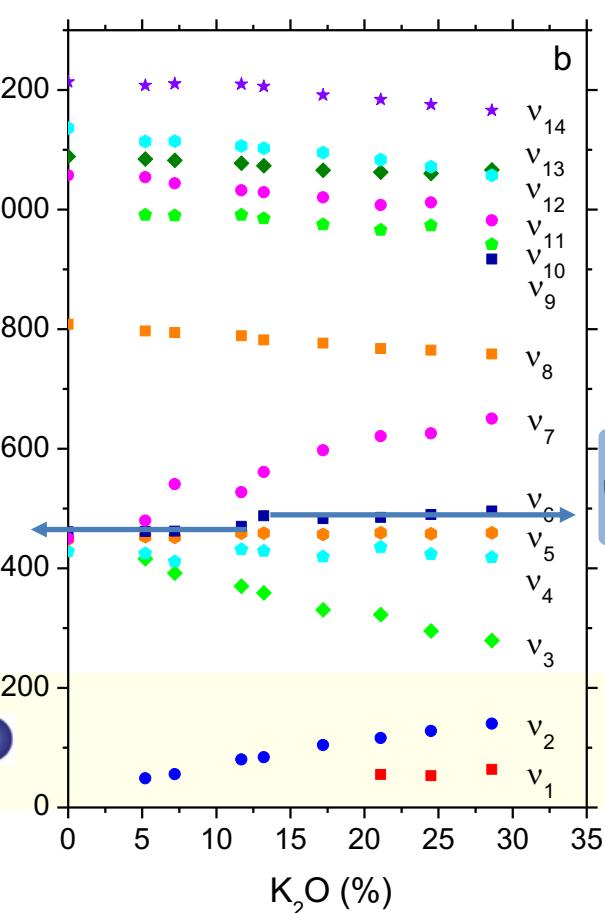
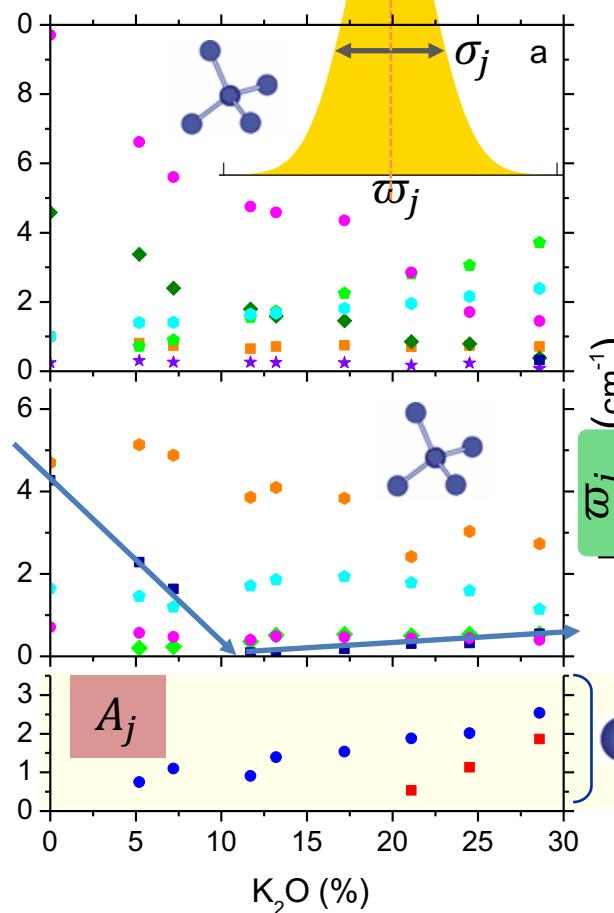


$K_2O - SiO_2$ glass system

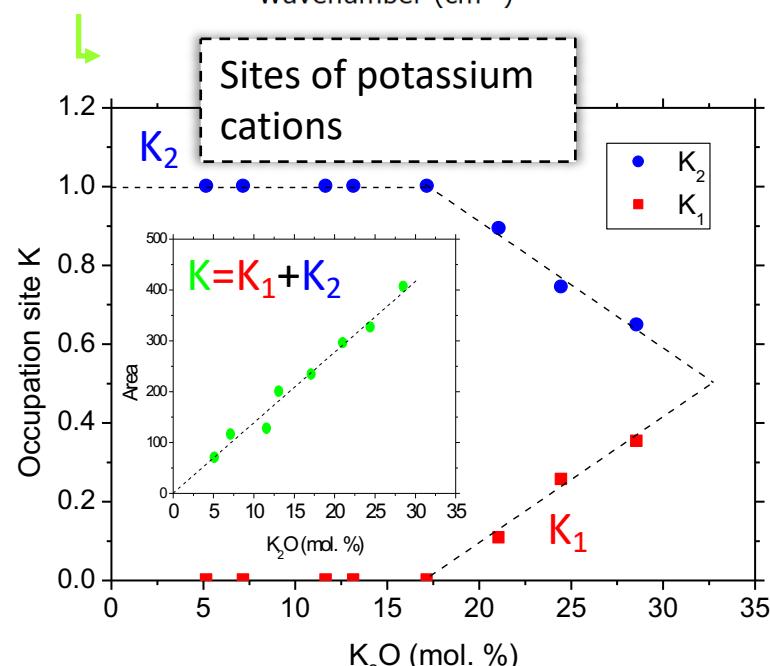
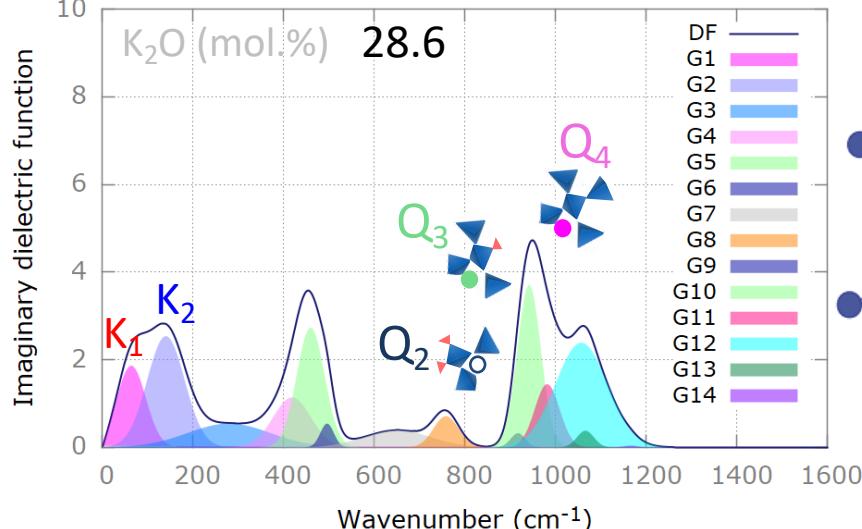
$$\varepsilon(\bar{\omega}) = \varepsilon_\infty + \sum_j \frac{2A_j}{\sqrt{\pi}} \left[D\left(2\sqrt{\ln 2} \frac{\bar{\omega} + \bar{\omega}_j}{\sigma_j}\right) - D\left(2\sqrt{\ln 2} \frac{\bar{\omega} - \bar{\omega}_j}{\sigma_j}\right) \right] + i A_j \left[\exp\left(-4\ln 2 \left(\frac{\bar{\omega} - \bar{\omega}_j}{\sigma_j}\right)^2\right) - \exp\left(-4\ln 2 \left(\frac{\bar{\omega} + \bar{\omega}_j}{\sigma_j}\right)^2\right) \right]$$

A_j

Dawson function: $D(x) = \exp(-x^2) \int_0^x \exp(t^2) dt$

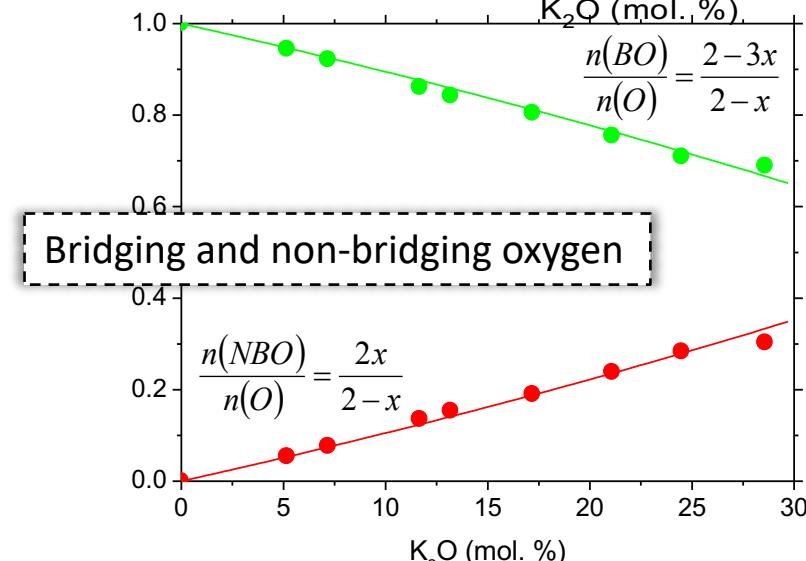
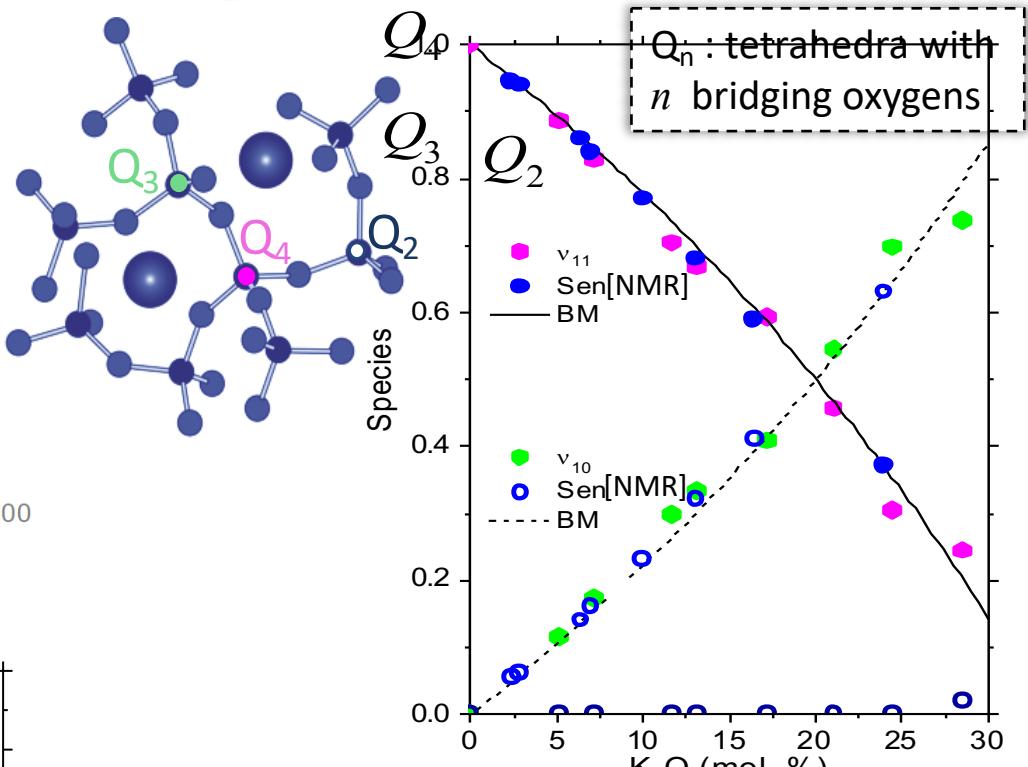


K_2O - SiO_2 glass system : short range order

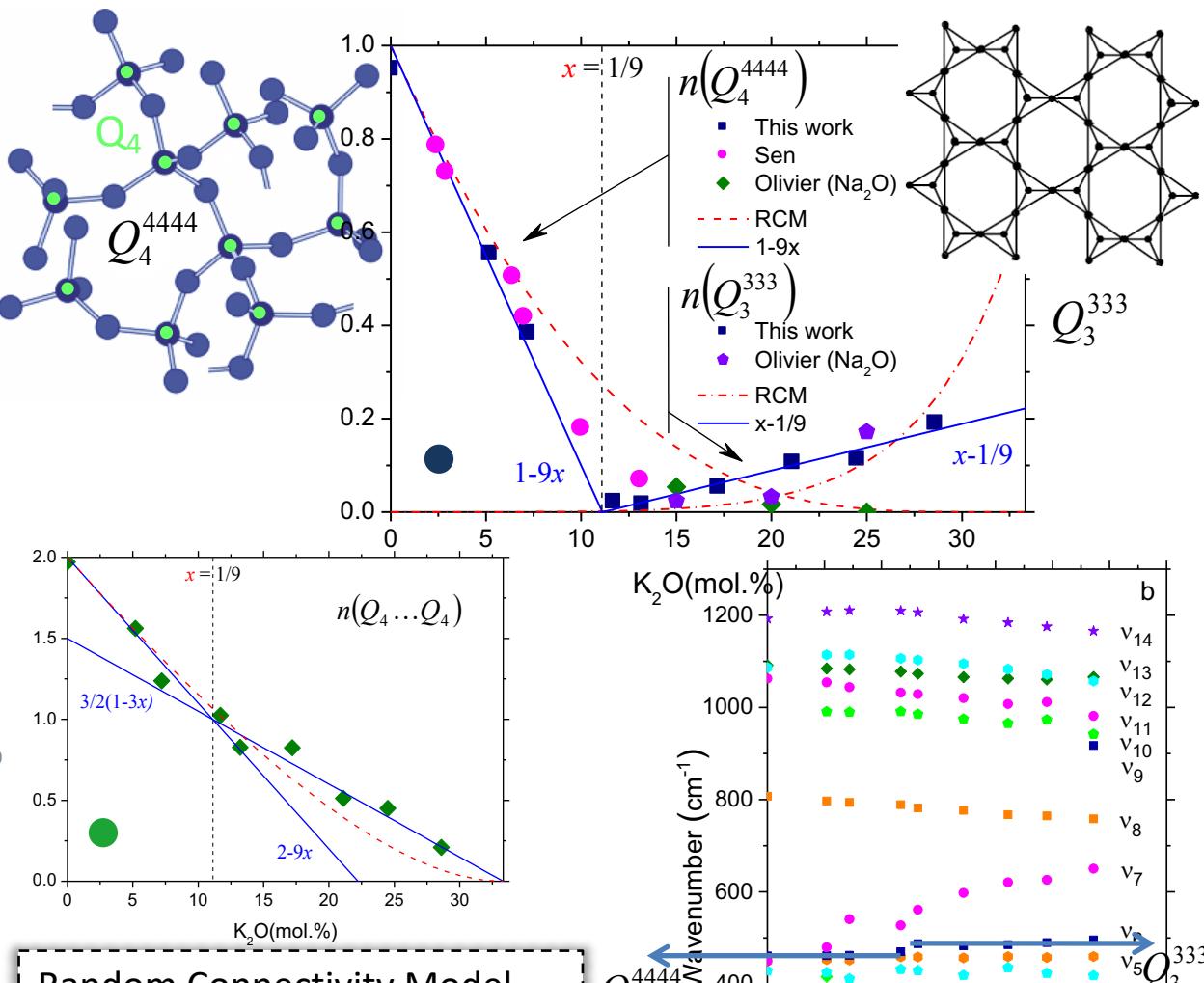
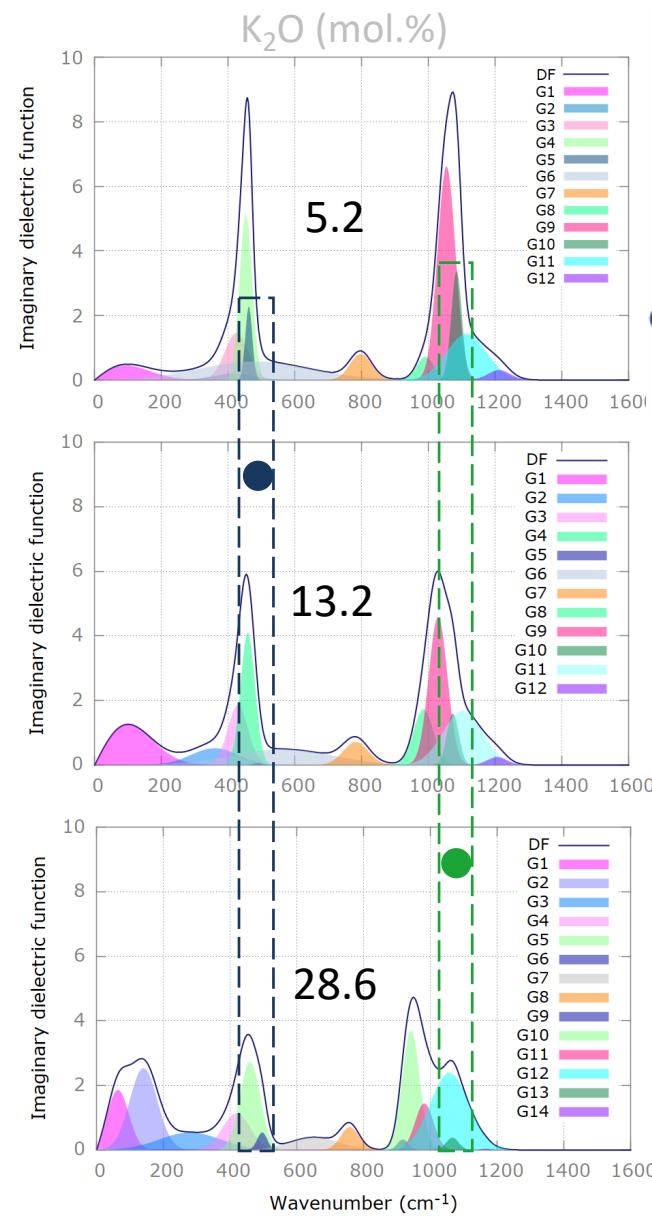


[NMR] Sen S, Youngman R E 2003 *J. Non-Cryst. Solids* 331 100

[BM] Binary model



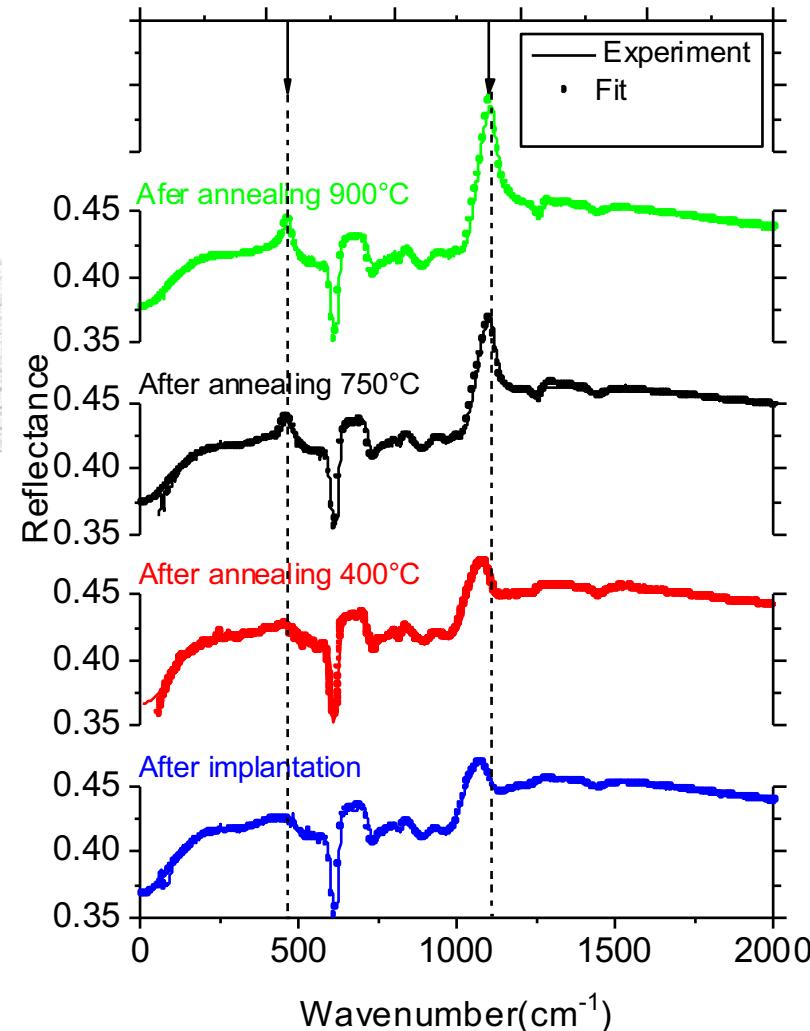
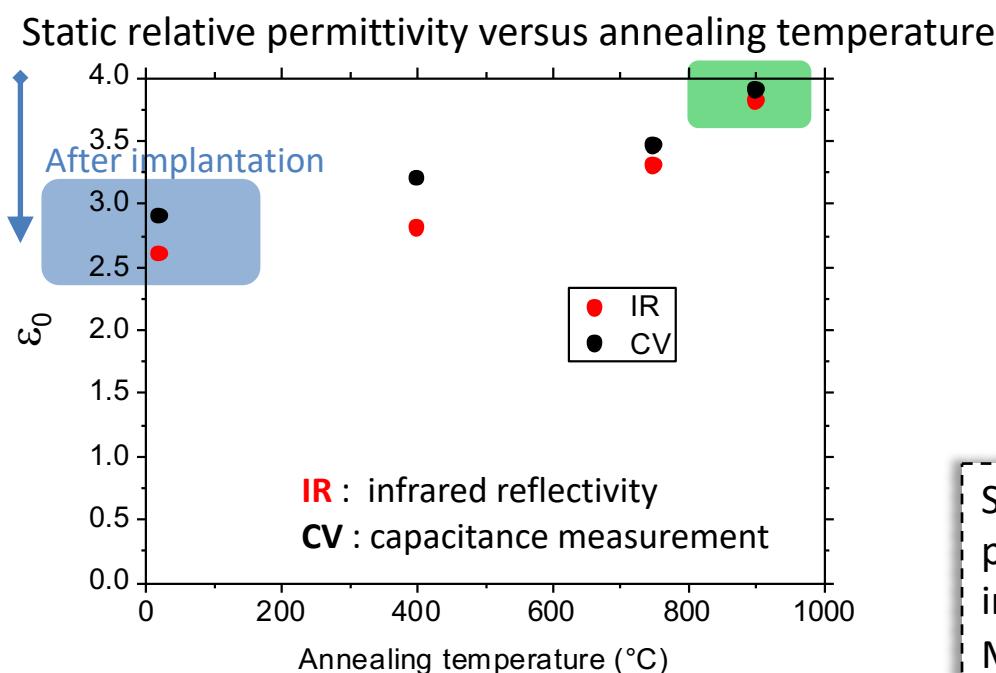
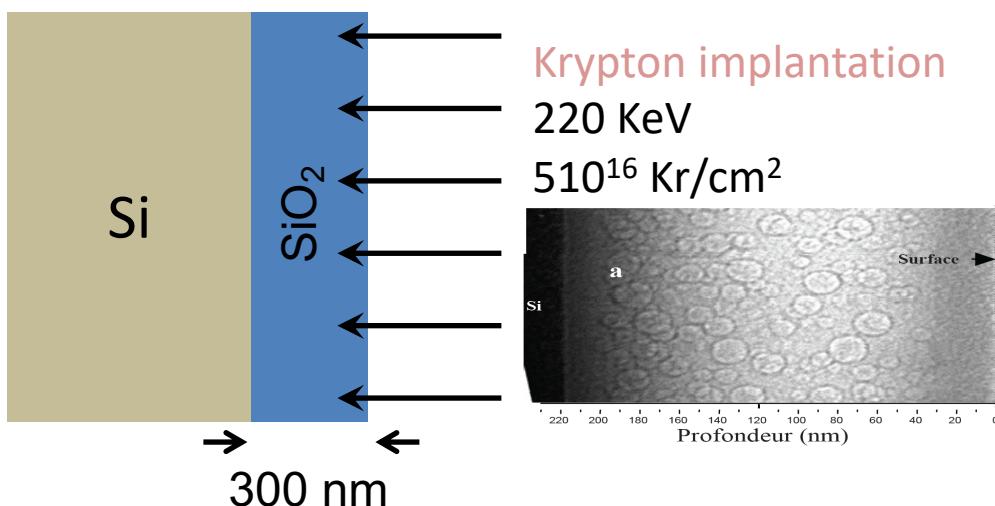
K_2O - SiO_2 glass system : medium range order



[NMR] Sen S, Youngman R E 2003 *J. Non-Cryst. Solids* 331 100

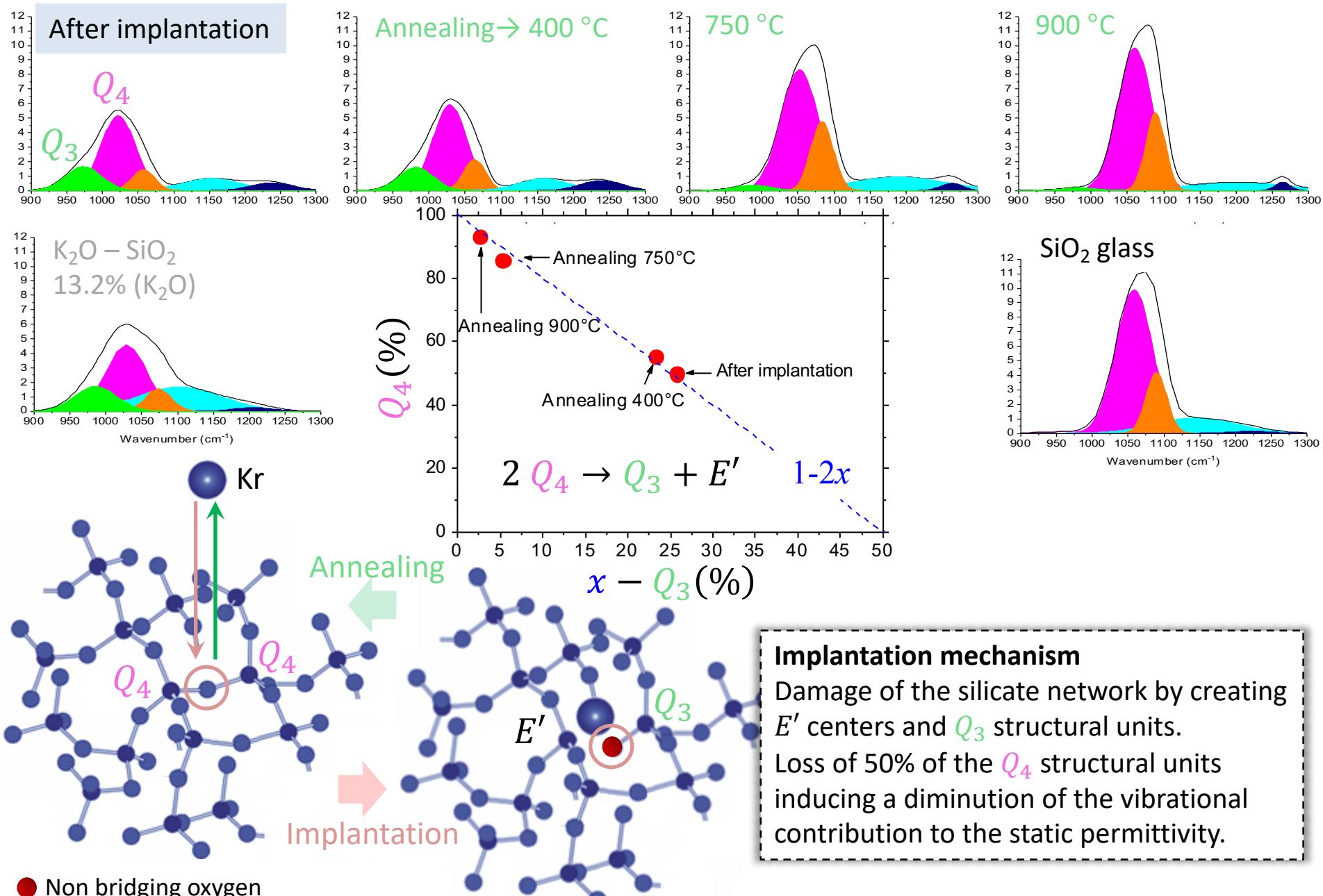
[NMR] Olivier L, Yuan X, Cormack A N, Jäger C 2001 *J. Non-Cryst. Solids* 293-295 53

SiO_2 thin film implanted with Krypton

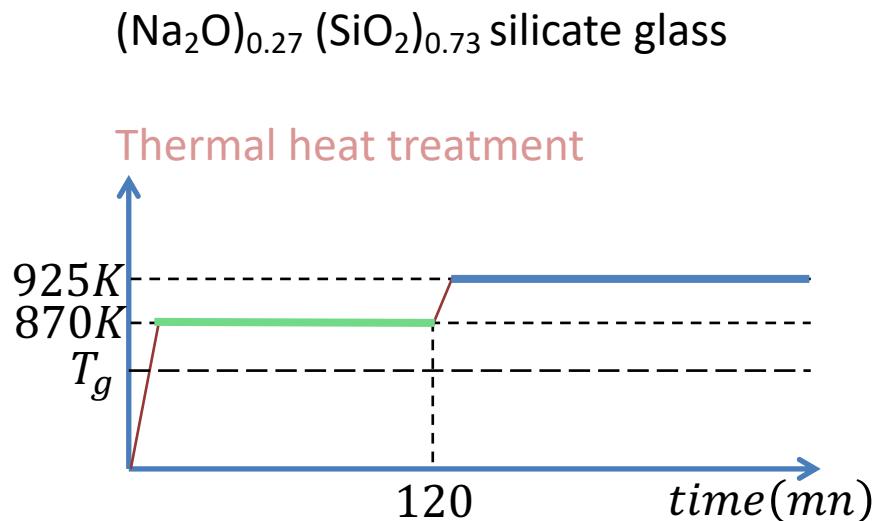
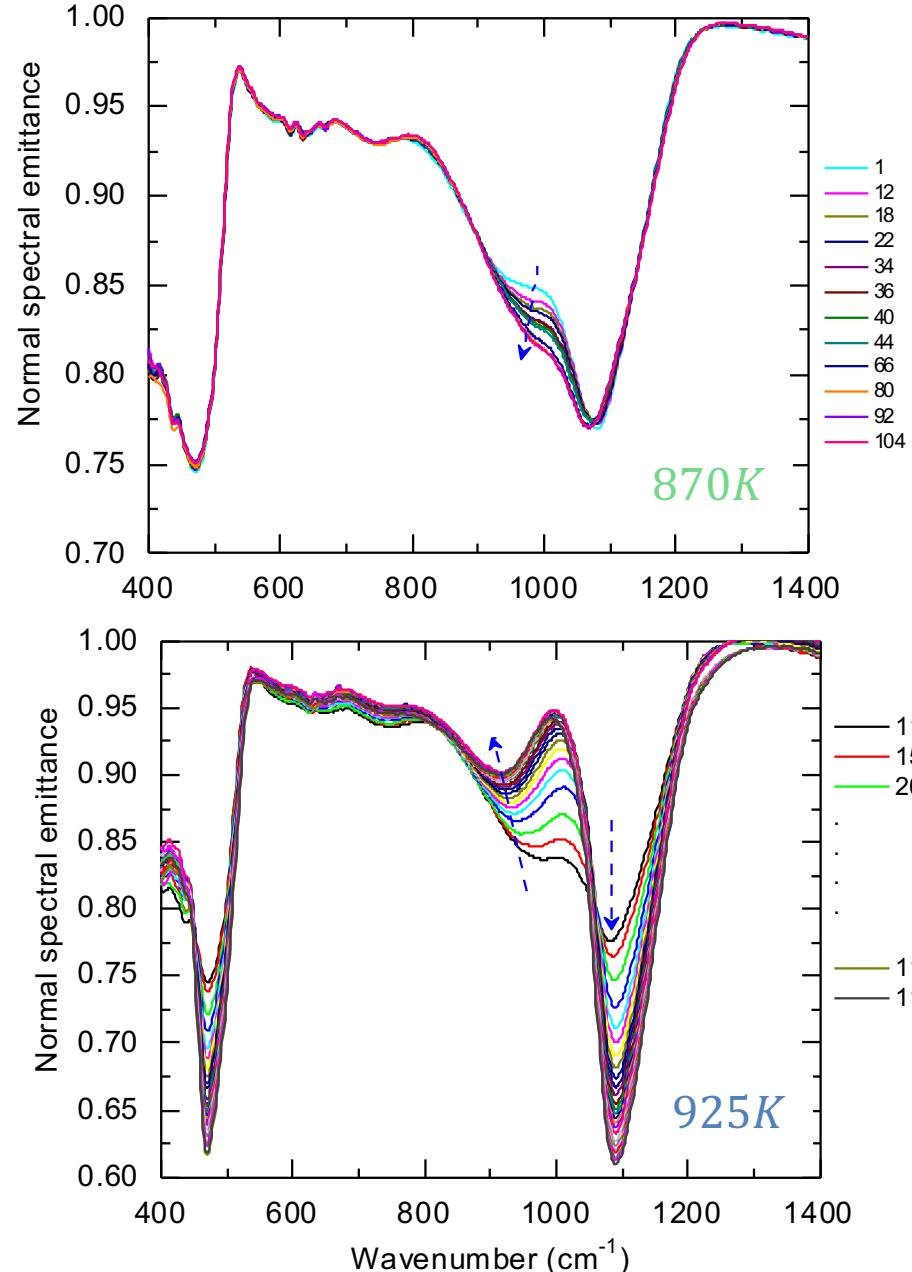


Strong decrease of the static relative permittivity of the SiO_2 thin film after implantation.
Material healing after annealing at 900 °C

SiO_2 thin film implanted with Krypton

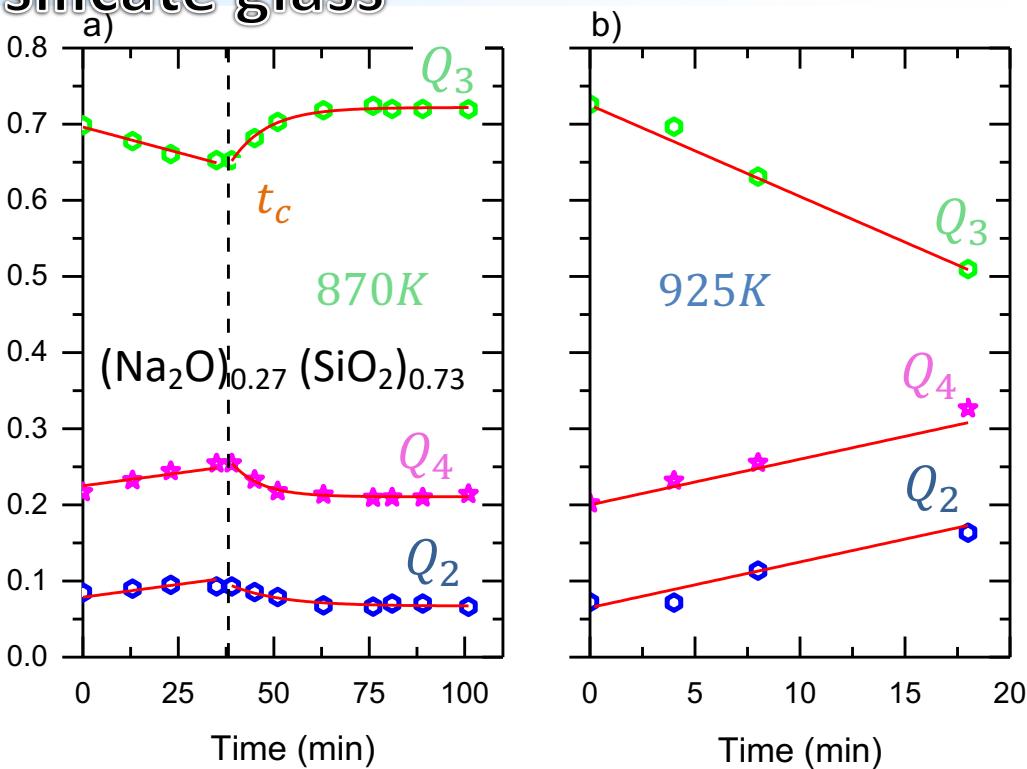
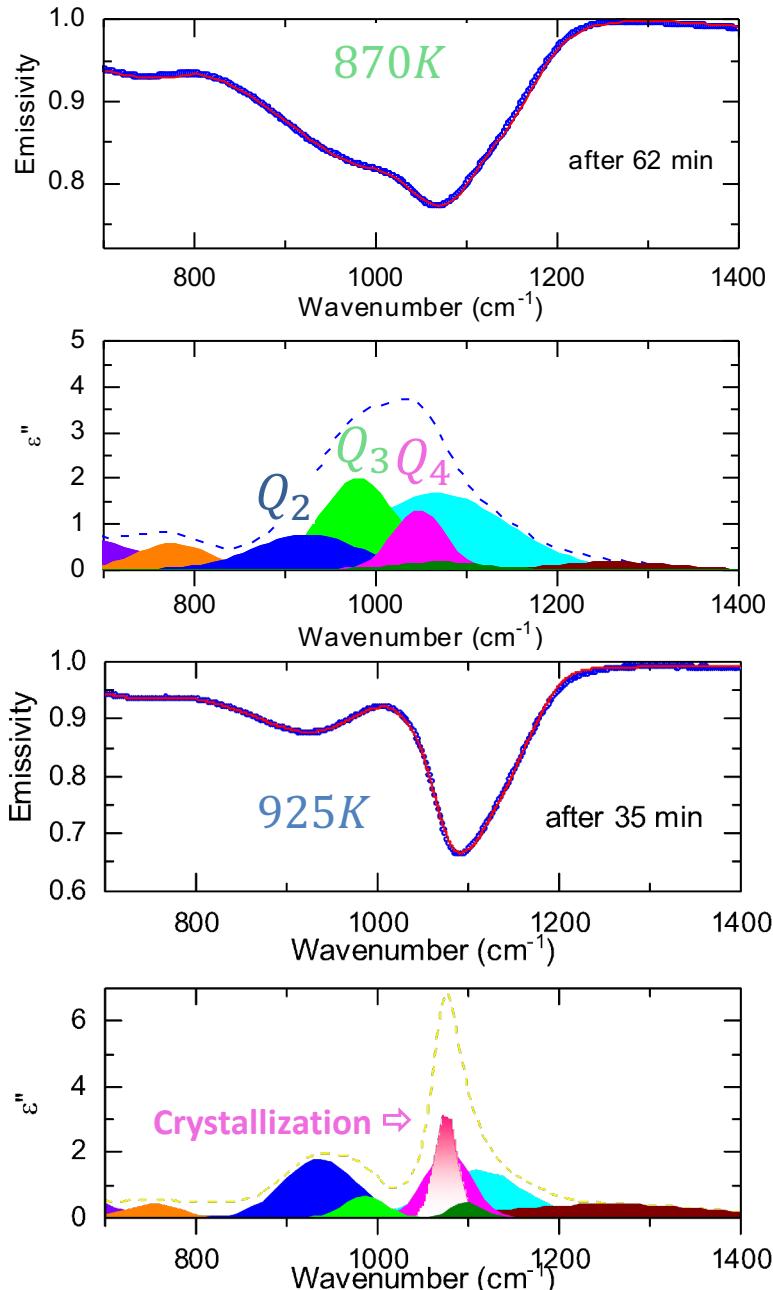


Structural relaxation of a silicate glass



Glass transition temperature (T_g): $\approx 730\text{K}$
Continuous acquisition of spectra during annealing at 870 K and 925K

Structural relaxation of a silicate glass



Annealing at 870 K does not lead to crystallization of the glass.
 $2Q_3 \leftrightarrow Q_2 + Q_4$

First step, small shift of the chemical equilibrium to the right.

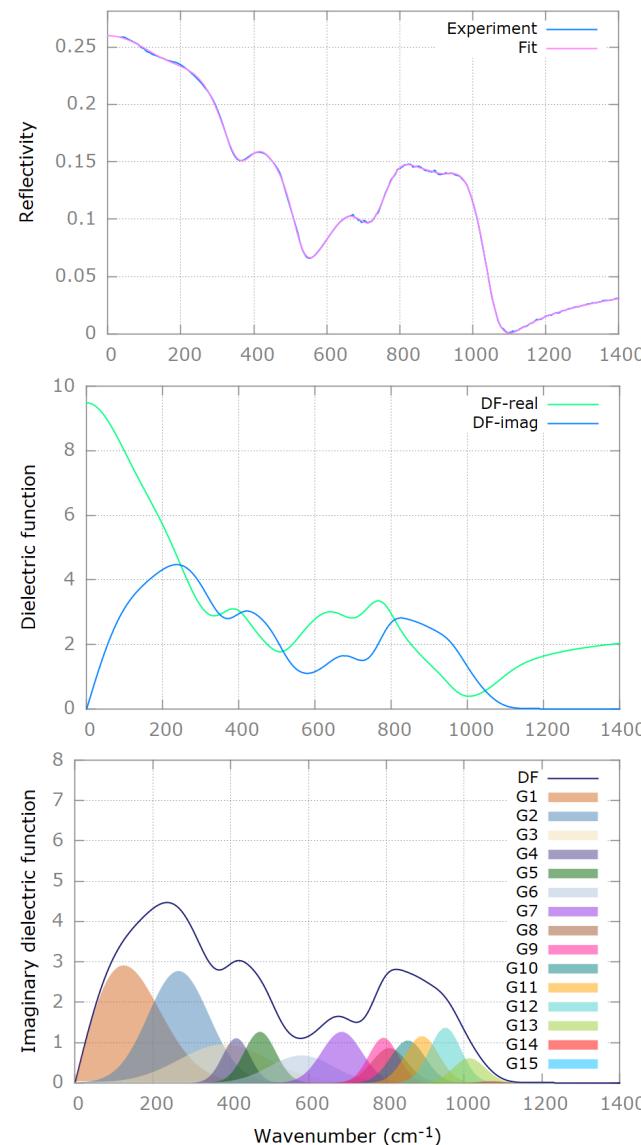
After t_c , structural relaxation ($\tau \approx 10 \text{ mn}$) and shift to the left of the chemical equilibrium.

$$Q_n(t) = c_n \exp\left(-\frac{t - t_c}{\tau}\right) + d_n$$

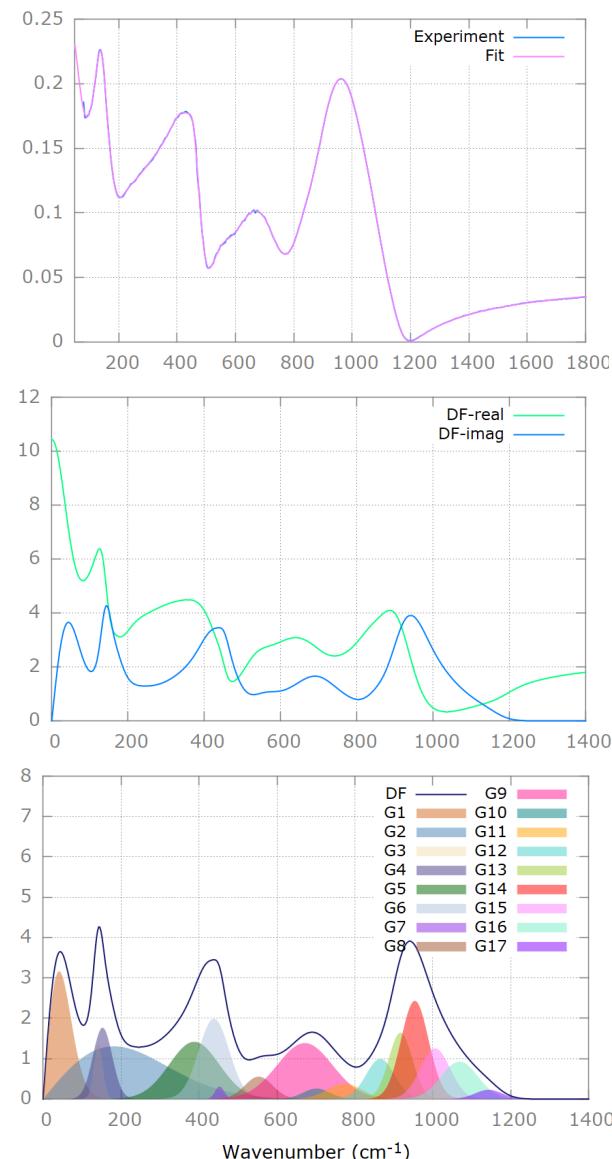
At 925 K crystallization is evidenced after 20 mn.

Infrared response of aluminosilicate glasses

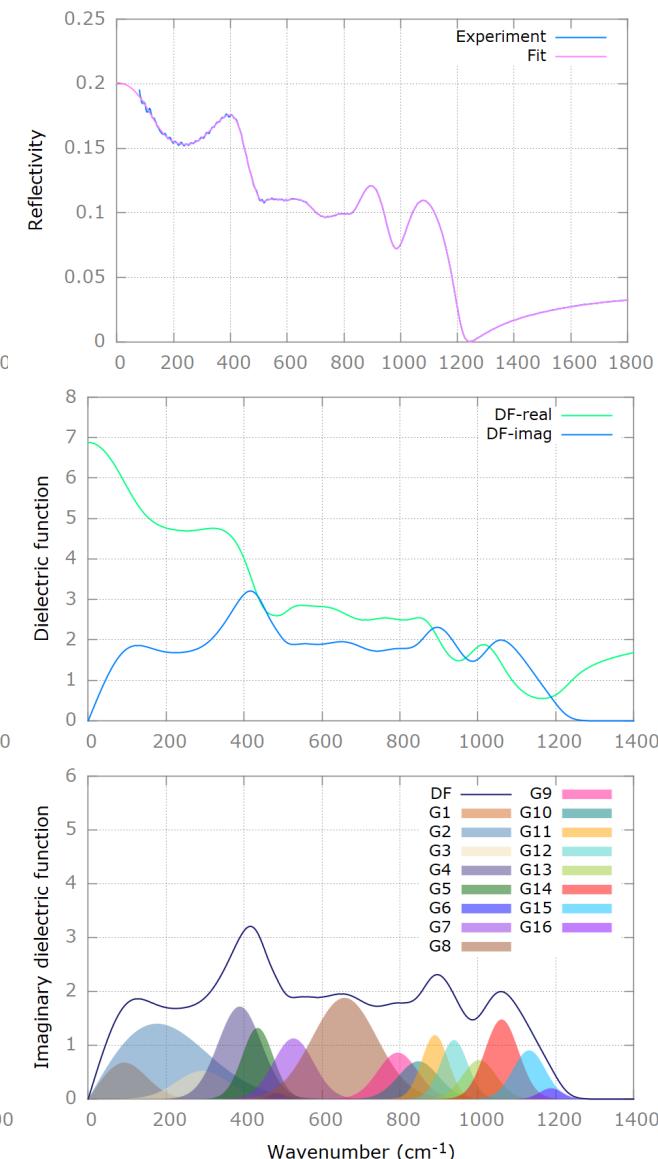
$\text{Ca}_2\text{Al}_2\text{SiO}_7$ glass



$\text{BaAl}_2\text{Si}_2\text{O}_8$ glass

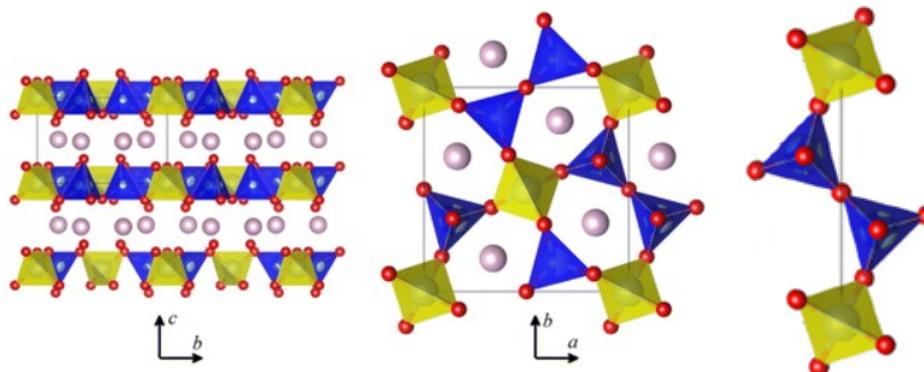


$\text{ZnAl}_2\text{Si}_2\text{O}_8$ glass

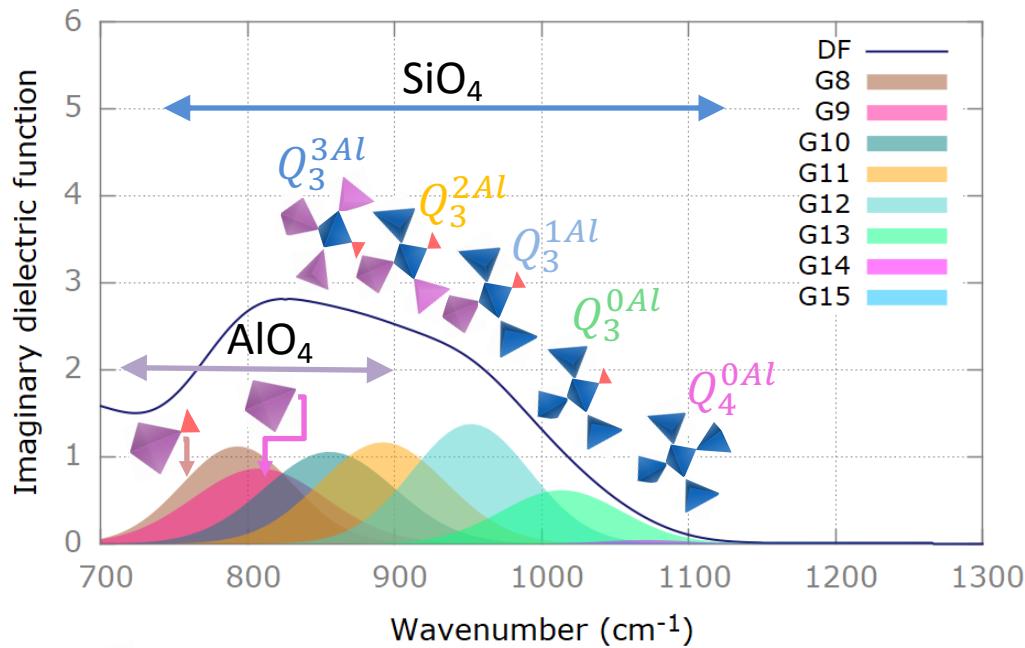


Infrared response of aluminosilicate glasses

Crystal structure of gehlenite



$\text{Ca}_2\text{Al}_2\text{SiO}_7$ glass



AlO_4 with a non bridging oxygen

Yellow tetrahedra : Wyckoff site 2a labelled T₁ is fully occupied by Al atoms



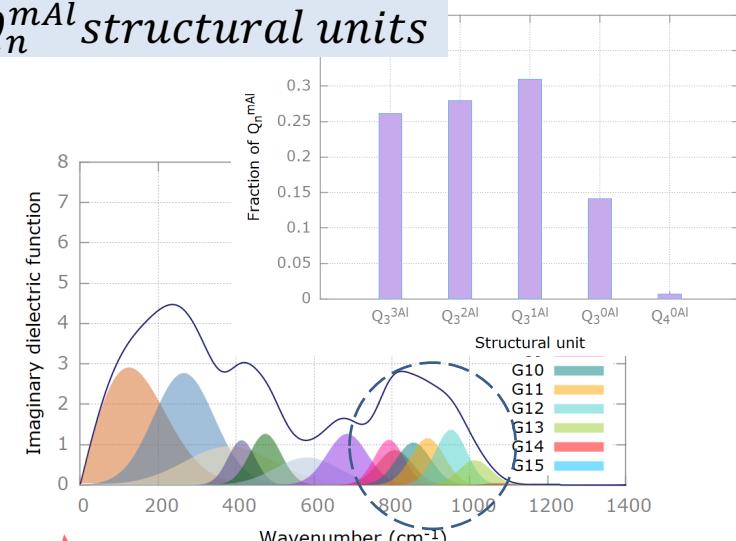
Blue tetrahedra : Wyckoff site 4e, labelled T₂ is filled with a mix of Al (50 %) and Si (50 %) atoms



100% $\text{Q}_3^{3\text{Al}}$



$Q_n^{m\text{Al}}$ structural units



SiO_4 with a non bridging oxygen

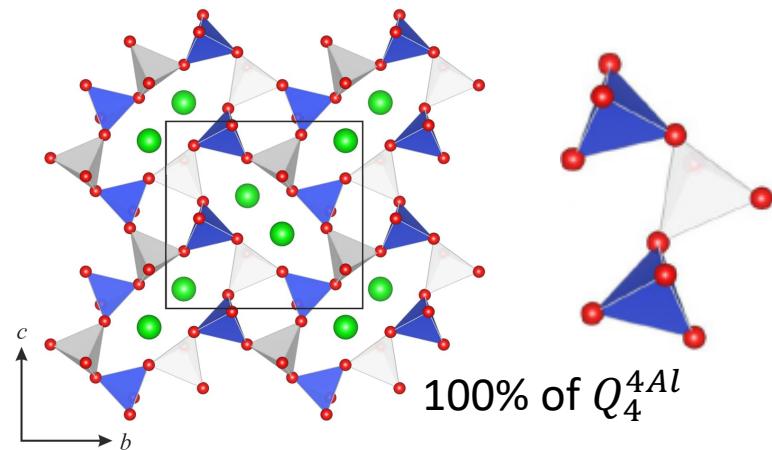
Access to structural information

$Q_n^{m\text{Al}}$ structural units

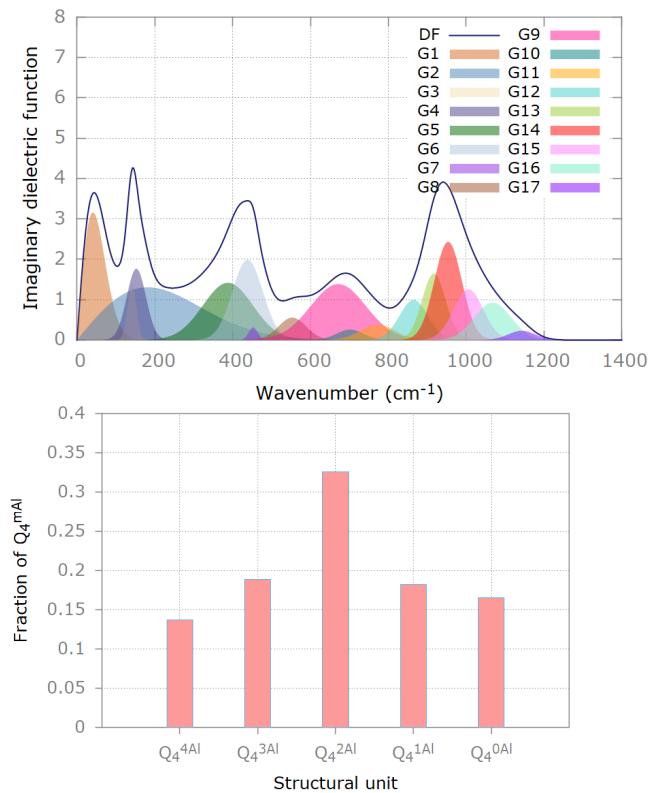
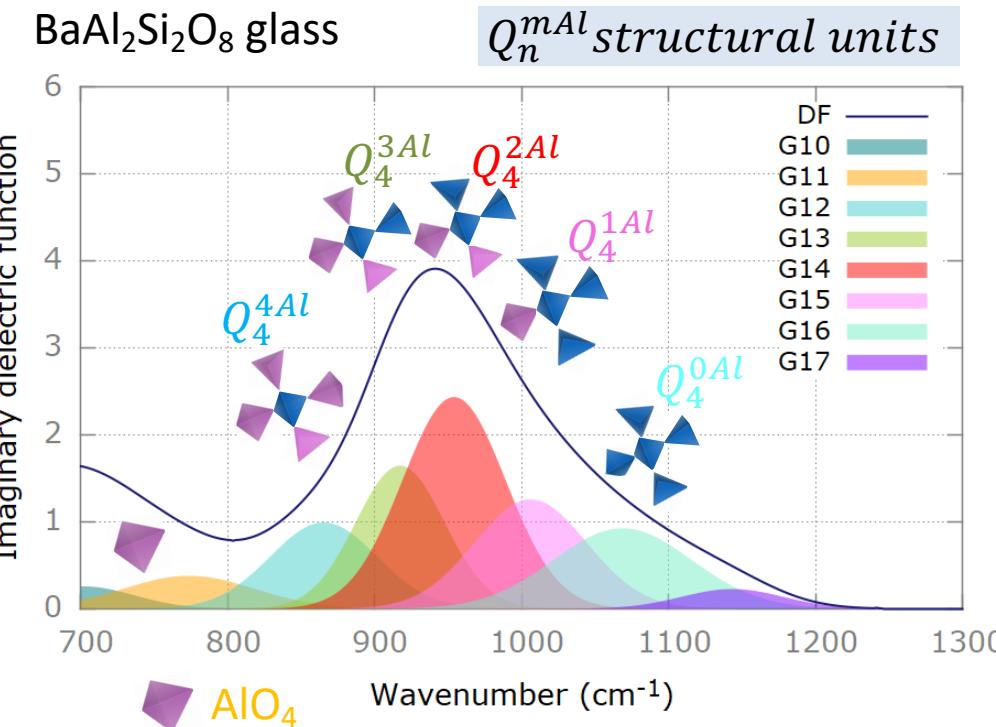
Nature of AlO_4 tetrahedra

Infrared response of aluminosilicate glasses

Crystal structure of $\text{BaAl}_2\text{Si}_2\text{O}_8$ (paracelsian)



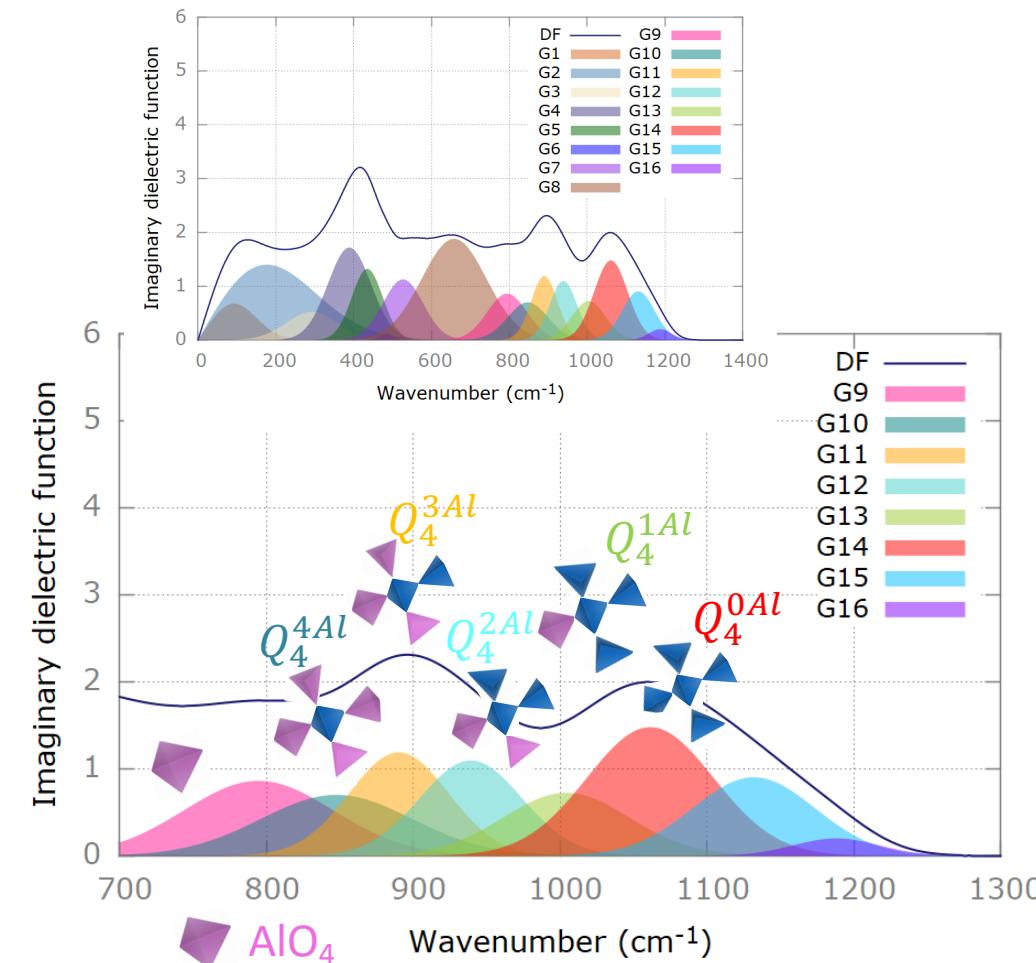
Blue tetrahedra : Al atoms (AlO_4) surrounded by 4 Al atoms.
Gray tetrahedra : Si atoms (SiO_4) surrounded by 4 Al atoms.



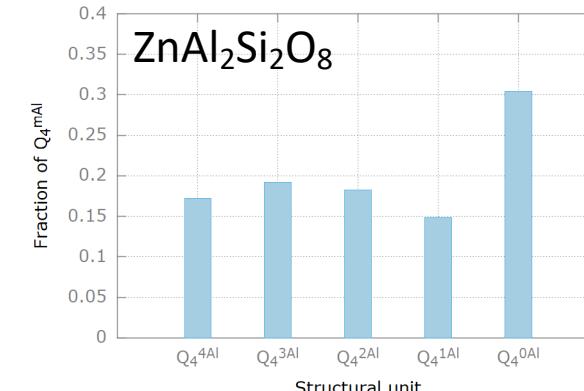
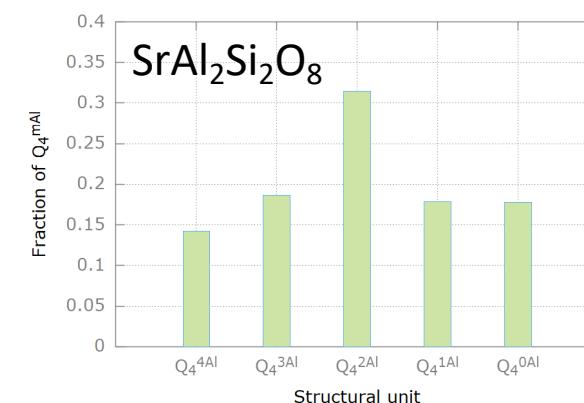
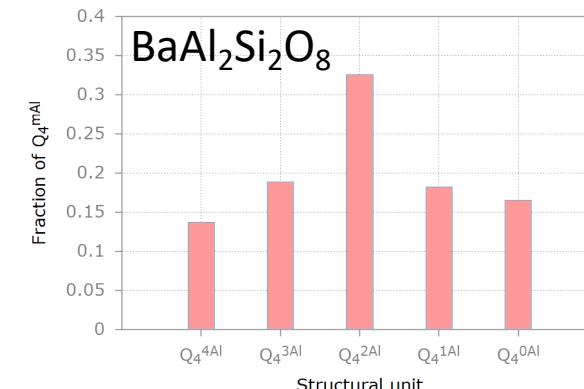
Broad distribution of Q_4^{mAl} structural units.
Al-O-Al bonds

Infrared response of aluminosilicate glasses

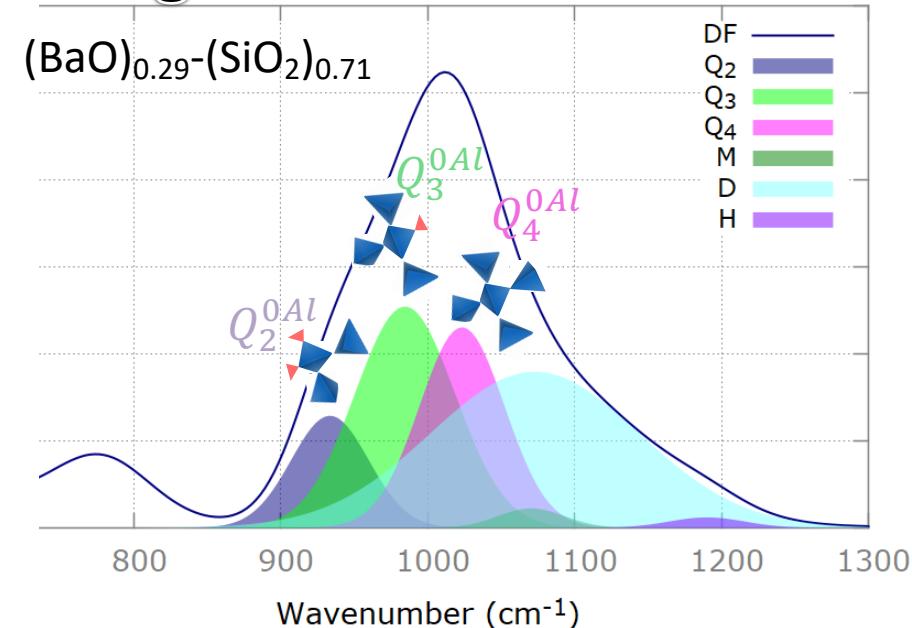
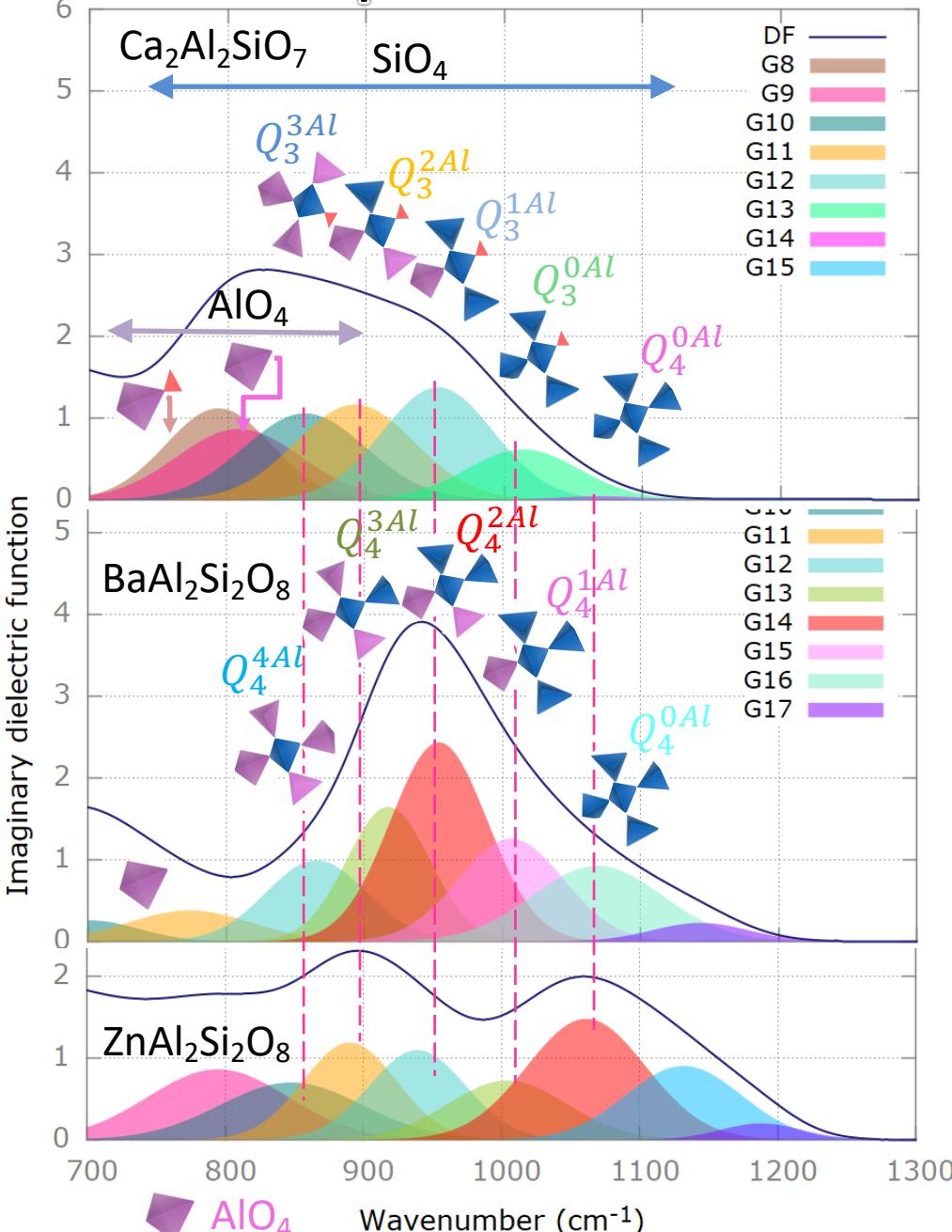
ZnAl₂Si₂O₈ glass



$Q_n^{m\text{Al}}$ structural units



Infrared response of aluminosilicate glasses

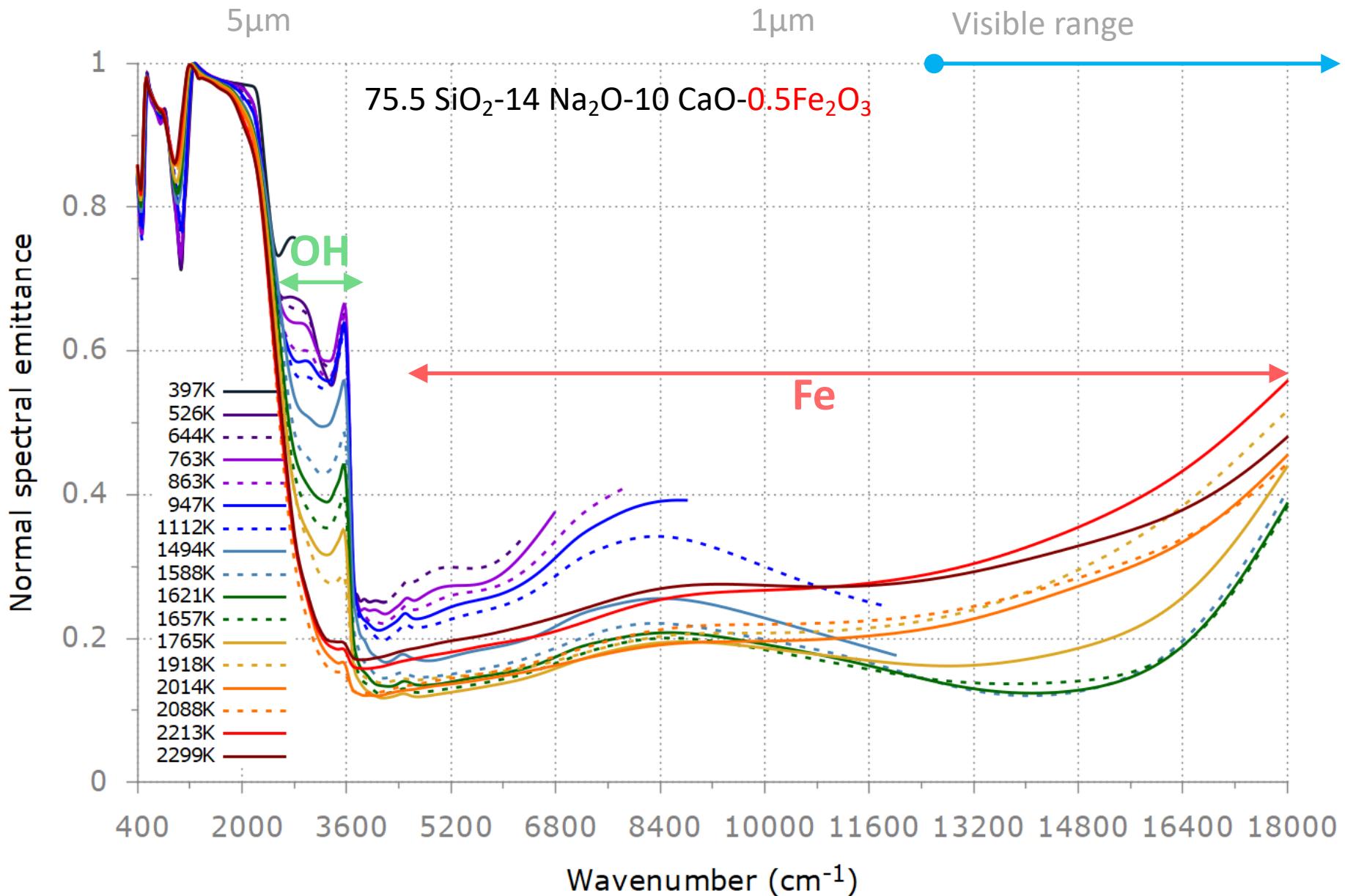


Q_n^{mAl} structural units

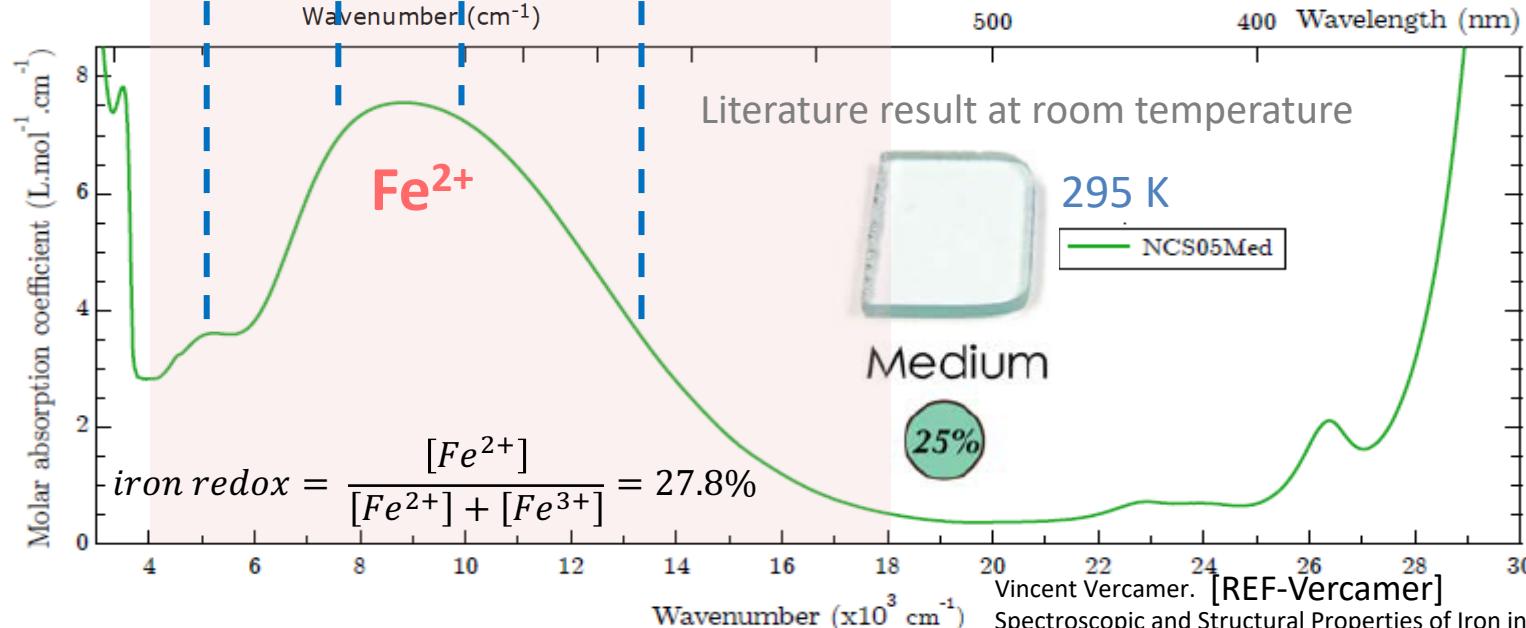
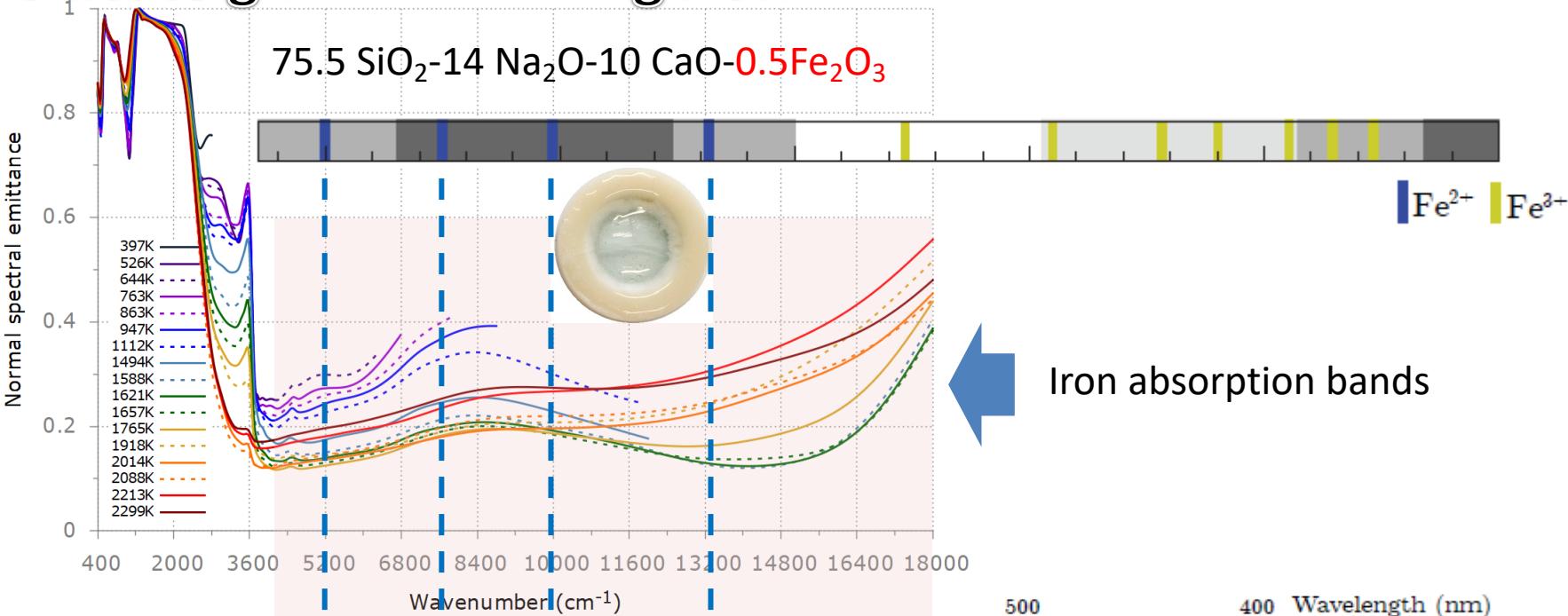
Absorption band position (cm^{-1})

$\cong 860$	$\cong 900$	$\cong 950$	$\cong 1010$	$\cong 1060$
Q_4^{4Al}	Q_4^{3Al}	Q_4^{2Al}	Q_4^{1Al}	Q_4^{0Al}
Q_3^{3Al}	Q_3^{2Al}	Q_3^{1Al}	Q_3^{0Al}	
		Q_2^{0Al}		

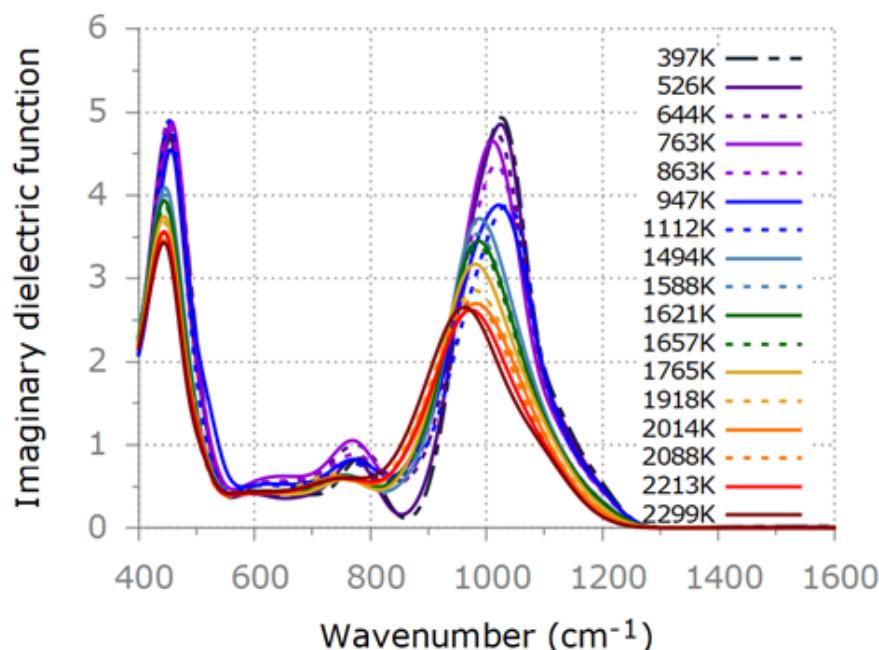
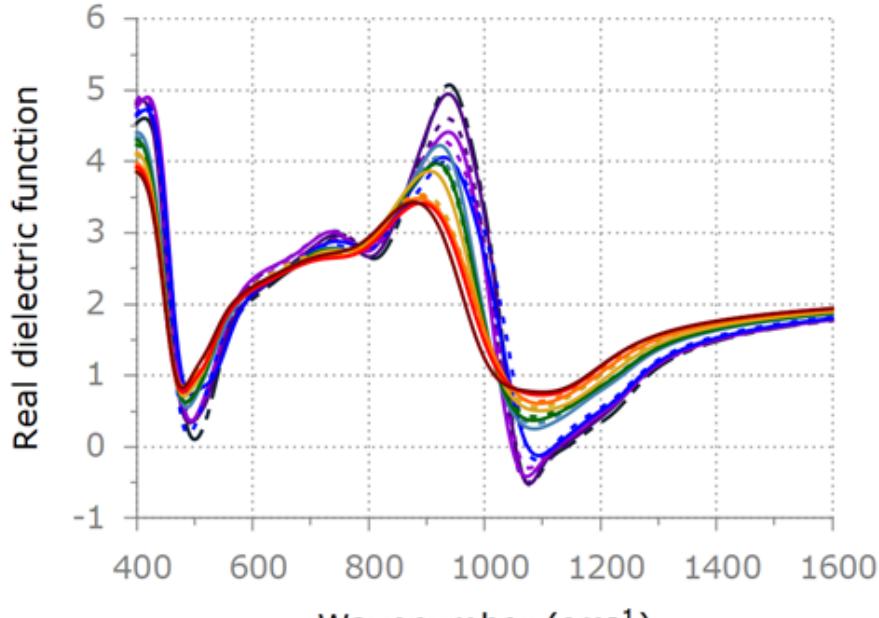
Silicate glass containing iron



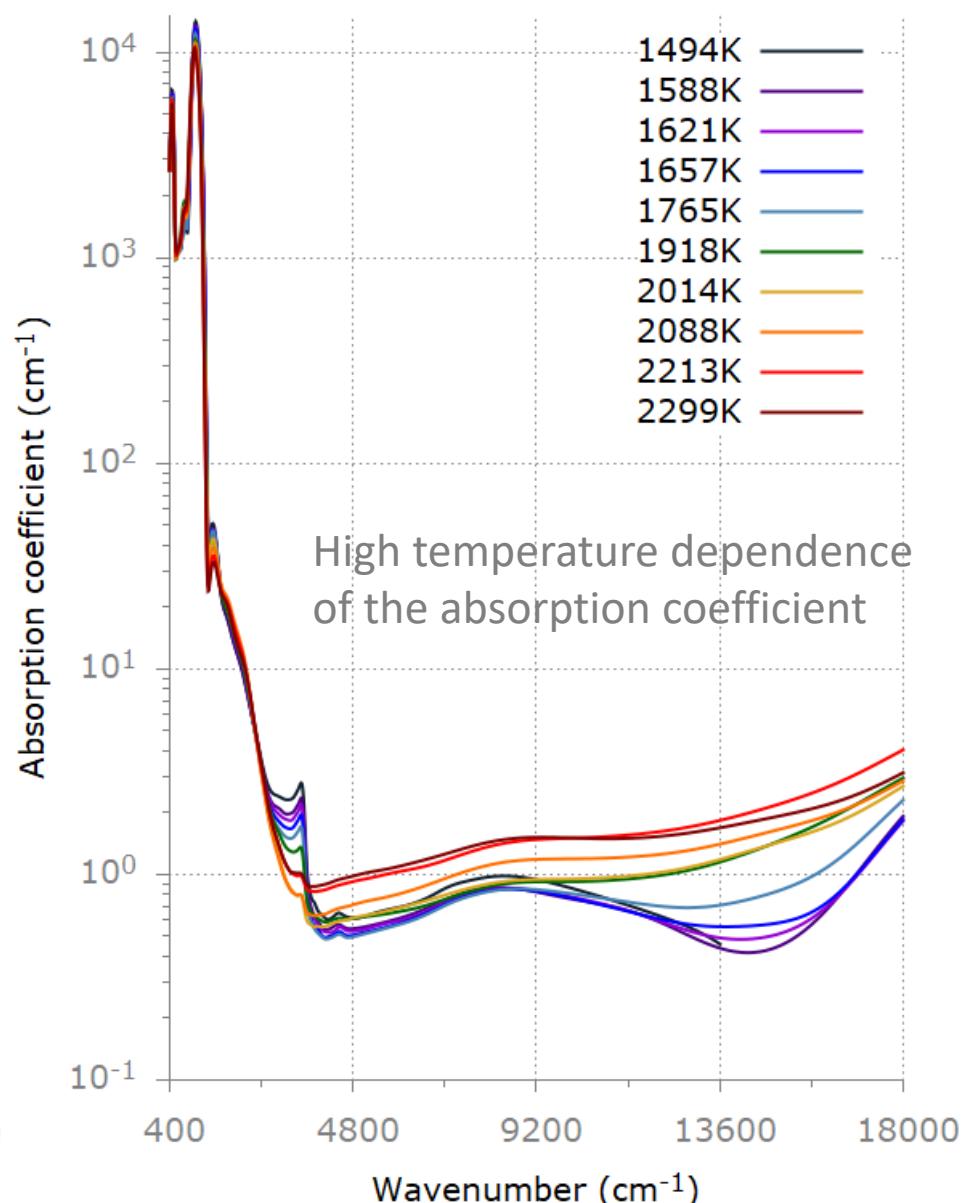
Silicate glass containing iron



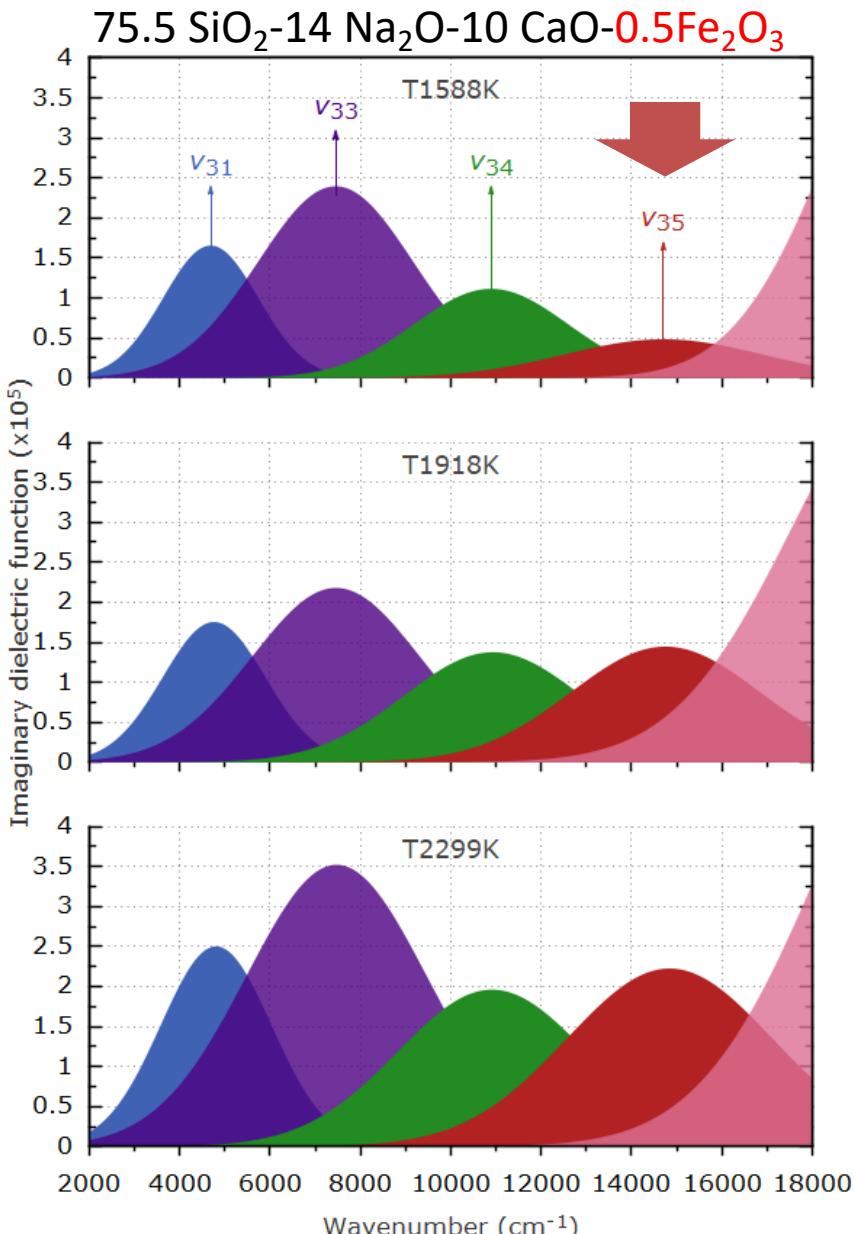
Silicate glasses containing iron



75.5 SiO_2 -14 Na_2O -10 CaO - $0.5\text{Fe}_2\text{O}_3$



Silicate glasses containing iron



Fit of Fe²⁺ bands with 3 Gaussian functions for NCS05Red [REF-Vercamer]

	Position (cm^{-1})	σ (cm^{-1})	FWHM (cm^{-1})	Intensity (cm^{-1})	$\varepsilon_{\text{Fe}^{2+}}$ (L/mol/cm)	Area (cm^{-2})
NCS05Red fit3						
#1	4848	492	1159	0.75	4.8	651.6
#2	7812	1277	3007	0.96	6.2	2181.4
#3	9775	3177	7482	3.65	23.7	20557.5

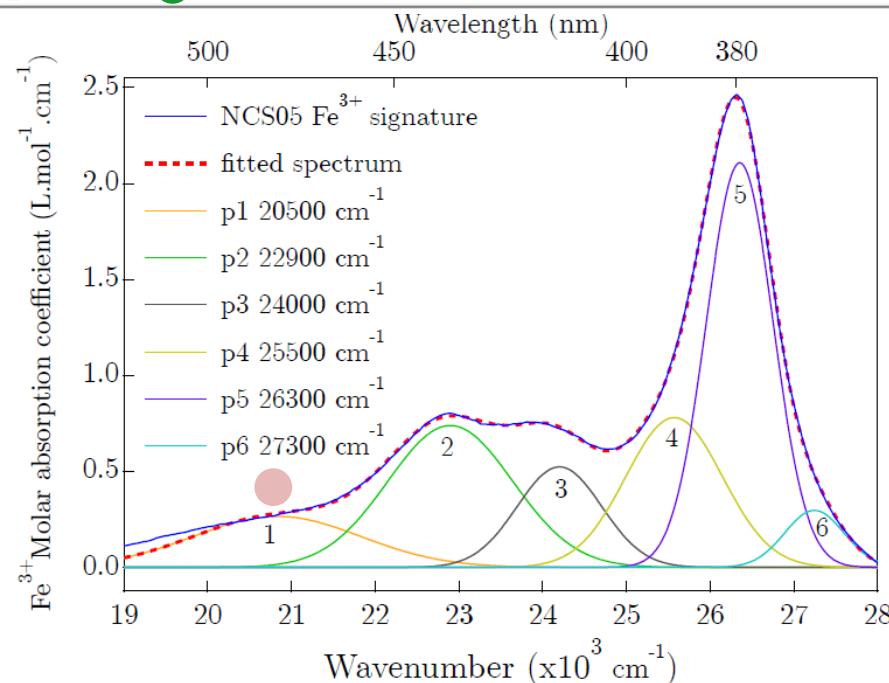
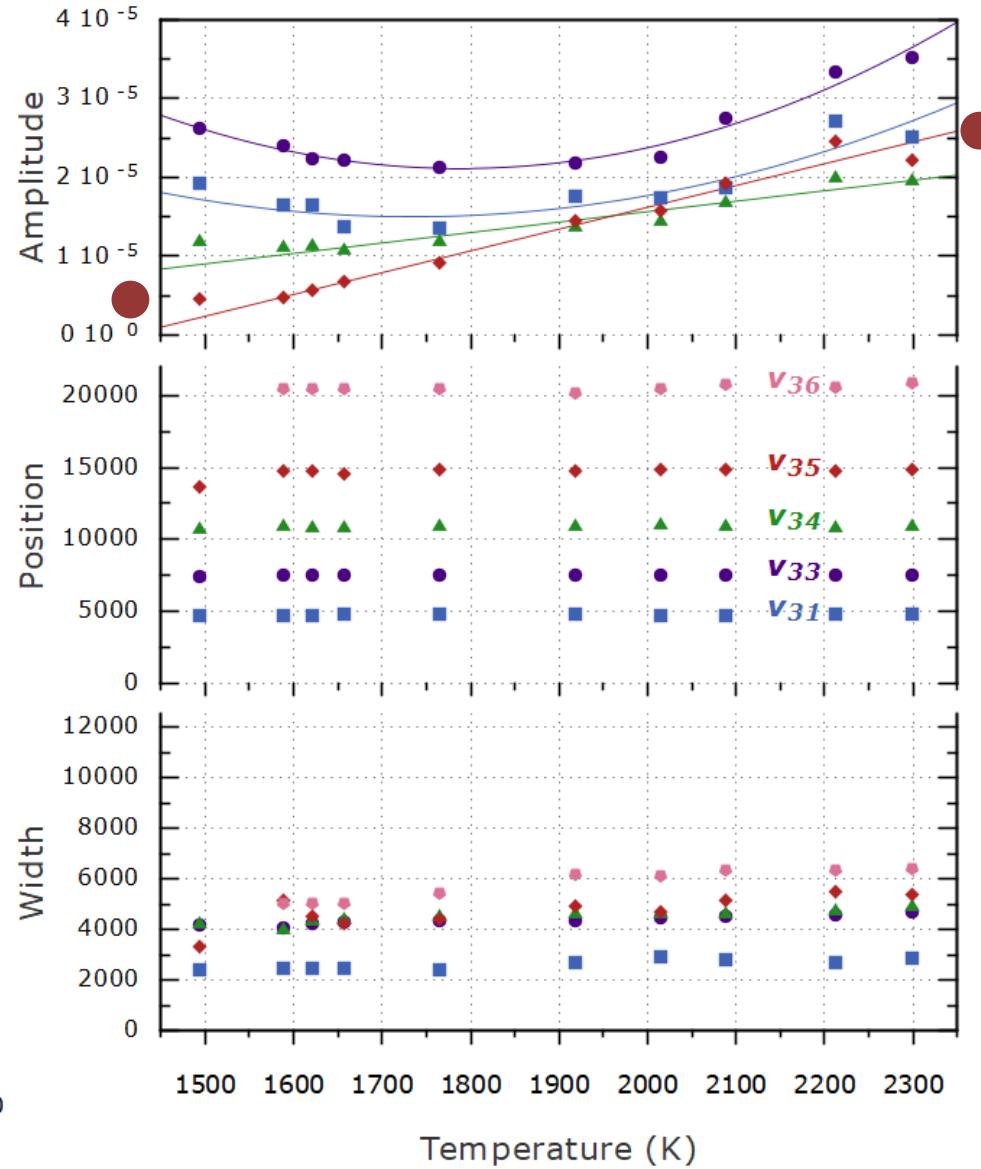
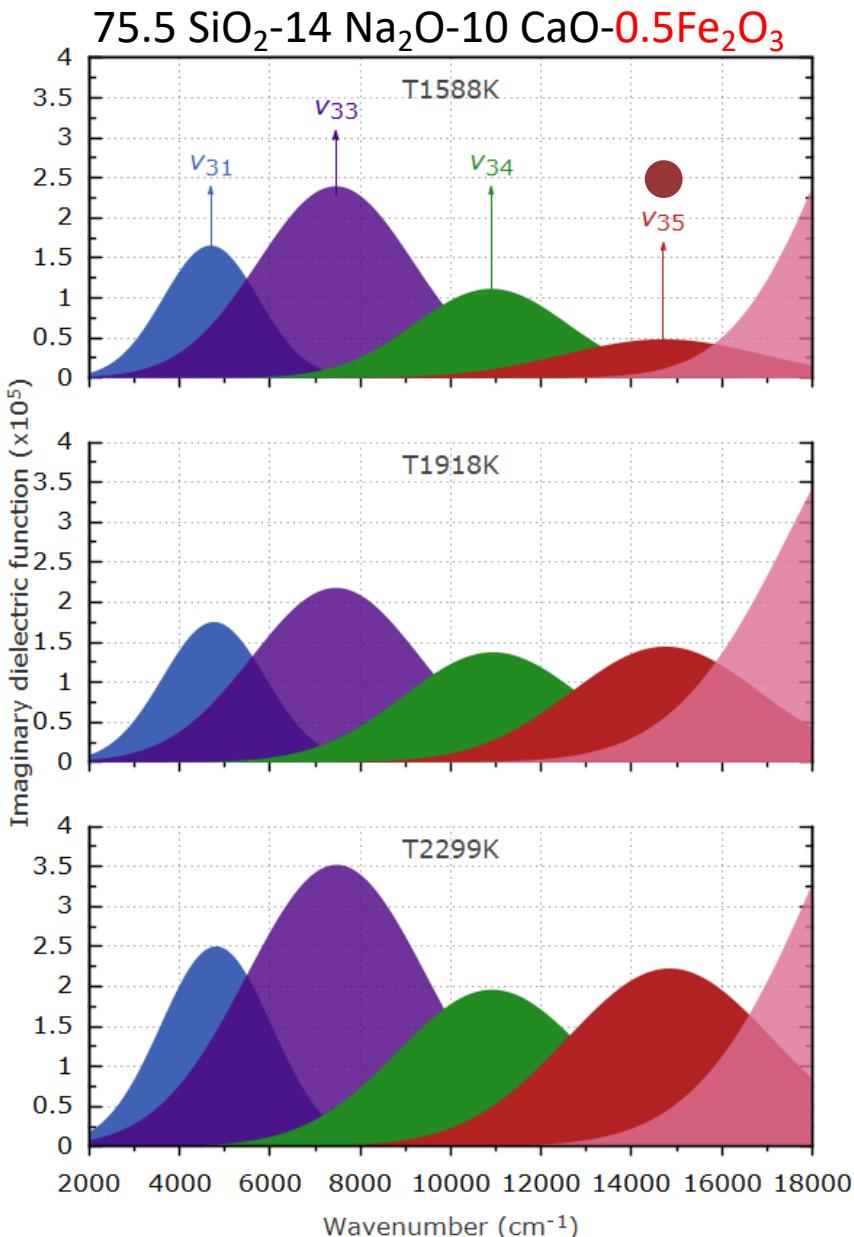


Figure 5.15 – Molar absorption coefficient of Fe³⁺ in the soda-lime oxidized glass (NCS05Ox) after UV-edge removal. Example of Fe³⁺ bands fitted with 6 Gaussians.

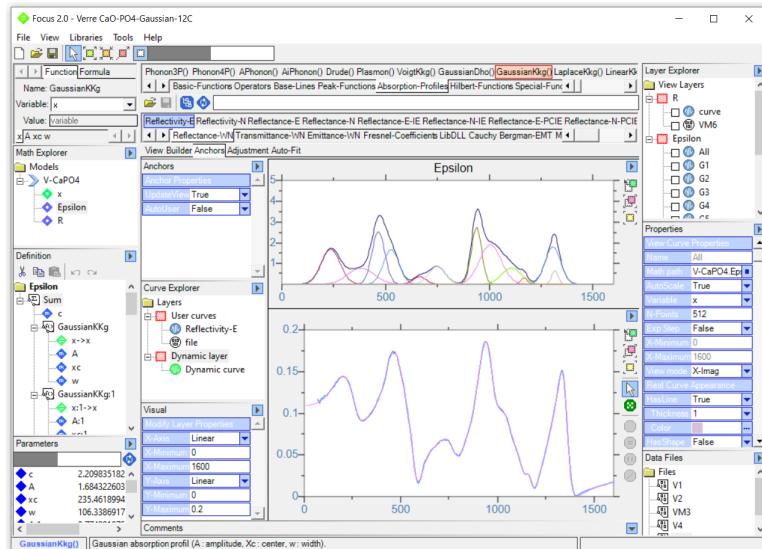
Intervalence Charge Transfer (IVCT) ●
Transfer of an electron between two adjacent Fe²⁺-Fe³⁺ ions.
Strong increase at high temperature in the melt

Silicate glasses containing iron

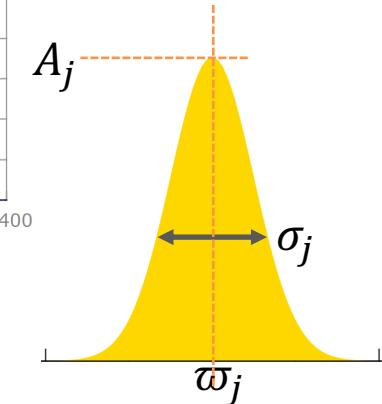
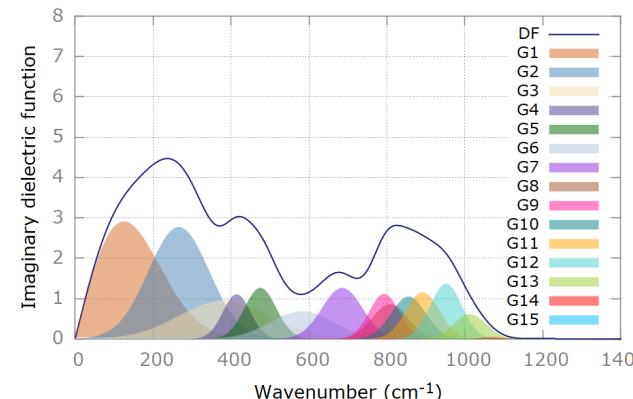


Conclusion

Infrared spectroscopy is a powerful tool to investigate the structural and optical properties of glasses and melts at high temperature.



Infrared spectroscopy practical



Thank you for your attention

