

# Coordination Numbers of Glass Formers – Composition-dependence

Alex Hannon  
ISIS Facility, UK



alex.hannon@stfc.ac.uk  
<http://alexhannon.co.uk>

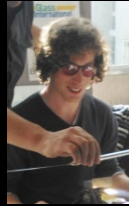
*GDR-Verres Spring School  
27-31 March  
Cargèse, Corsica, France*



# Acknowledgements

With thanks to...

*Oliver Alderman*  
Materials Development Inc,  
USA



*Rui Almeida, Daniela di Martino, Luis Santos*  
Instituto Superior Técnico, Lisbon



*Norimasa Umesaki*  
Osaka University, Japan



*Emma Barney*  
Nottingham University,  
UK



*Masahiro Tatsumisago*  
Osaka Prefecture University,  
Japan



*Diane Holland*  
Warwick University, UK



*Robin Orman*  
Johnson Matthey, UK



*Steve Feller*  
Coe College, USA



# Overview

1. Neutron diffraction
2. Pure  $\text{GeO}_2$  glass
3.  $\text{Cs}_2\text{O-GeO}_2$  glasses
4. Charge avoidance model
5.  $\text{Li}_2\text{O-GeO}_2$  glasses
6.  $\text{CaO-GeO}_2$  glasses
7. Pure amorphous  $\text{TeO}_2$
8.  $\text{K}_2\text{O-TeO}_2$  glasses

## 5

# NEUTRON DIFFRACTION TECHNIQUES FOR STRUCTURAL STUDIES OF GLASSES

Alex C. Hannon

*ISIS Facility, Rutherford Appleton Laboratory, Chilton, Didcot,  
Oxon, UK*

## 5.1 INTRODUCTION

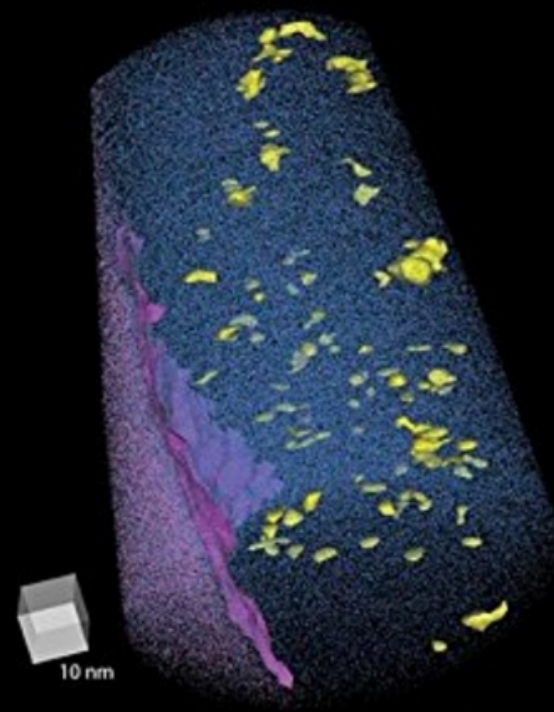
Neutron diffraction (ND) is an important experimental technique for the investigation of the structure of glasses. It can be used to study oxide glasses, chalcogenide glasses, metallic glasses, amorphous semiconductors, molecular glasses, amorphous polymers, organic glasses, and so on. An ND experiment yields a measurement of the distribution of interatomic distances that can be more accurate than for any other experimental method. The shortest distances in the glass (the short range order, SRO) can be characterized in terms of coordination numbers, bond lengths, and other short distances. These can be measured very accurately by ND, and used to determine the coordination polyhedra that form the basis of the glass structure. The way in which these units connect together (the intermediate range order, IRO) is also probed by ND, although in a more subtle way, and its investigation usually requires some kind of modeling of the ND results. The results of an ND experiment can be predicted exactly for a structural model, and hence ND provides a rigorous test of structural models.

The main aim of this chapter is to provide empirical information to enable a new researcher, such as a research student, to plan and perform an ND investigation of the structure of glass samples, to analyze the experimental data, and to begin to interpret

*Modern Glass Characterization*, First Edition. Edited by Mario Affatigato.

© 2015 The American Ceramic Society and John Wiley & Sons, Inc. Published 2015 by John Wiley & Sons, Inc.

Please also see this long (83 pages) book chapter



## Modern Glass Characterization

EDITED BY MARIO AFFATIGATO



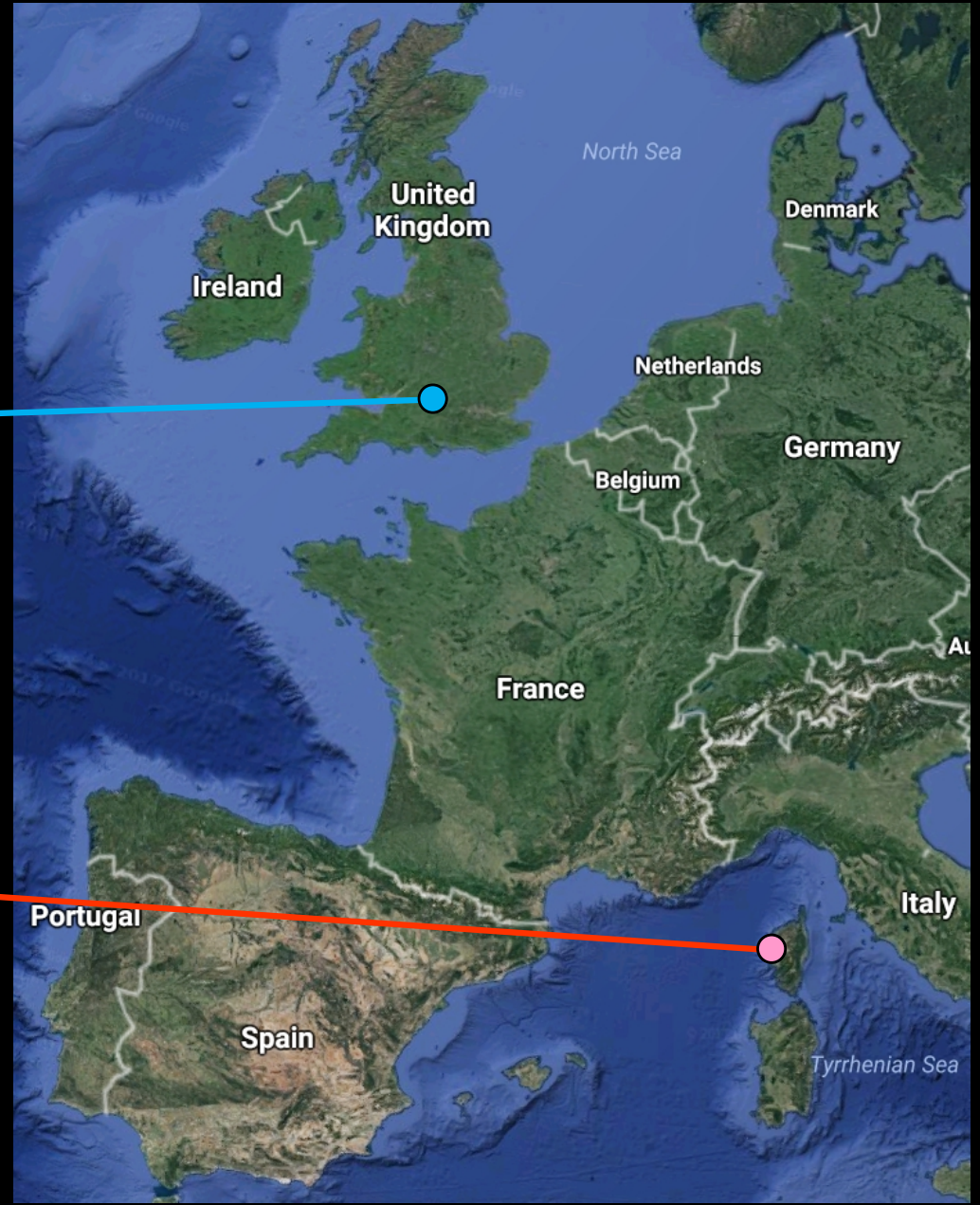
WILEY

# The ISIS Facility

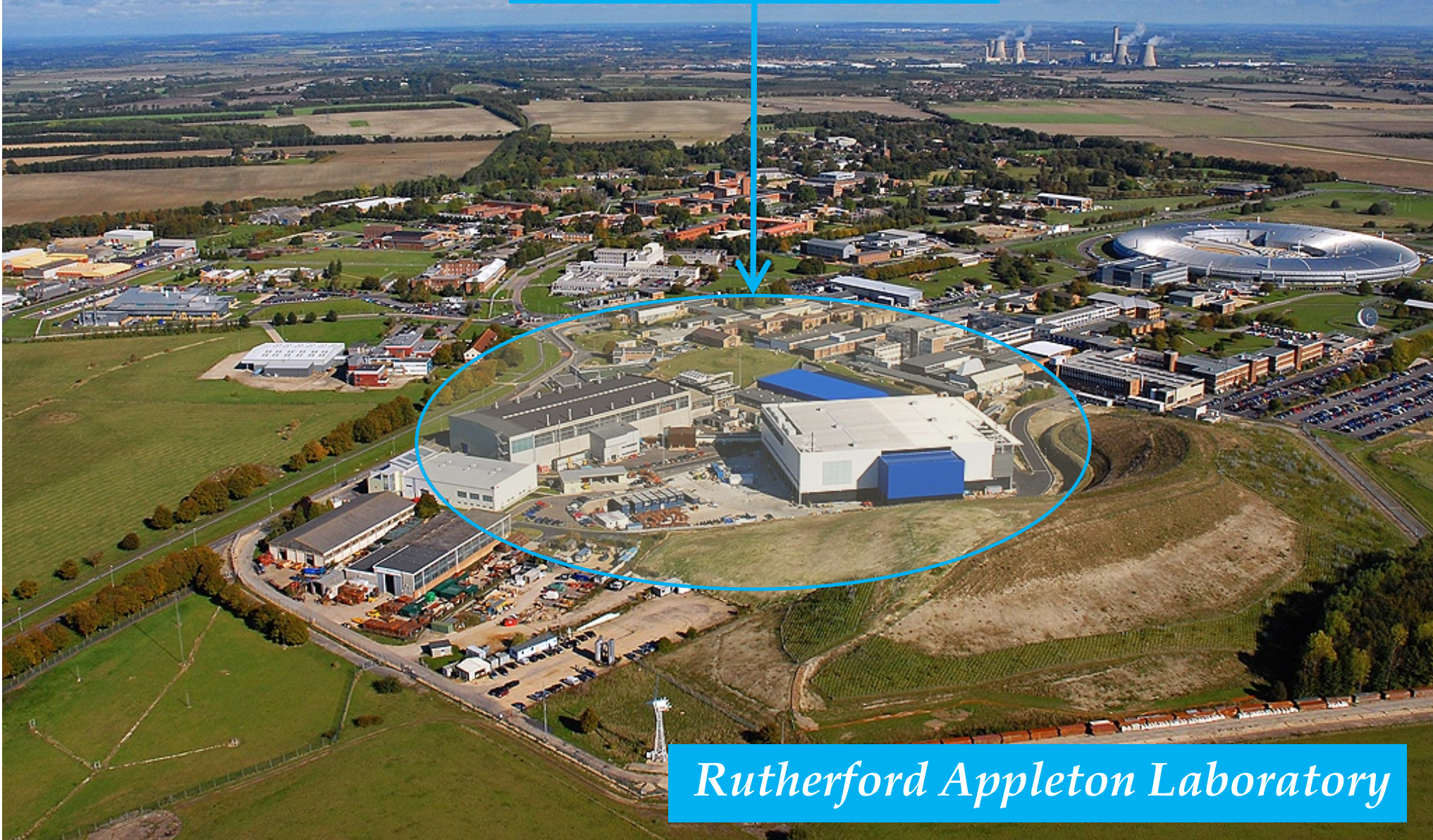


The world's leading pulsed neutron and muon source

Nous sommes ici



# ISIS Facility, Neutron Source



*Rutherford Appleton Laboratory*

# ISIS – the name

- ISIS is not an acronym (Intense Safety Instruction Seminary?)
- ISIS is not involved in Syria or Iraq
- ISIS is the Egyptian goddess of rebirth



*Isis was the wife of the god Osiris.  
His brother, Seth, slew Osiris and dropped  
his body into the Nile.  
Isis rescued the body of her husband.  
Seth stole the body and hacked it into fourteen pieces.  
Isis gathered together his pieces and bound  
him together to make him whole.*



- The ISIS accelerator was constructed from the parts of a previous nuclear physics accelerator.



# ISIS Neutron Source from Above

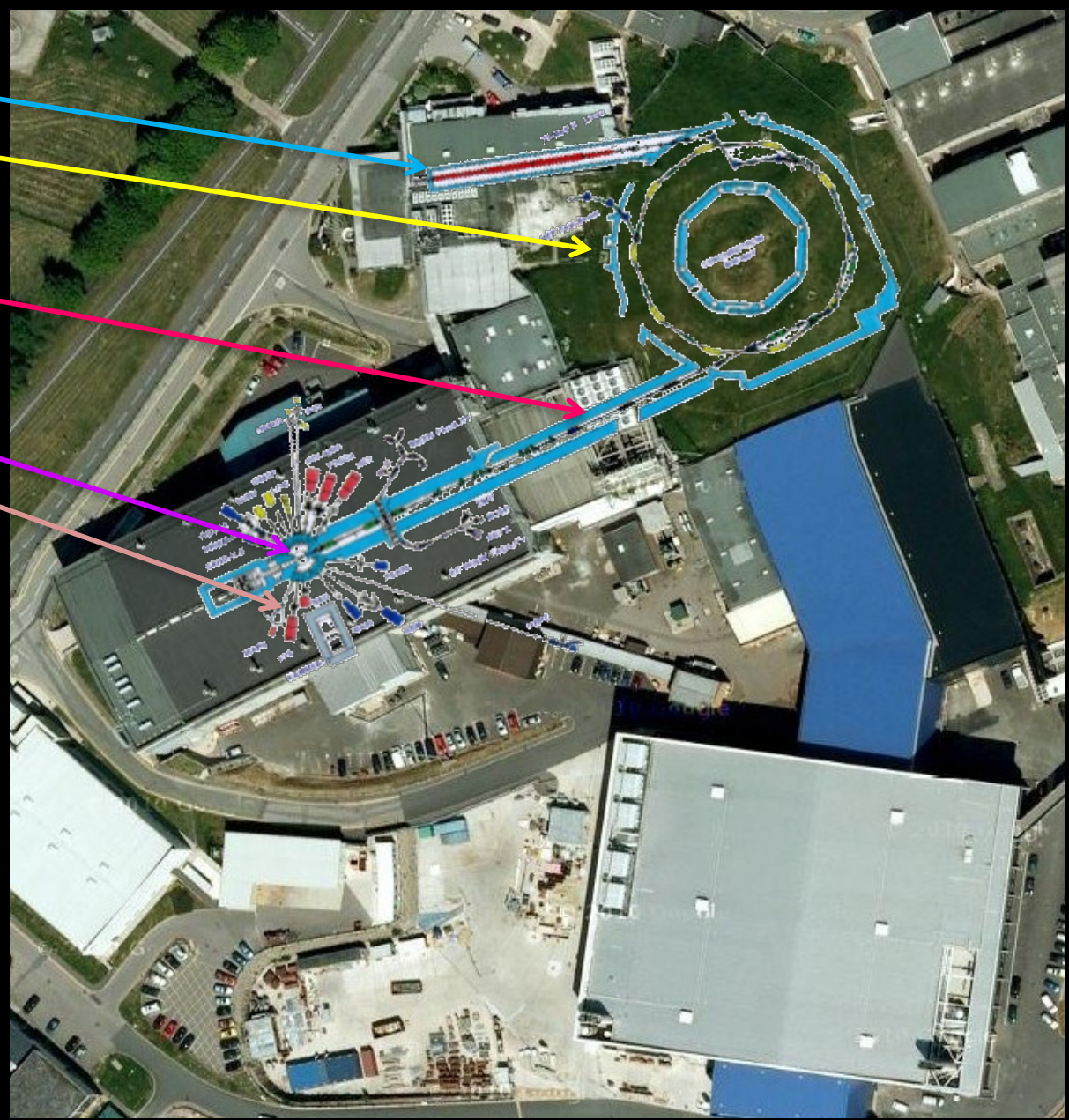
H- Linac

Proton synchrotron

Proton beam

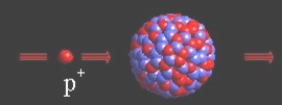
Neutron target

Neutron scattering instruments

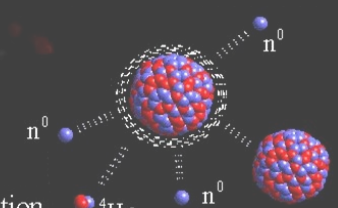


Spallation: Energetic proton  $\rightarrow$  heavy nucleus  $\rightarrow$  neutrons + lighter nucleus

800 MeV proton



Tantalum nucleus

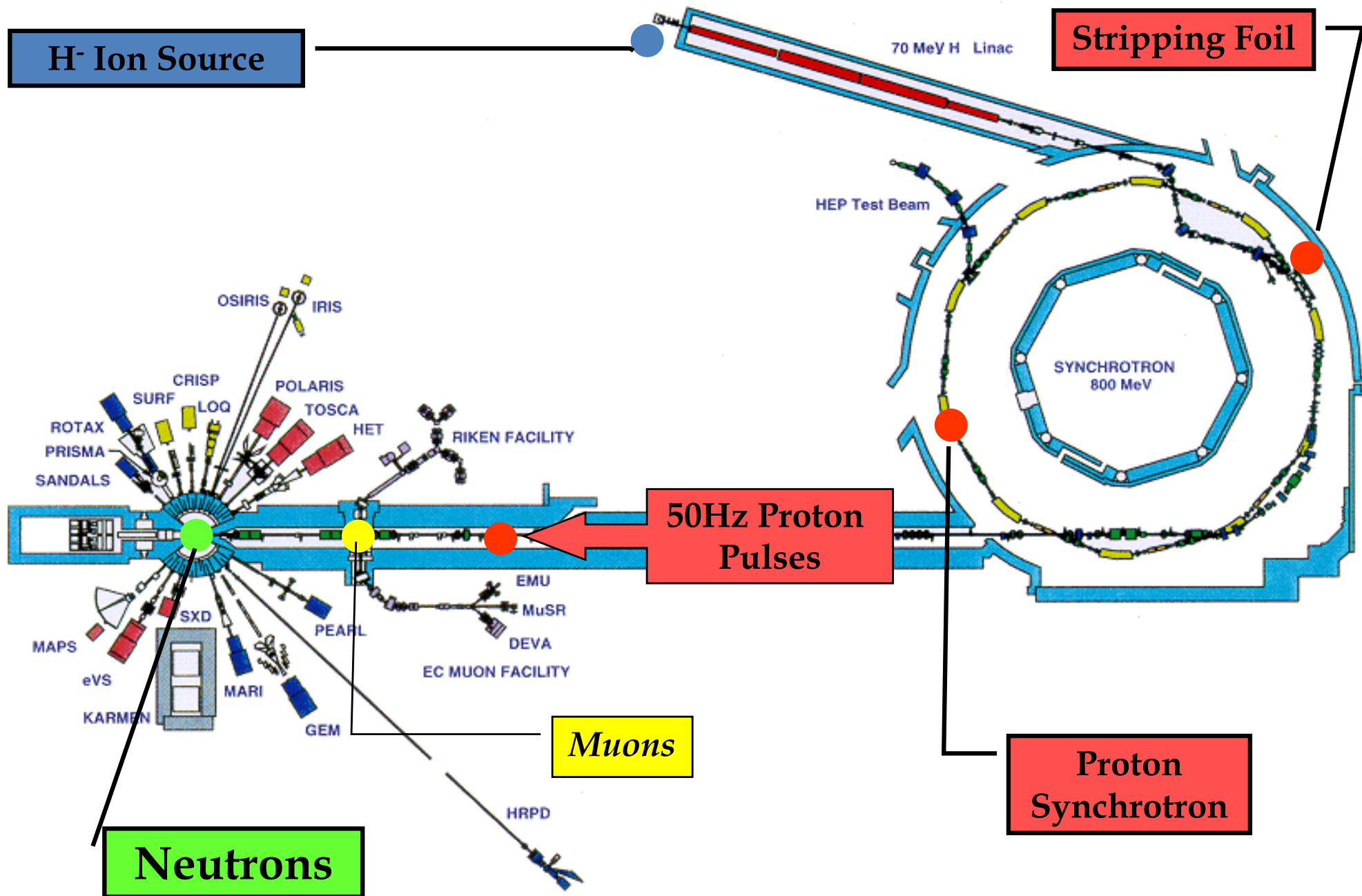


Spallation

spallation product



# The ISIS Spallation Neutron Source

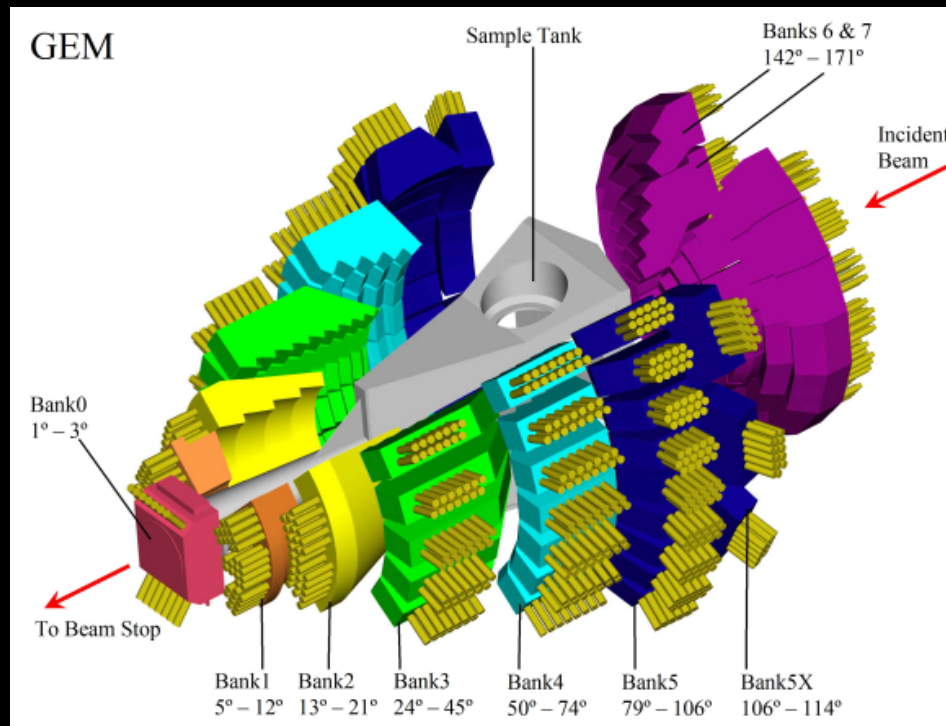


# GEM (General Materials Diffractometer)

funded by EPSRC + Riken  
(total cost ~ £4-5 million)



GEM diffractometer (*Hannon, Nucl Inst Meth A 2005*)



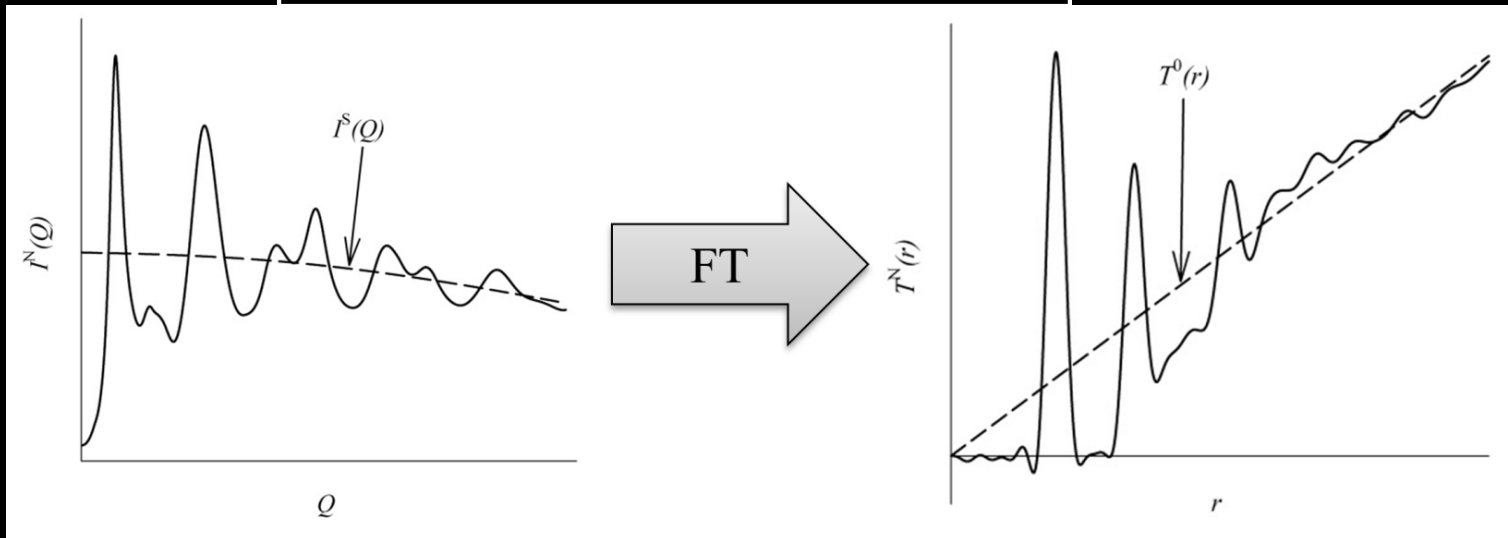
7290 detectors  
construction from 1999 to 2004

- State of the art neutron diffractometer for glass and powder diffraction at the ISIS Facility

# Glass Diffraction

$$T(r) = T^0(r) + \frac{2}{\pi} \int_0^{\infty} Q i(Q) M(Q) \sin(rQ) dQ$$

$$Q = \frac{4\pi}{\lambda} \sin \theta$$



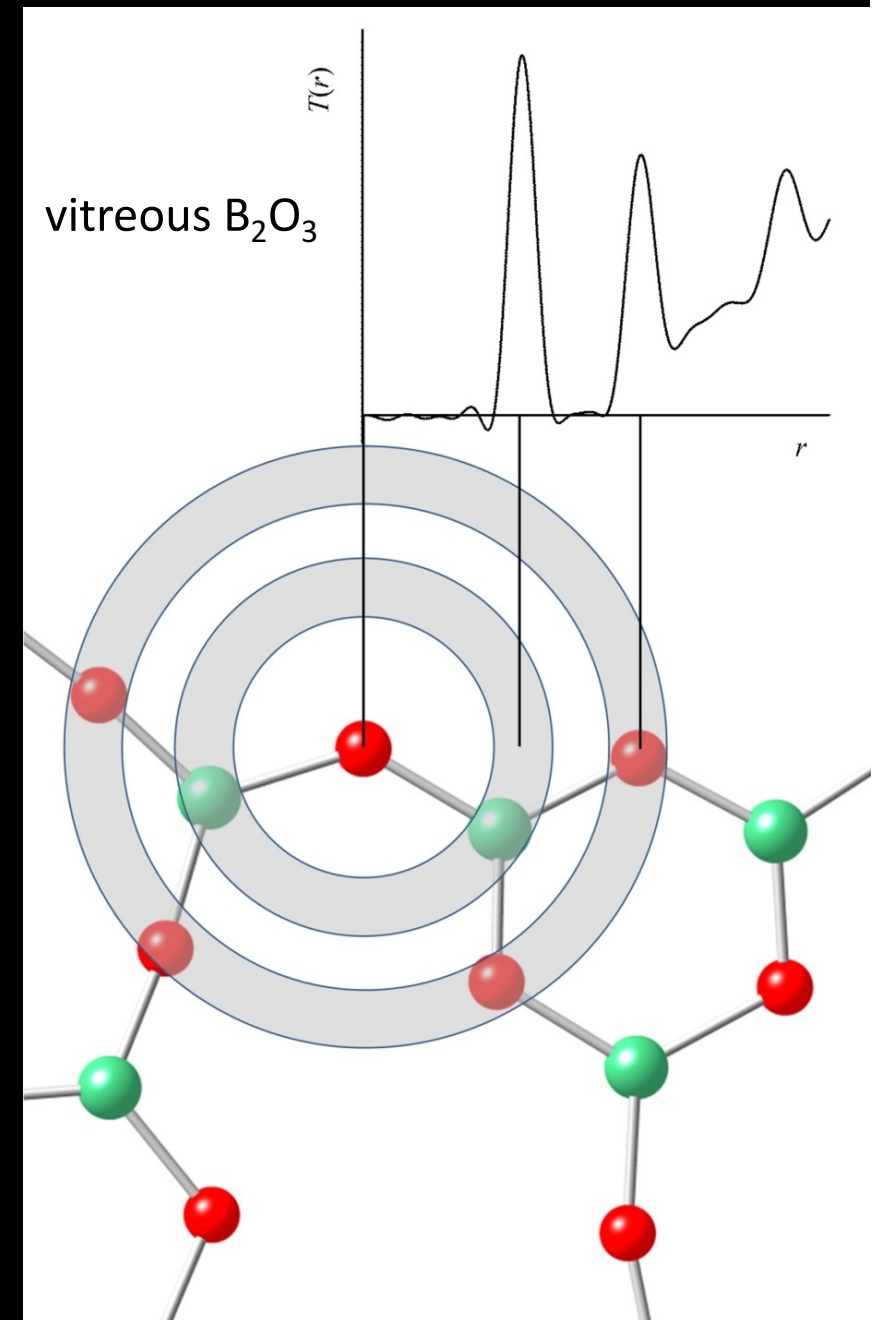
Diffraction pattern  $I(Q)$

Total correlation function  $T(r)$

- Glass diffraction pattern,  $I(Q)$ , consists of broad peaks, similar to a damped sine wave
- Fourier transformation leads to a real-space correlation function
- Pulsed neutrons give high  $Q$ , leading to good real-space resolution

# What does the correlation function mean?

- A peak in  $T(r)$  indicates an interatomic distance that occurs frequently in the sample
- Peak area gives the coordination number  $n_{jk}$
- Peak position  $r_{jk}$  gives the bond length
- Peak width/shape gives distribution of distances



# Correlation Function Peak

- Peak area  $A_{jk}$  gives coordination number  $n_{jk}$
- Peak position  $r_{jk}$  gives bond length
- Peak width  $\sigma$  arises from:
  - $r$ -space resolution ( $Q_{\max}$ )
  - thermal motion
  - static disorder

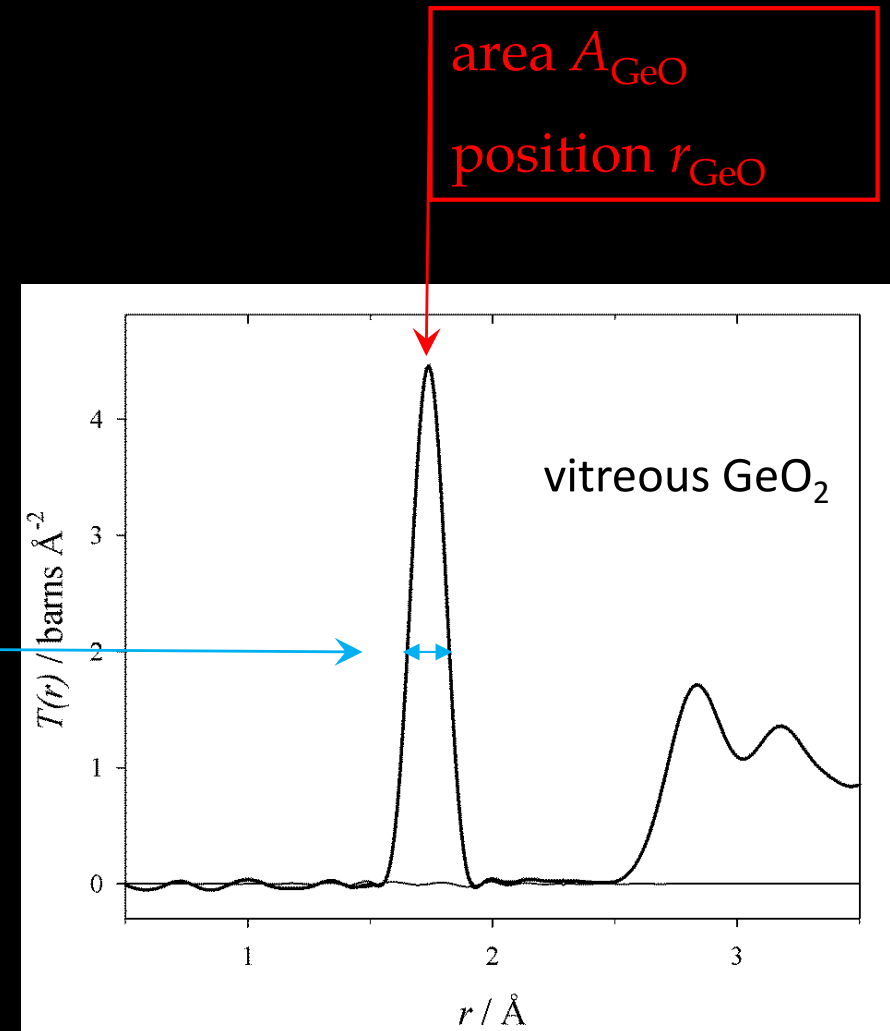
$$n_{jk} = \frac{r_{jk} A_{jk}}{(2 - \delta_{jk}) c_j \bar{b}_j \bar{b}_k}$$

width  $\sigma$

Accurate coordination numbers need:

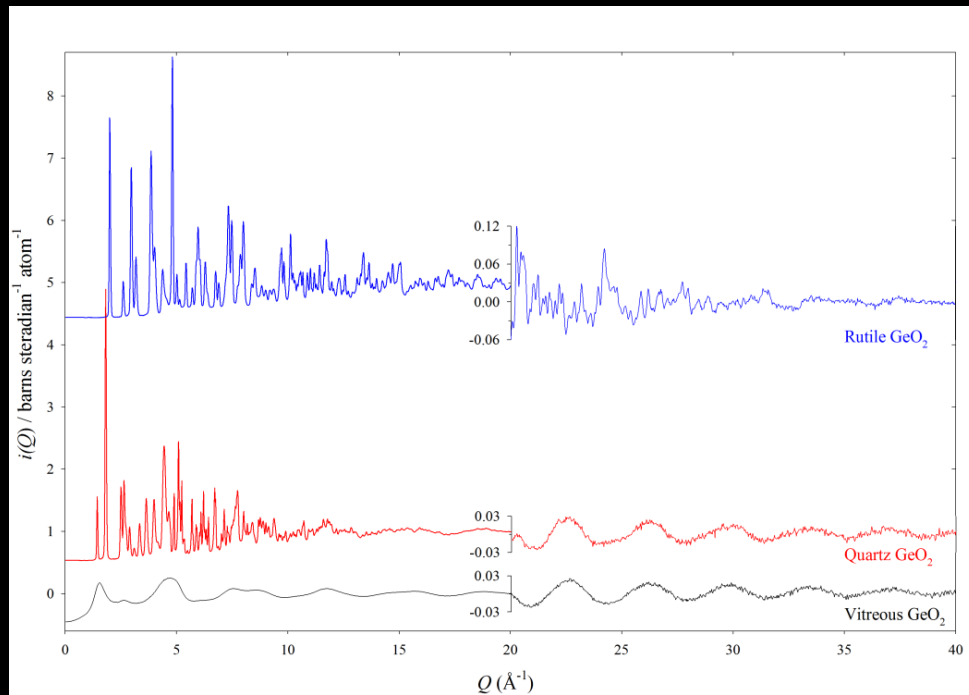
1. accurate sample composition
2. accurate density

(Alderman, *J Non-Cryst Solids* 2014)

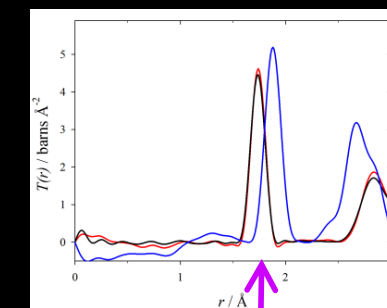
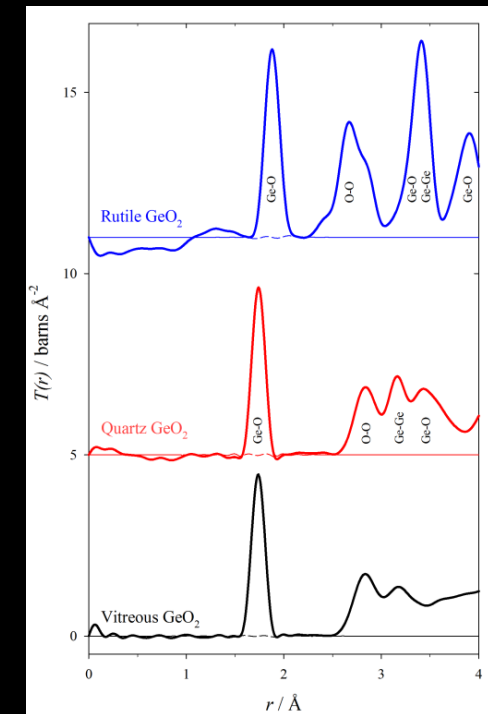


(Hannon, *J Phys Chem B* 2007)

# Pure GeO<sub>2</sub> Neutron Diffraction



(Hannon, *J Phys Chem B* 2007)



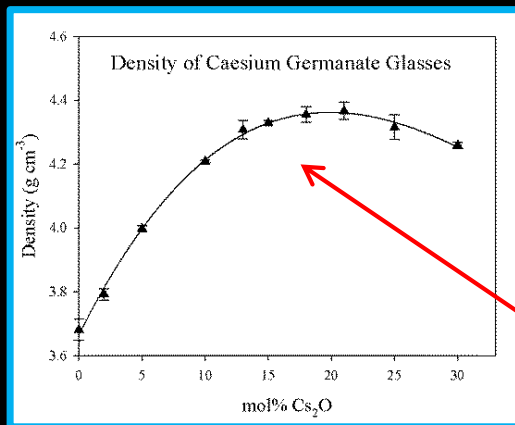
Ge-O  
peak

## Fits to Ge-O peak

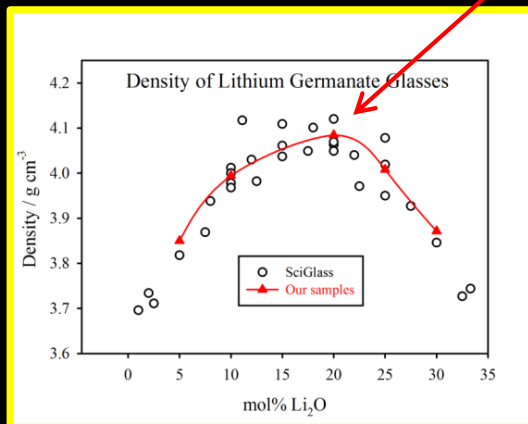
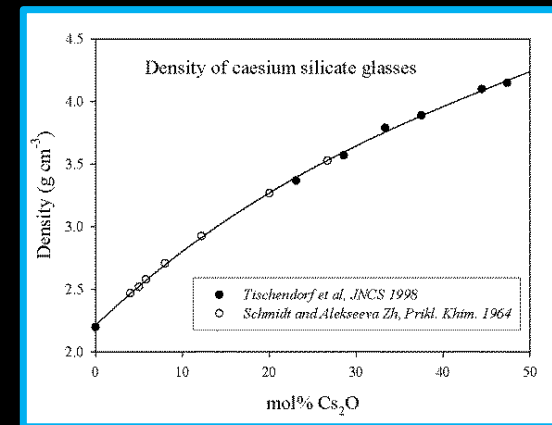
Rutile GeO <sub>2</sub>	$n_{\text{GeO}}=5.70$	Octahedral	$r_{\text{GeO}}=1.8805\text{Å}$
Quartz GeO <sub>2</sub>	$n_{\text{GeO}}=4.06$	Tetrahedral	$r_{\text{GeO}}=1.7402\text{Å}$
GeO <sub>2</sub> Glass	$n_{\text{GeO}}=4.03$	Tetrahedral	$r_{\text{GeO}}=1.7369\text{Å}$

# The Germanate Anomaly

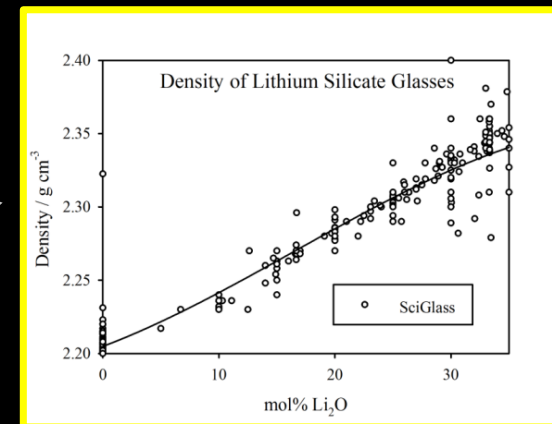
- Thermophysical properties of germanate glasses (e.g. density) show a maximum/minimum as modifier (e.g.  $\text{Cs}_2\text{O}$  or  $\text{Li}_2\text{O}$ ) is added – this is the *germanate anomaly*



Density maximum at  
~20 mol%  $\text{Cs}_2\text{O}$  or  $\text{Li}_2\text{O}$  for  
germanate glasses



No such density  
maximum for silicate  
glasses



# Change in Ge-O Coordination

- In 1960s the *germanate anomaly* was ascribed to a growth and decline in number of  $\text{GeO}_6$  octahedra in the glass  
(Ivanov & Evstropiev, Dok. Ak. Nauk SSSR 1962; Murthy & Ip, Nature, 1964)

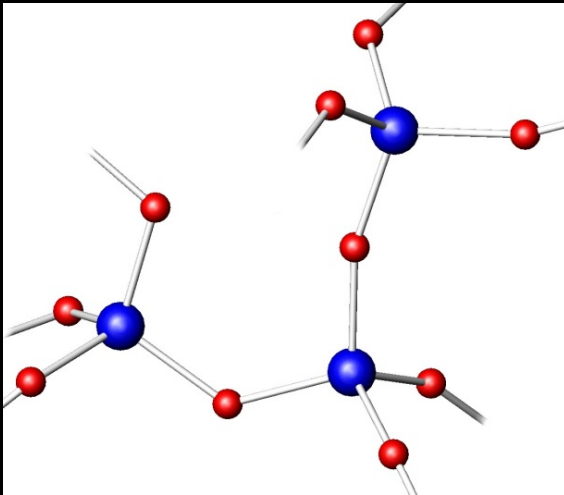
Crystalline forms of $\text{GeO}_2$			
Quartz $\text{GeO}_2$	All $\text{GeO}_4$ tetrahedra	$\rho = 4.28 \text{ g/cm}^3$	$r_{\text{GeO}} = 1.7402 \text{ \AA}$
Rutile $\text{GeO}_2$	All $\text{GeO}_6$ octahedra	$\rho = 6.25 \text{ g/cm}^3$	$r_{\text{GeO}} = 1.8805 \text{ \AA}$

- No direct evidence for Ge-O coordination change in glasses was available in the 1960s.

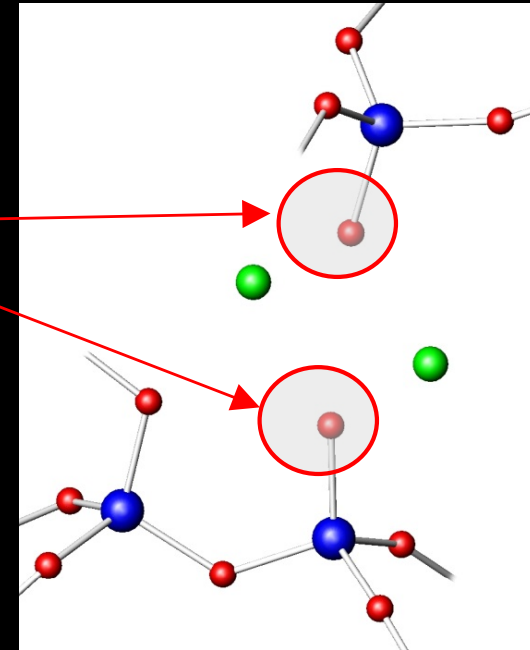


# The creation of $\text{GeO}_6$ Octahedra

Pure  $\text{GeO}_2$  glass



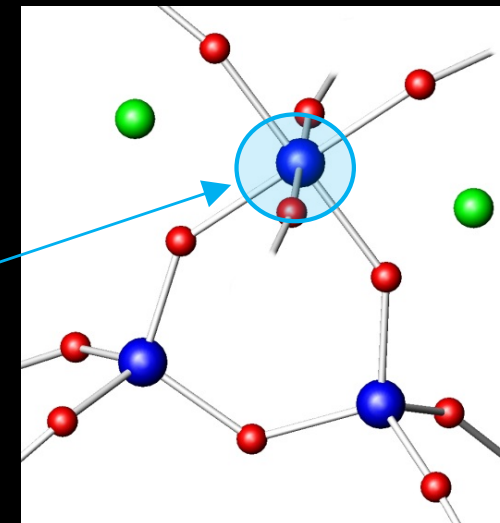
EITHER create  
two non-bridging  
oxygens



add  $\text{Cs}_2\text{O}$



OR create one  
octahedral  
germanium

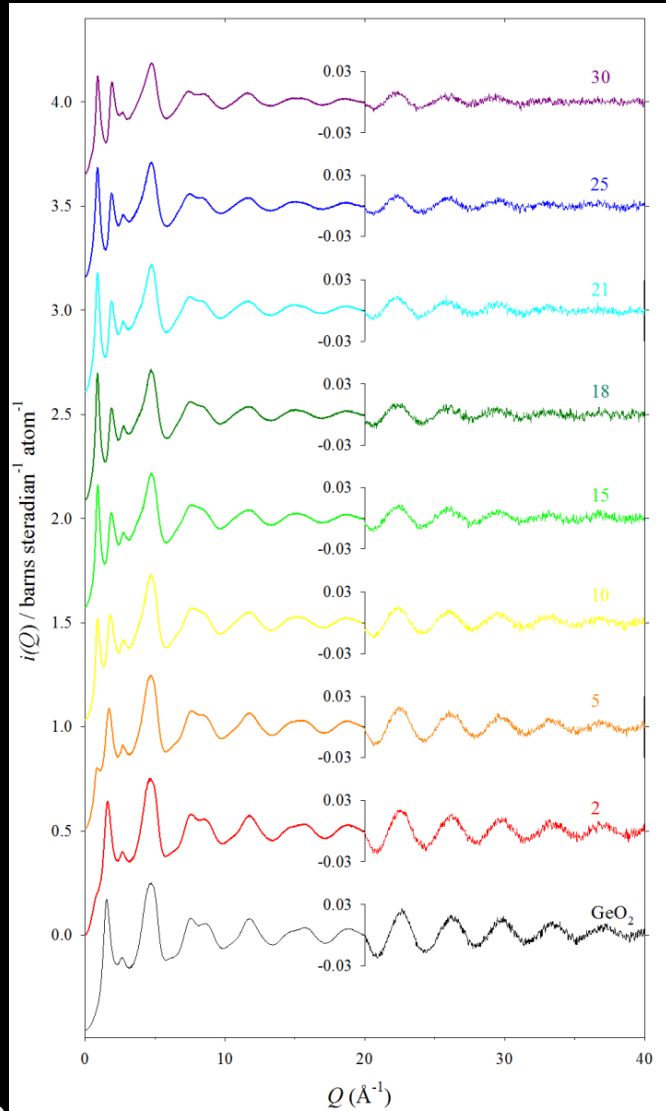


# Neutron Diffraction – Caesium Germanate Glasses

30 mol.%  
Cs<sub>2</sub>O

Diffraction patterns

increasing Cs<sub>2</sub>O content

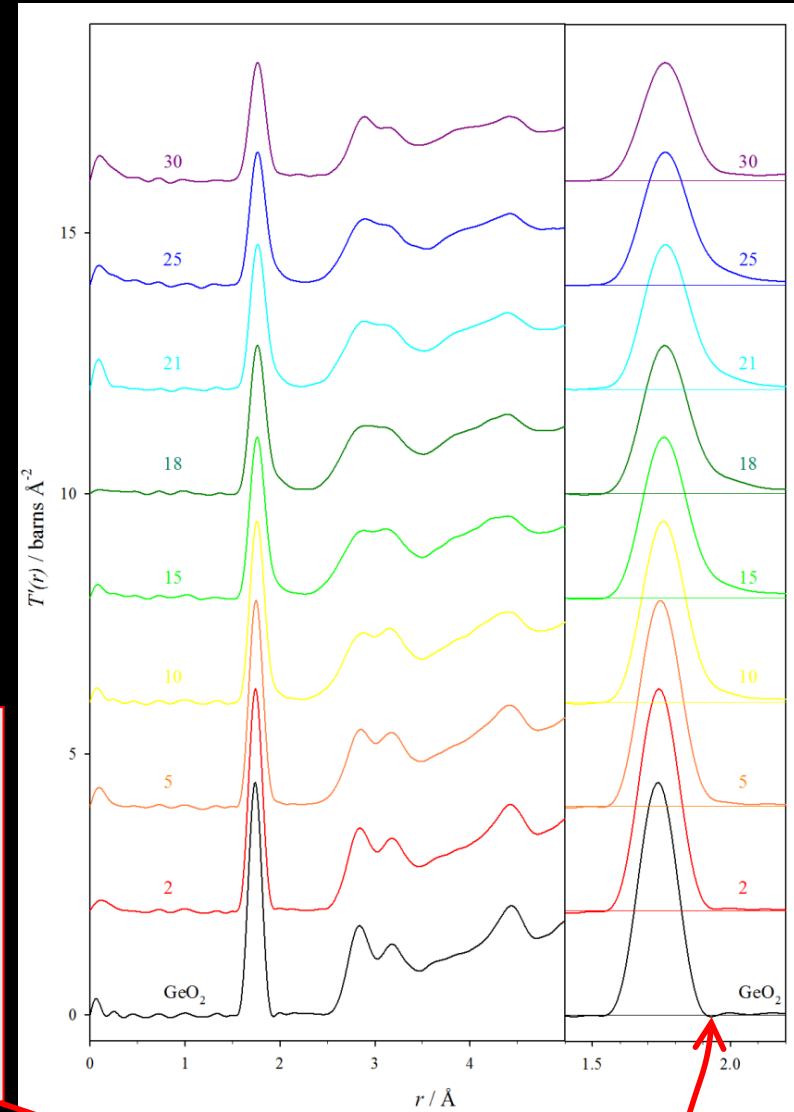


pure  
GeO<sub>2</sub>

Neutron  
diffraction on  
glasses with  
0, 2, 5, 10, 15,  
18, 21, 25 & 30  
mol.% Cs<sub>2</sub>O

Ge-O peak  
moves to longer  
distance and a  
high- $r$  shoulder  
develops

Correlation functions

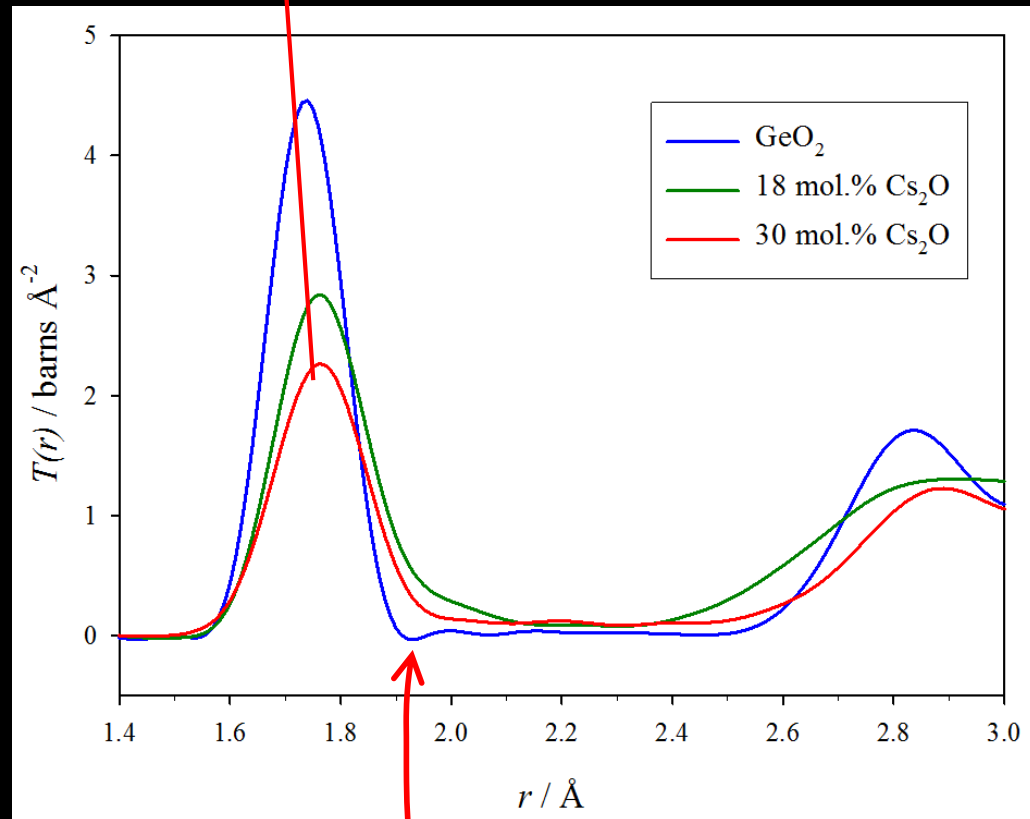


Cs<sub>2</sub>O-GeO<sub>2</sub> glasses

# Ge-O peak in correlation functions

Cs<sub>2</sub>O-GeO<sub>2</sub> glasses

Ge-O peak moves to longer distance

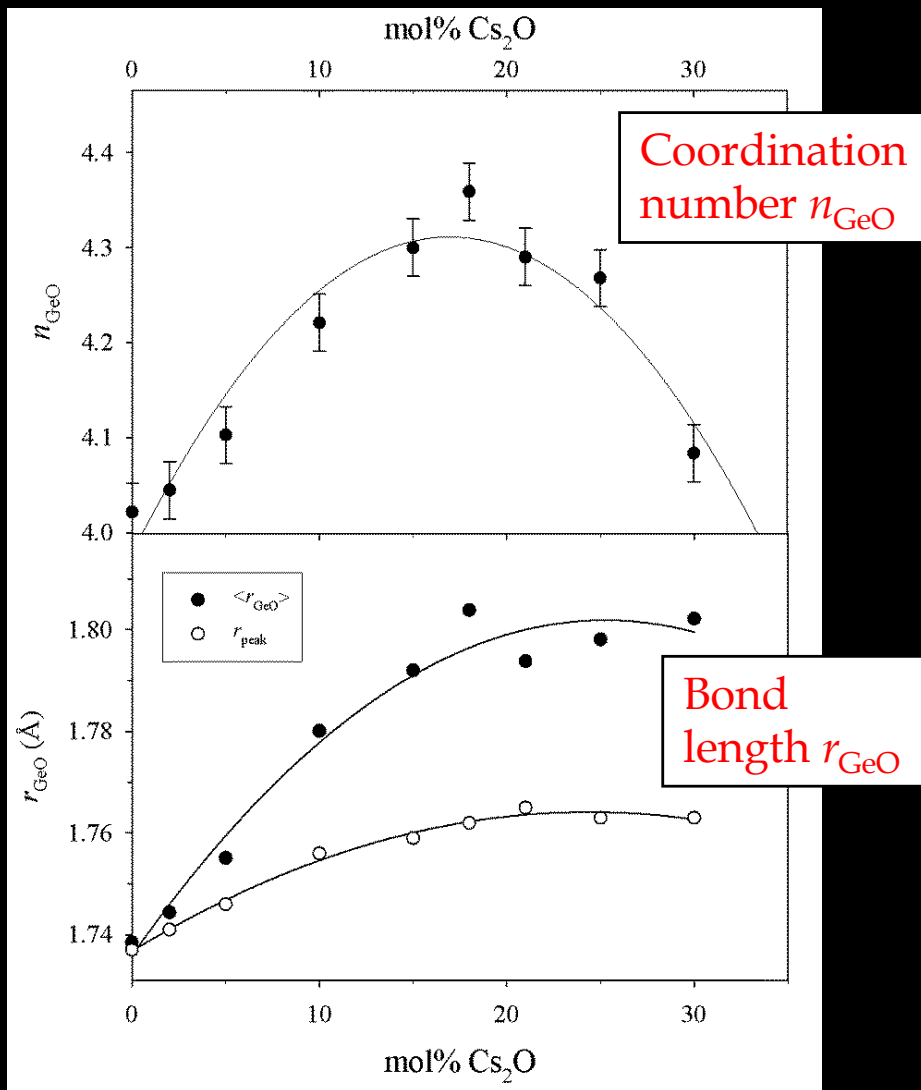


(Cs-O bond lengths  $\sim 3.2 \text{\AA}$ )

a high- $r$  shoulder develops

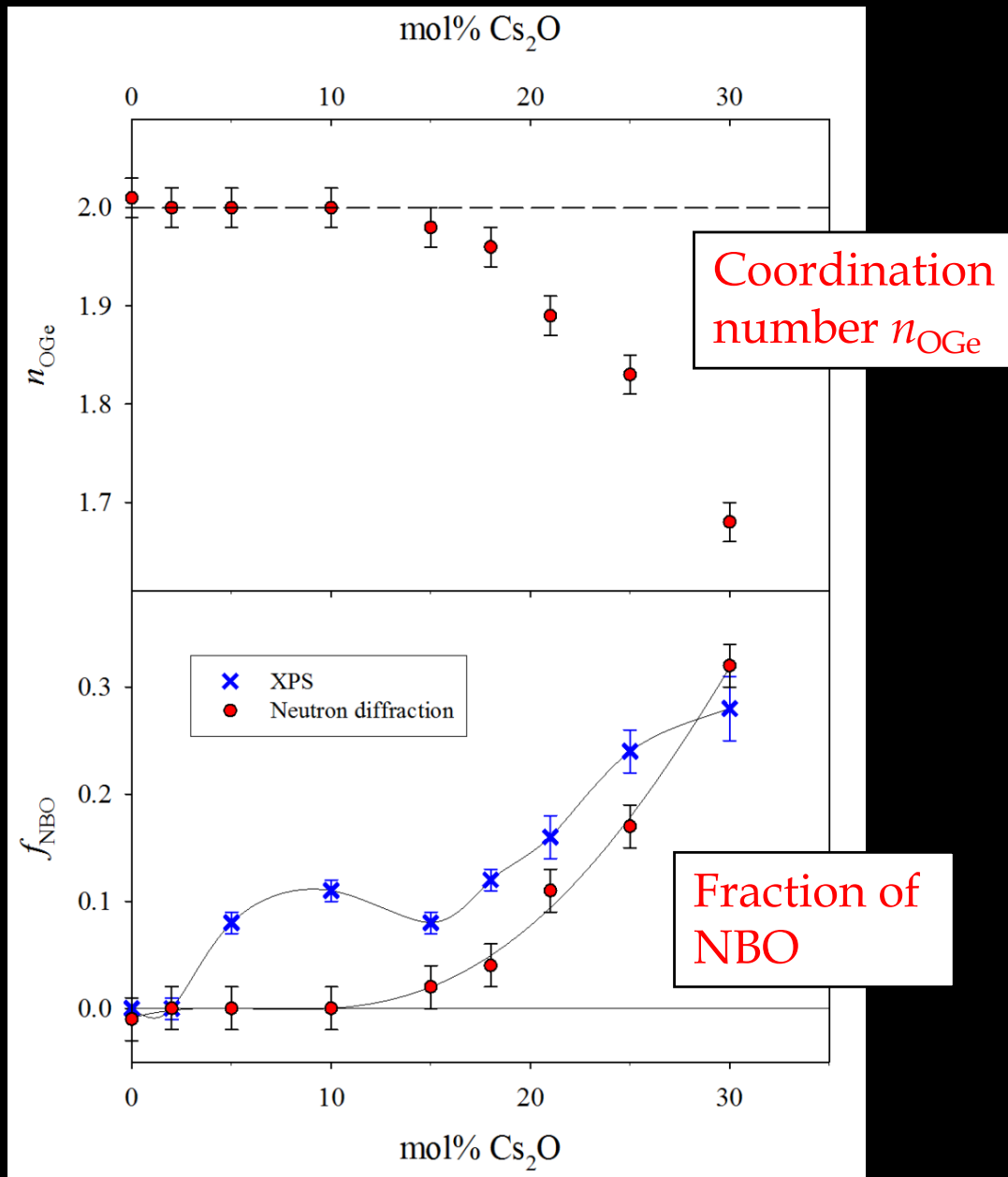
# Measured Ge-O Coordination

Cs<sub>2</sub>O-GeO<sub>2</sub> glasses



- Strong evidence for a growth and decline in Ge-O coordination number,  $n_{\text{GeO}}$

# Measured O-Ge Coordination



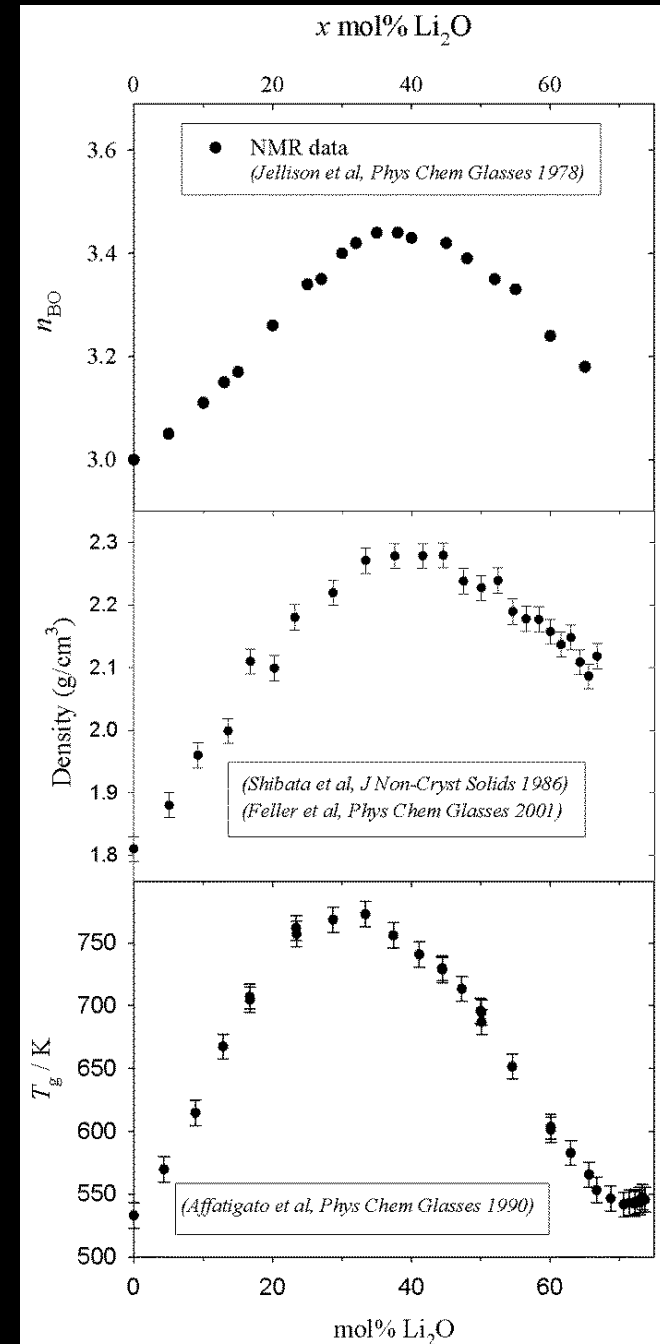
- In rutile GeO<sub>2</sub> and some alkali germanate crystals there are 3-coordinated oxygens, OGe<sub>3</sub>, associated with octahedral Ge
- But our results show  $n_{\text{OGe}}$  does not exceed two  
→ no evidence for 3-coordinated oxygen in these glasses

(NBO=Non-Bridging Oxygen)

Cs<sub>2</sub>O-GeO<sub>2</sub> glasses

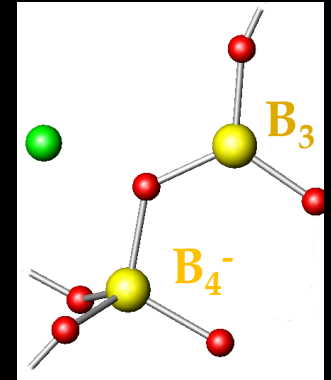
# Borate Glasses

- NMR on  $^{73}\text{Ge}$  is difficult and unhelpful
- But  $^{11}\text{B}$  NMR is very successful
- Much more is known about the *borate anomaly*
- Widest ranging NMR measurement is for Li borates
- Behaviour of B-O coordination number  $n_{\text{BO}}$  is similar to physical properties (density,  $T_g$ , ...)



# Charge Avoidance Model for Borates

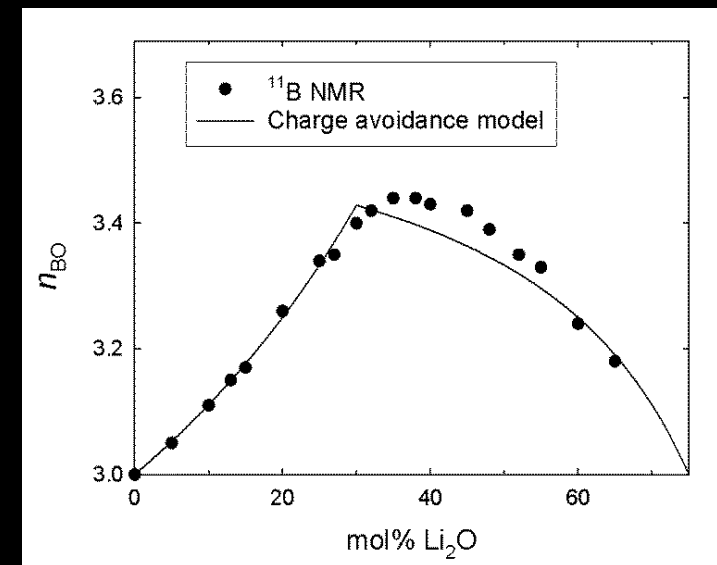
- Assume that centres of negative charge avoid each other...
  1.  $\text{BO}_4^-$  formation preferred over NBO formation
  2. No bridges between  $\text{BO}_4^-$
  3. No  $\text{BO}_4^-$  with NBOs
- No adjustable/fitted parameters
- Predicts...



- $n_{\text{BO}} = 3 + \frac{x}{1-x}$  for low  $x$
- alternating  $\text{BO}_3$  &  $\text{BO}_4^-$  at  $x=30$  mol%  $\text{Li}_2\text{O}$

(Wright et al, MRS Symp Proc 1997)

(NBO=Non-Bridging Oxygen)



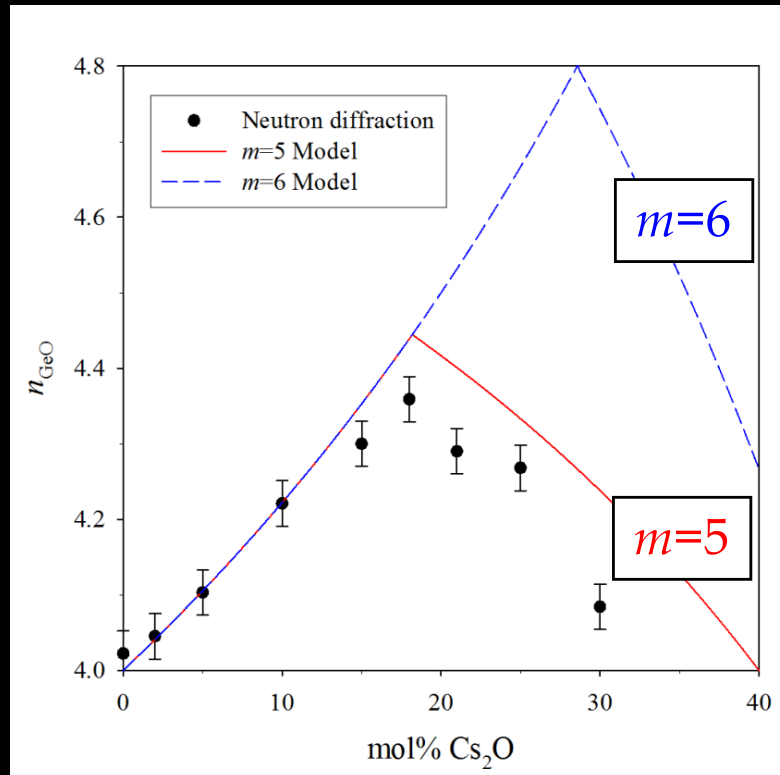
(Hannon & Holland, Phys Chem Glasses 2006)

# Charge Avoidance Model for Germanates

- $\text{GeO}_m$  units cannot be close to other centres of negative charge
- Two possible Ge-O coordinations, either 4 or  $m$  (either 5 or 6)
- No 3-coordination oxygens,  $\text{OGe}_3$
- Number of  $\text{GeO}_m$  units is maximised, subject to...
  - No bridges between two  $\text{GeO}_m$  units
  - $\text{GeO}_m$  units include no NBOs
  - $\text{GeO}_4$  tetrahedra with more than one NBO cannot exist if  $\text{GeO}_m$  units are present



# Model/Experiment Comparison

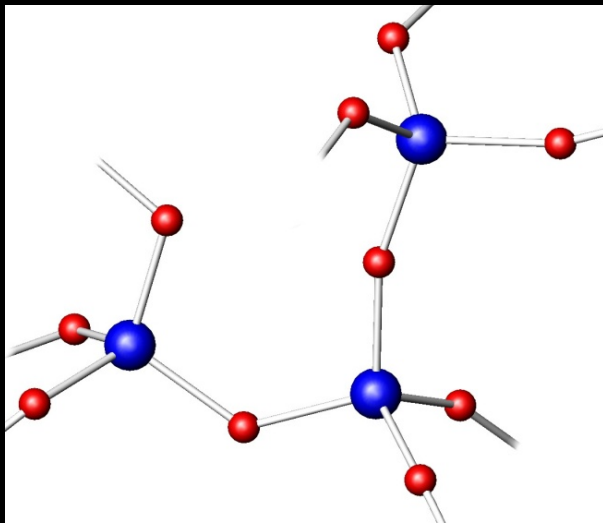


Cs<sub>2</sub>O-GeO<sub>2</sub> glasses

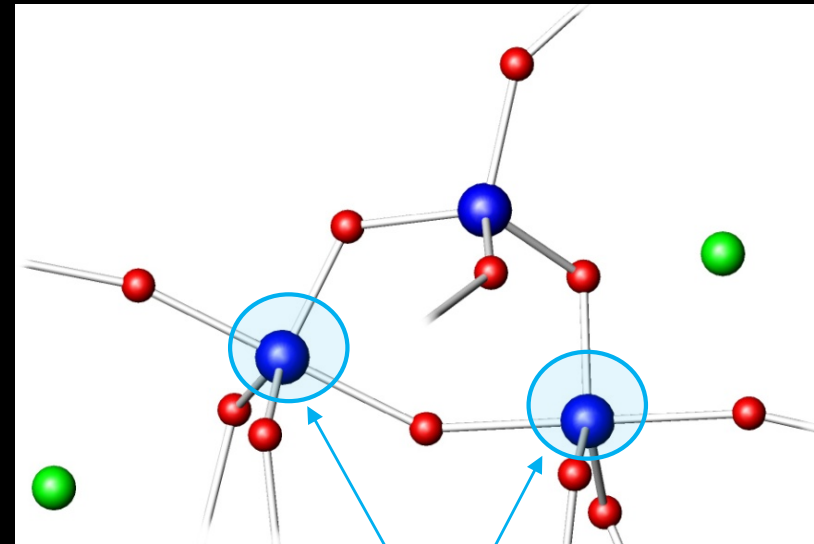
- The  $m=5$  model agrees much better with experiment
- This indicates the formation of GeO<sub>5</sub> units, not GeO<sub>6</sub> units
- 3-coordinated oxygen occurs more readily for GeO<sub>6</sub> → the lack of OGe<sub>3</sub> also indicates GeO<sub>5</sub> units

# GeO<sub>5</sub> Units

Pure GeO<sub>2</sub> glass



add Cs<sub>2</sub>O



create two  
GeO<sub>5</sub> units

**GeO<sub>5</sub> units occur in some germanate crystals:**

K<sub>2</sub>Ge<sub>8</sub>O<sub>17</sub>, Bi<sub>2</sub>GeO<sub>5</sub>, PbGe<sub>3</sub>O<sub>7</sub>, CaCuGe<sub>2</sub>O<sub>6</sub>, CuNd<sub>2</sub>Ge<sub>2</sub>O<sub>8</sub>,  
BaGe<sub>2</sub>O<sub>5</sub>-II (high pressure phase), La<sub>3</sub>AlGe<sub>5</sub>O<sub>16</sub>,  
La<sub>3</sub>GaGe<sub>5</sub>O<sub>16</sub>, Ce<sub>3</sub>AlGe<sub>5</sub>O<sub>16</sub>, Y<sub>3</sub>GeO<sub>5</sub>((OH)<sub>0.5</sub>F<sub>0.5</sub>)<sub>3</sub>,  
YAlGeO<sub>5</sub>, Ba<sub>3</sub>Ge<sub>9</sub>O<sub>20</sub>(OH)<sub>2</sub>, Dy<sub>3</sub>GeO<sub>5</sub>(OH)<sub>3</sub>,  
Gd<sub>3</sub>GeO<sub>5</sub>(OH)<sub>3</sub>, Sm<sub>3</sub>GeO<sub>5</sub>(OH)<sub>3</sub>, La<sub>2</sub>Ge<sub>3</sub>O<sub>9</sub>, Ce<sub>2</sub>Ge<sub>3</sub>O<sub>9</sub>,  
ErAlGeO<sub>5</sub>.

**Glass studies in support of GeO<sub>5</sub> units:**

**MD:** (Karthikeyan & Almeida, *JNCS* 2001; Watanabe & Sakai, *Phys Chem Glasses* 2017)

**Neutron diffraction:** (Hoppe et al, *JNCS* 1999)

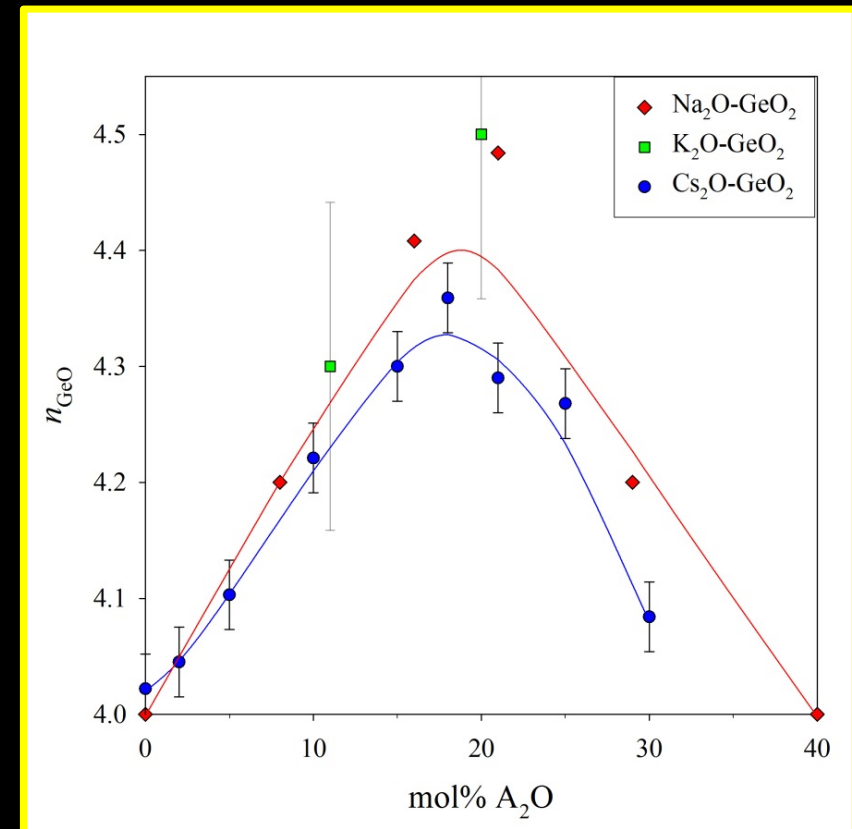
**XANES:** (Wang & Henderson, *Phys Chem Glasses* 2005)

**Raman:** (di Martino et al, *JNCS* 2001; Henderson & Amos, *JNCS* 2003)

**NMR:** (Du & Stebbins, *J Phys Chem B* 2006)

# Ge-O coordination numbers from neutron diffraction

- For alkali germanate glasses, neutron diffraction consistently shows  $n_{\text{GeO}}$  growth and a maximum



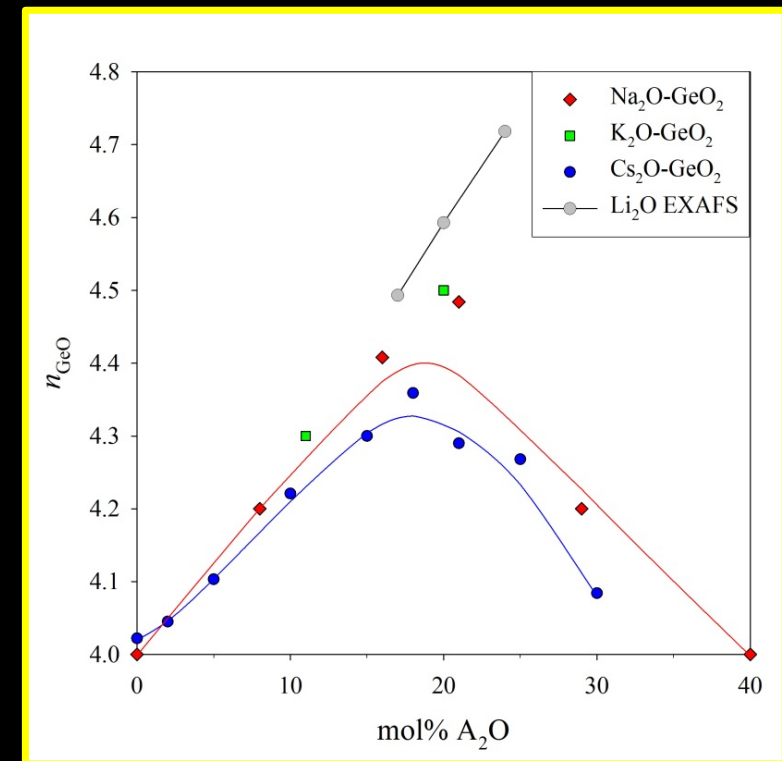
$\text{Na}_2\text{O}$ : (Ueno et al, *Physica B*, 1983)

$\text{K}_2\text{O}$ : (Hoppe et al, *J Non-Cryst Sol*, 1999)

$\text{Cs}_2\text{O}$ : (Hannon et al, *J Phys Chem B*, 2007)

# Lithium germanate EXAFS

- Recent EXAFS on Li germanates  
(*Arima et al, J Min Pet Sci 2005*)
- $n_{\text{GeO}}$  larger, no maximum  
- not consistent with ND results  
for K, Na, Cs germanates



Li<sub>2</sub>O: (*Arima et al, J Min Pet Sci, 2005*)

# Neutron diffraction with Lithium

Isotope	Scattering length $b$ / fm	Absorption cross-section $\sigma_a$ / barns
NatLi	-1.90	70.5
$^6\text{Li}$	2.00	940
$^7\text{Li}$	-2.22	0.0454
nullLi	0	495

- In crystalline  $\text{GeO}_2$ :  
 $r_{\text{GeO}} = 1.73 \text{ \AA}$  in tetrahedra,  $r_{\text{GeO}} = 1.88 \text{ \AA}$  in octahedra
- Typical  $r_{\text{LiO}} \approx 1.95 \text{ \AA}$   
 $\rightarrow$  big overlap with Ge-O bond lengths
- Neutron diffraction:  
 Use isotopic substitution, absorption is a problem
- Null lithium is made by mixing  $^6\text{Li}$  and  $^{\text{Nat}}\text{Li}$

# Isotopic substitution ND

- Neutron correlation function is sum of partial functions for all atom pairs (Ge-Ge, Ge-O, Ge-Li, Li-O, Li-Li, O-O):

$$T^N(r) = \sum_{l,l'} c_l \bar{b}_l \bar{b}_{l'} t_{ll'}(r)$$

- With  ${}^{\text{null}}\text{Li}$ , Li-X terms are absent:

$$T_{\text{null}}(r) = c_{\text{Ge}} \bar{b}_{\text{Ge}}^2 t_{\text{GeGe}}(r) + 2c_{\text{Ge}} \bar{b}_{\text{Ge}} \bar{b}_{\text{O}} t_{\text{GeO}}(r) + c_{\text{O}} \bar{b}_{\text{O}}^2 t_{\text{OO}}(r)$$

(only Ge-Ge, Ge-O and O-O terms are present)

- With  ${}^{7/6}\text{Li}$ , Li-X terms are present, and a difference isolates these terms:

$$T_{7\text{-Li}}(r) = T_{\text{null}}(r) + c_{\text{Li}} \bar{b}_{7\text{-Li}}^2 t_{\text{LiLi}}(r) + 2c_{\text{Li}} \bar{b}_{7\text{-Li}} \bar{b}_{\text{O}} t_{\text{LiO}}(r) + 2c_{\text{Li}} \bar{b}_{7\text{-Li}} \bar{b}_{\text{Ge}} t_{\text{LiGe}}(r)$$

$$\begin{aligned} \Delta_{7-0}(r) &= T_{7\text{-Li}}(r) - T_{\text{null}}(r) \\ &= c_{\text{Li}} \bar{b}_{7\text{-Li}}^2 t_{\text{LiLi}}(r) + 2c_{\text{Li}} \bar{b}_{7\text{-Li}} \bar{b}_{\text{O}} t_{\text{LiO}}(r) + 2c_{\text{Li}} \bar{b}_{7\text{-Li}} \bar{b}_{\text{Ge}} t_{\text{LiGe}}(r) \end{aligned}$$

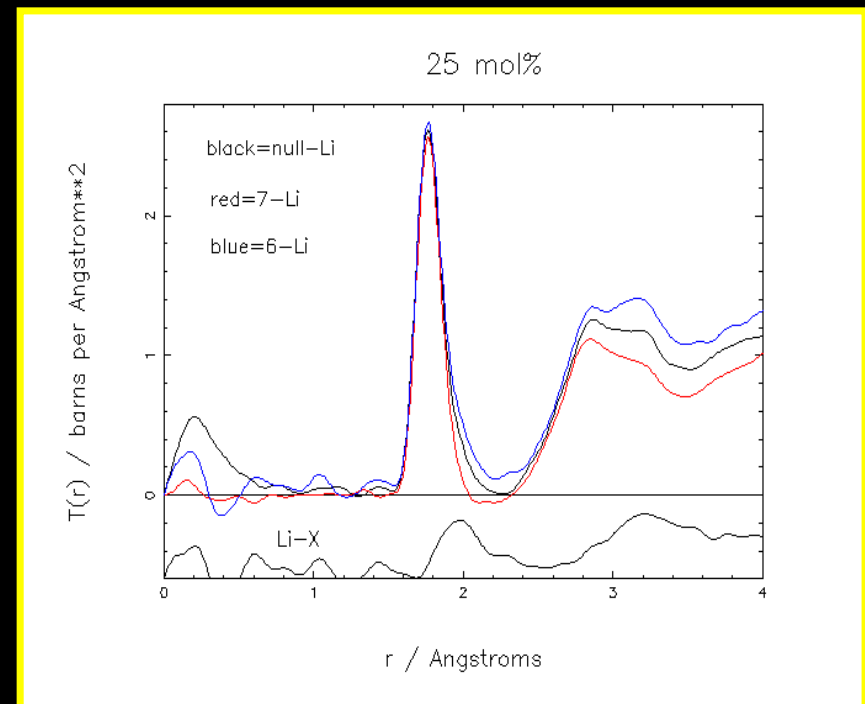
(Li-O, Li-Ge and Li-Li terms are isolated)

# Lithium germanates ND

- Li<sub>2</sub>O-GeO<sub>2</sub> binary glass samples:

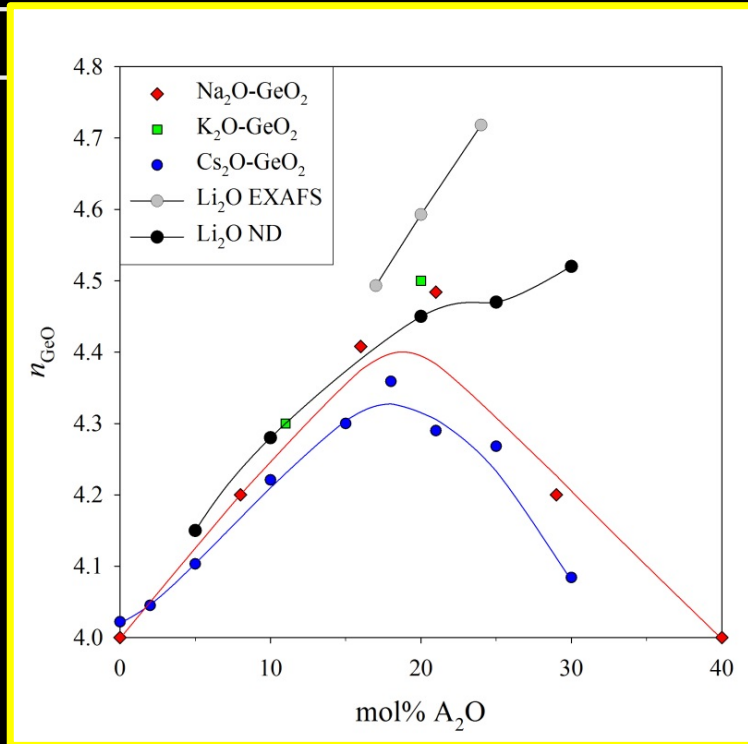
5 mol% Li <sub>2</sub> O	10 mol% Li <sub>2</sub> O	20 mol% Li <sub>2</sub> O	25 mol% Li <sub>2</sub> O	30 mol% Li <sub>2</sub> O
nullLi	nullLi	nullLi	nullLi	nullLi
<sup>7</sup> Li	<sup>7</sup> Li	<sup>7</sup> Li	<sup>7</sup> Li	<sup>7</sup> Li
	<sup>6</sup> Li	<sup>6</sup> Li	<sup>6</sup> Li	

- nullLi samples: Li-X correlations absent (but high absorption).  
Measures Ge-O distribution.
- <sup>7</sup>Li samples: Low absorption.  
Fixes normalisation of data.  
Measures Li-X correlations.
- <sup>6</sup>Li samples: Consistency check.  
Largest isotope difference.

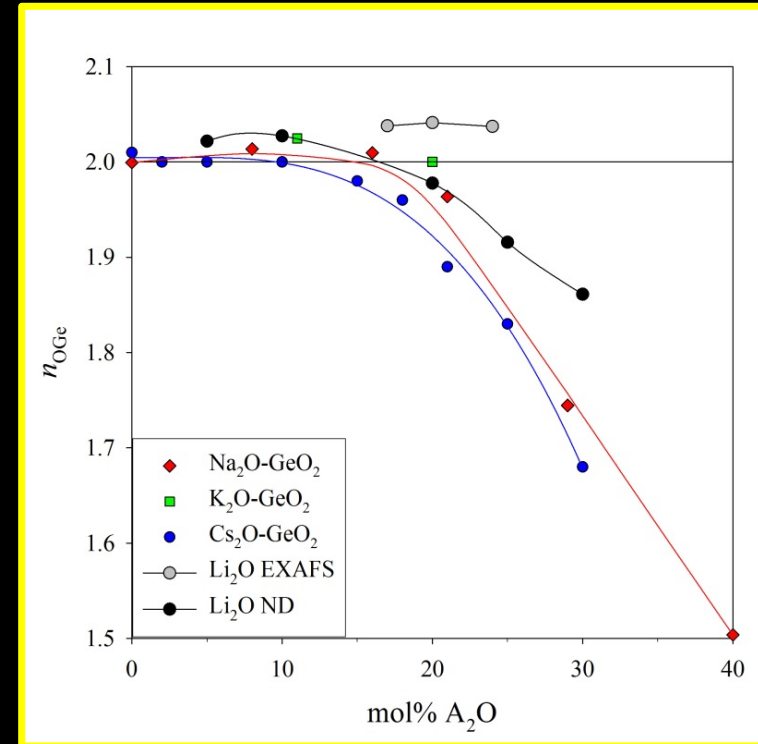


# Ge-O coordination numbers

Ge-O



O-Ge

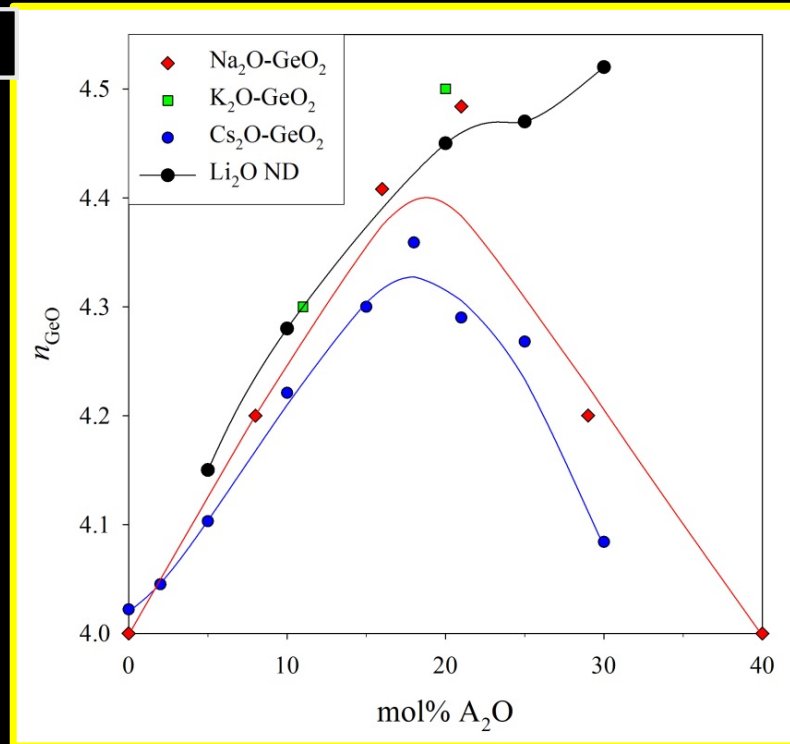


- Clearly EXAFS has over-estimated coordination numbers
- But, coordination number growth does fall
- And the fall is different for each alkali
- NBOs appear at  $\sim 20$  mol%  $\text{Li}_2\text{O}$

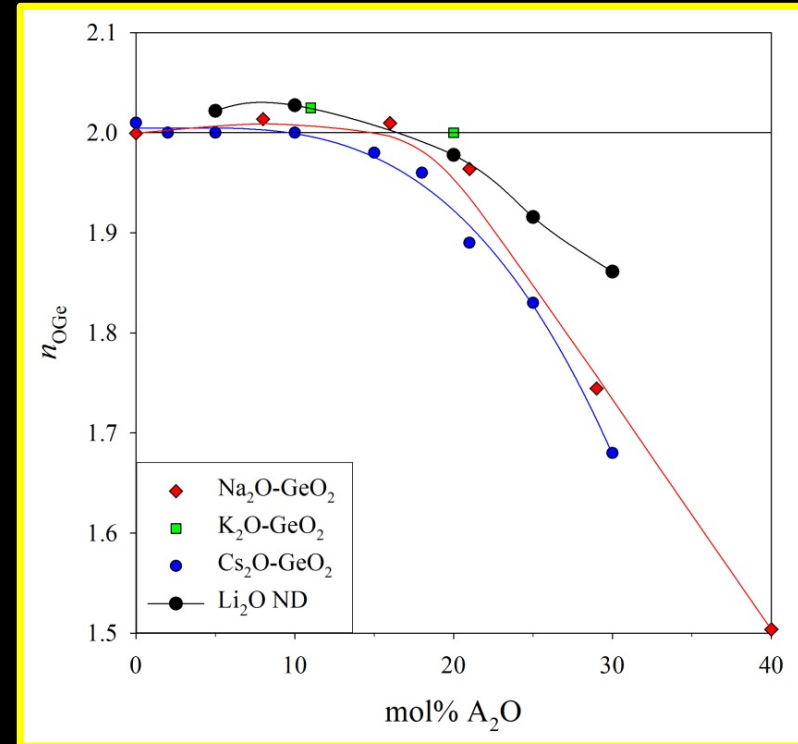


# Dependence on alkali

Ge-O



O-Ge



- Usually increasing alkali field strength  $z/r$  leads to increase in number of NBOs – we observe the opposite

*e.g. (Wu & Stebbins, J Non-Cryst Sol, 2009)*

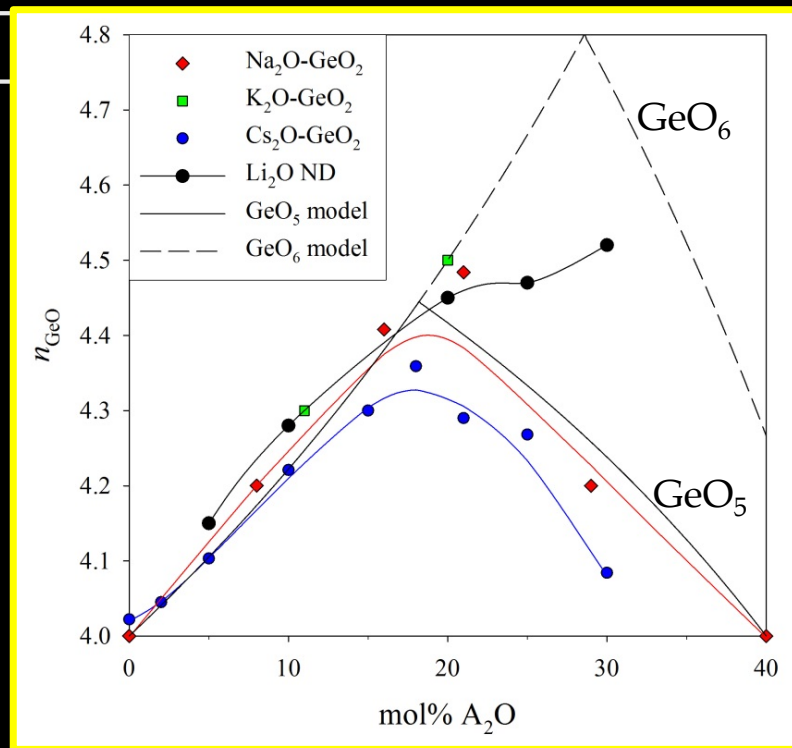
- On the other hand, a similar dependence on alkali is observed for  $N_4$  in borates

*(Michaelis et al, J Non-Cryst Sol, 2007)*

# Charge avoidance model

(Hannon et al, *J Non-Cryst Sol*, 2007)

Ge-O



(e.g. GeO<sub>6</sub>-GeO<sub>6</sub> bridges are forbidden)

- Charge avoidance model predicts  $n_{\text{GeO}}$  behaviour depends on higher Ge-O coordination number (5 or 6)
- Li germanate results are consistent with mostly GeO<sub>6</sub>  
(Cs and Na germanate results are consistent with mostly GeO<sub>5</sub>)
- Li<sup>+</sup> has larger field strength, and is better able to balance GeO<sub>6</sub><sup>2-</sup>

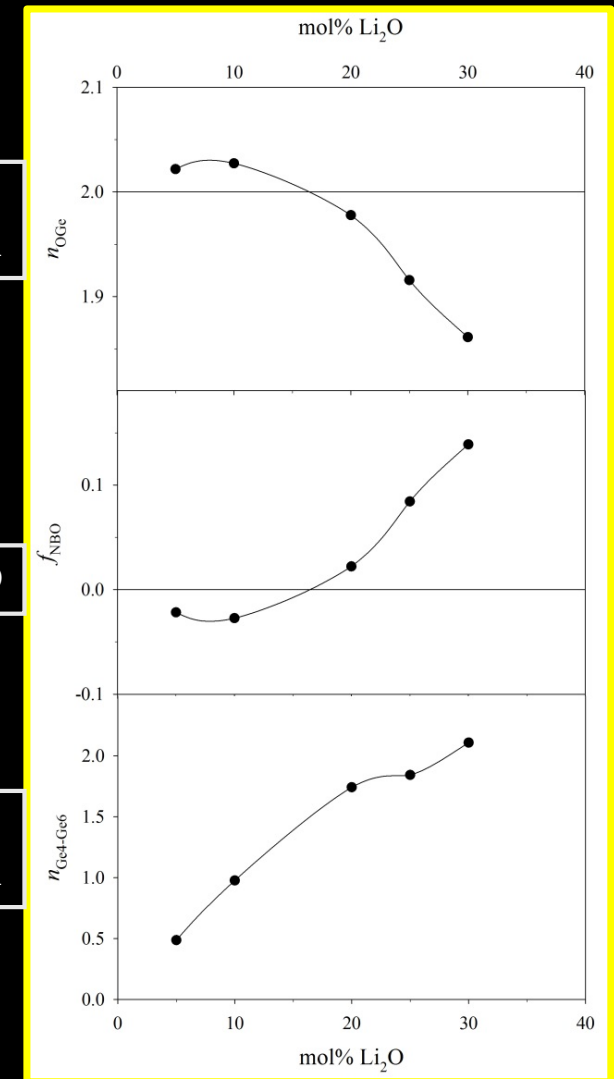
# Bridging and non-bridging oxygen

- There are few NBOs  
*e.g.* for 30 mol%  $\text{Li}_2\text{O}$ ,  
14% of oxygen are NBO
- There are many G4-G6 bridges  
*(i.e.* Ge4-O-Ge6)  
*e.g.* for 30 mol%  $\text{Li}_2\text{O}$ ,  
~half the bridges are G4-G6

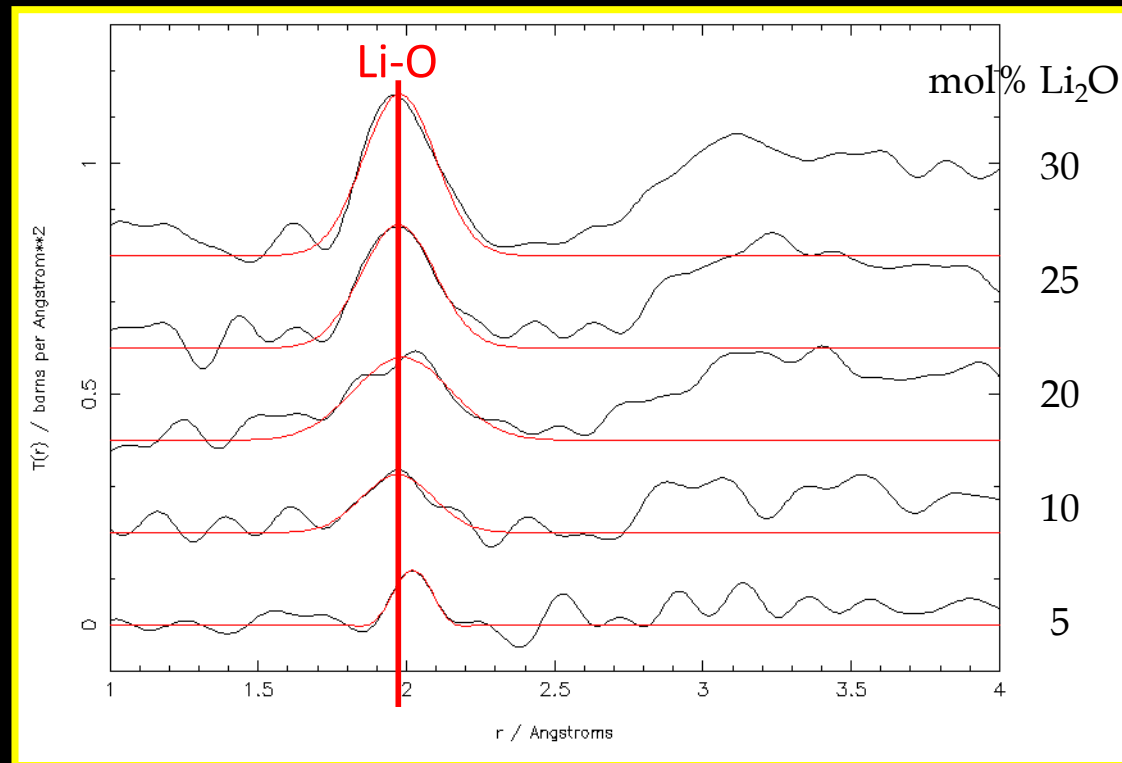
O-Ge  
coord num

frac NBO

Ge4-Ge6  
coord num



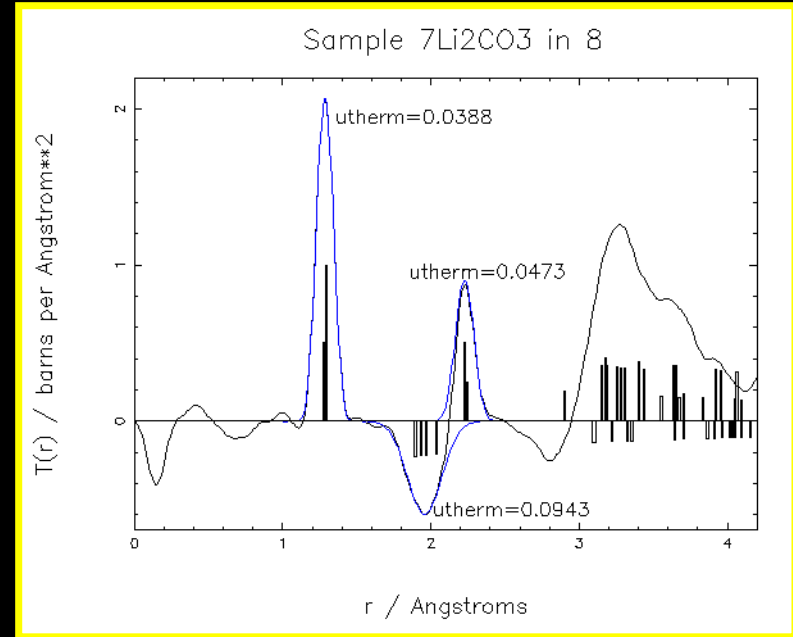
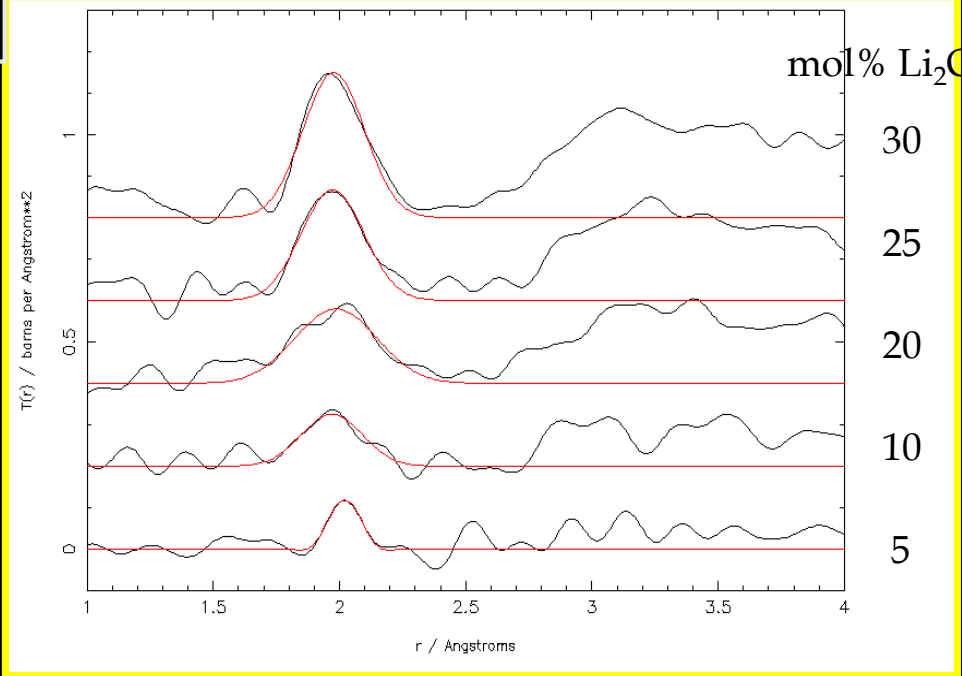
# Li-X correlations



- $^{\text{null}}\text{Li} - ^7\text{Li}$  difference reveals Li-O peak at  $\sim 1.98$  Å
- Li-Ge distances start at  $\sim 2.7$  Å
- Second Li-O distances at  $\sim 3.5$  Å

# Li-O thermal motion/static disorder

Li-X



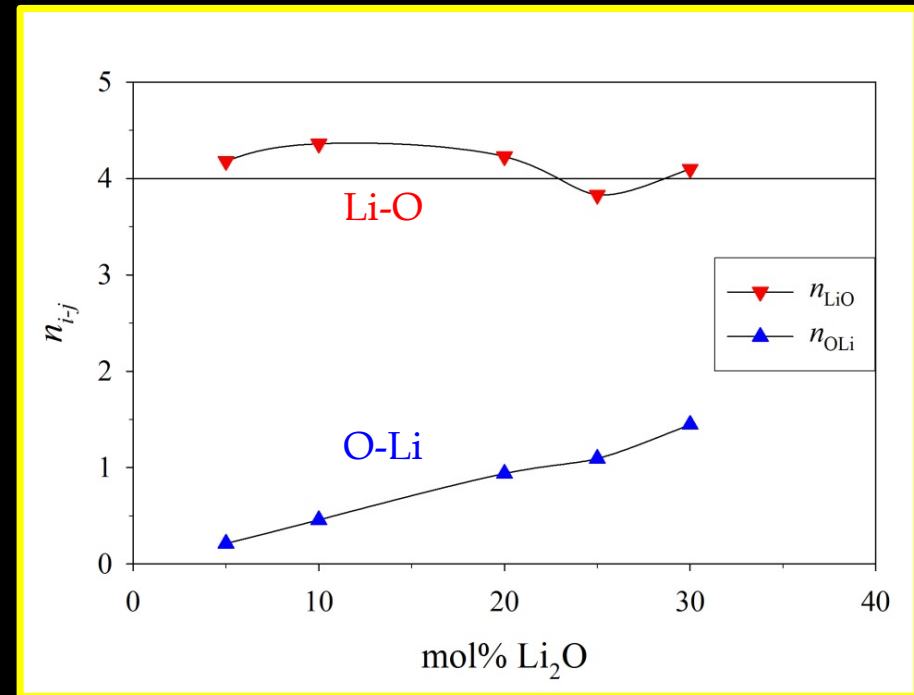
Li<sub>2</sub>CO<sub>3</sub>

- Li-O peak is unusually broad,  $\sigma_{\text{LiO}} \sim 0.11 \text{ \AA}$   
(compare  $\sigma_{\text{GeO}} = 0.04 \text{ \AA}$  in pure GeO<sub>2</sub>)
- $T(r)$  for crystalline Li<sub>2</sub>CO<sub>3</sub> shows thermal broadening of Li-O peak is  $\sigma_{\text{LiO}} = 0.094 \text{ \AA}$
- → Li is light and has large thermal motion
- Li-O peak is broad but distribution of distances is actually narrow

# Li-O coordination numbers

- Li-O coordination number  $\sim 4$
- O-Li coordination number grows to  $\sim 1.5$  for 30 mol%  $\text{Li}_2\text{O}$ ...

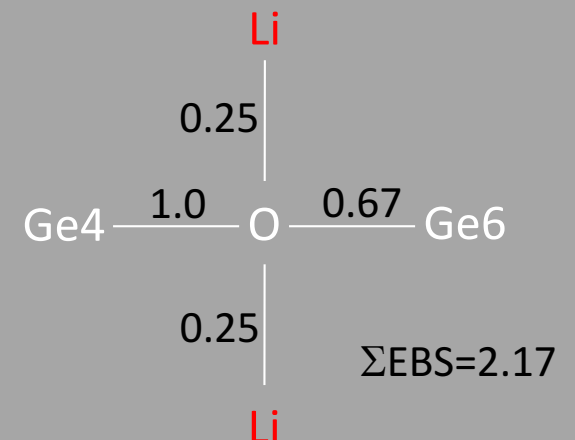
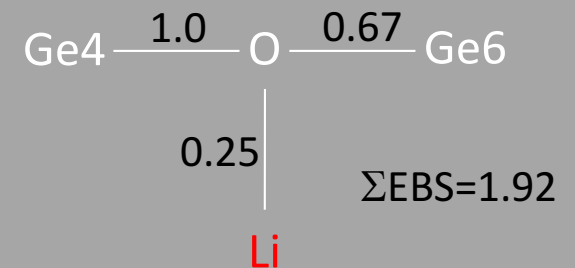
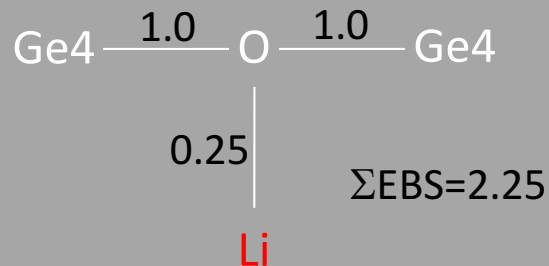
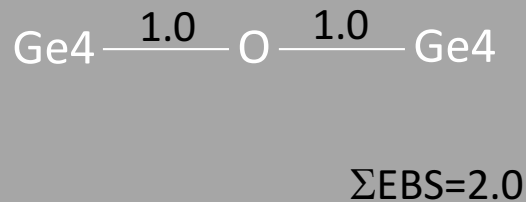
...then  $\sim$ half the BO are bonded to 2 Li



# Li-BO coordination

- Pauling's electrostatic bond strength (EBS) shows the likely oxygen environments...
- A Ge4-O-Ge4 bridge can accommodate 0 or 1 Li
- A Ge4-O-Ge6 bridge can accommodate 1 or 2 Li
- For 30 mol% Li<sub>2</sub>O half the bridges are Ge4-Ge6, and  $n_{\text{OLi}} \sim 1.5$

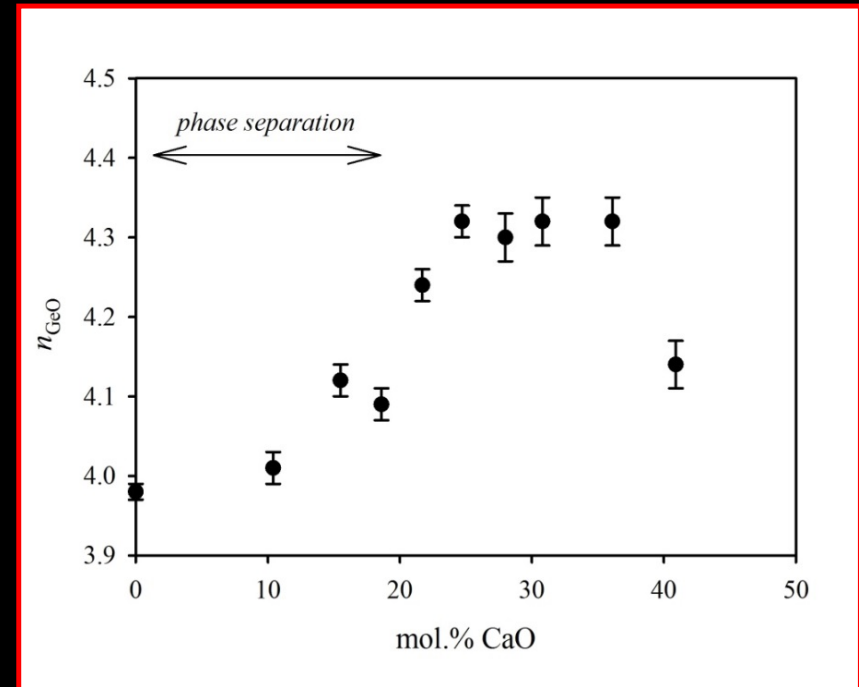
→ both types of bridge have their maximum number of Li



(Pauling, *J Am Chem Soc*, 1929)  
(Hannon, *J Non-Cryst Sol*, 2016)

# CaO-GeO<sub>2</sub> Neutron Diffraction

- Again Ge–O coordination numbers greater than 4 are observed
- What factors are involved in the *germanate anomaly*?

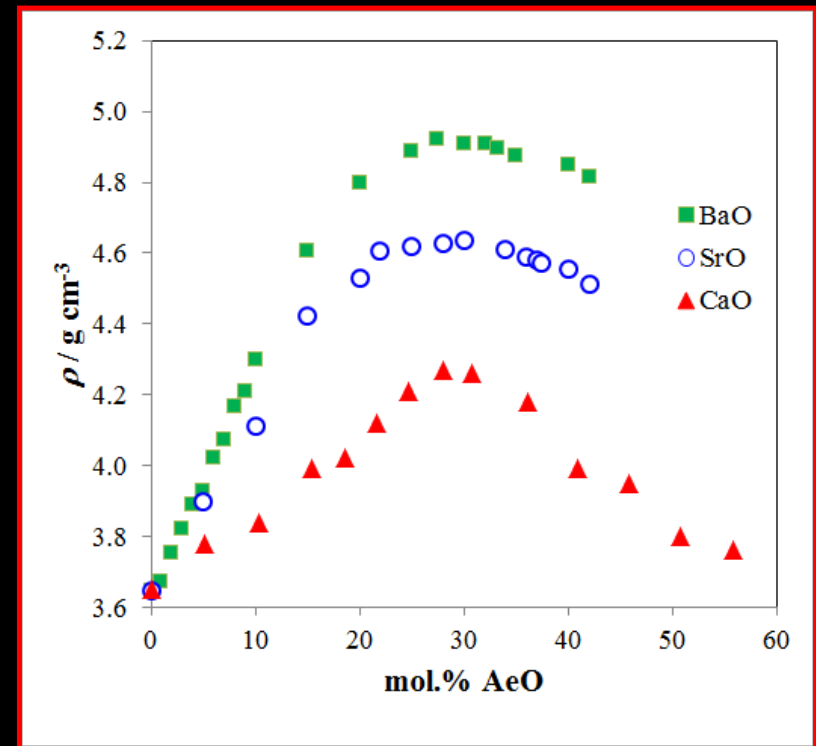


(Alderman, *J Phys Chem C* 2017)



# Density

- A maximum in the density is a key signature of the *germanate anomaly*
- Calcium germanate density maximum is at 29.4 mol% CaO
- Other alkaline earth germanates have similar density maxima, at similar positions



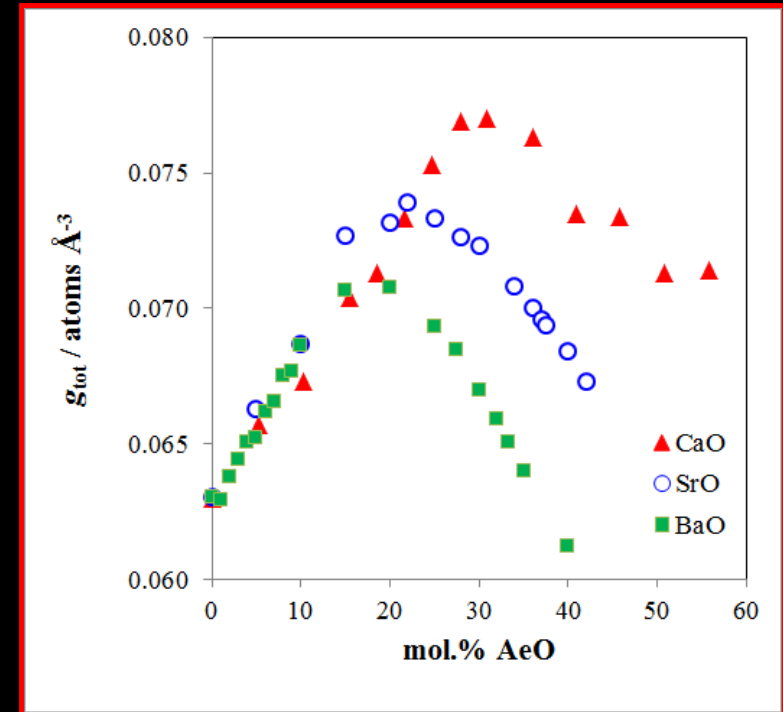
(Alderman, *J Phys Chem C* 2017)

# Atom number density

- Density (in  $\text{g cm}^{-3}$ ) is strongly influenced by atomic mass
- To investigate structure, remove the influence of mass  
(Hoppe, *J Non-Cryst Solids*, 1999)
- Instead of mass density, plot atom number density  $g_{\text{tot}}$   
*i.e.* number of atoms per unit volume

$$g_{\text{tot}} = \frac{\rho}{\text{amu} \sum_l c_l A_l}$$

Units for  $g_{\text{tot}}$ : atoms per cubic Ångstrom  
 $A_l$ =atomic number  $c_l$ =atomic fraction



(Alderman, *J Phys Chem C* 2017)

# Packing?

- All alkaline earth germanates follow the same  $g_{\text{tot}}$  line at low AeO content, then...
  - composition for deviation from the line depends on Ae ion size (Ca<Sr<Ba)
  - position of the maximum depends on Ae ion size

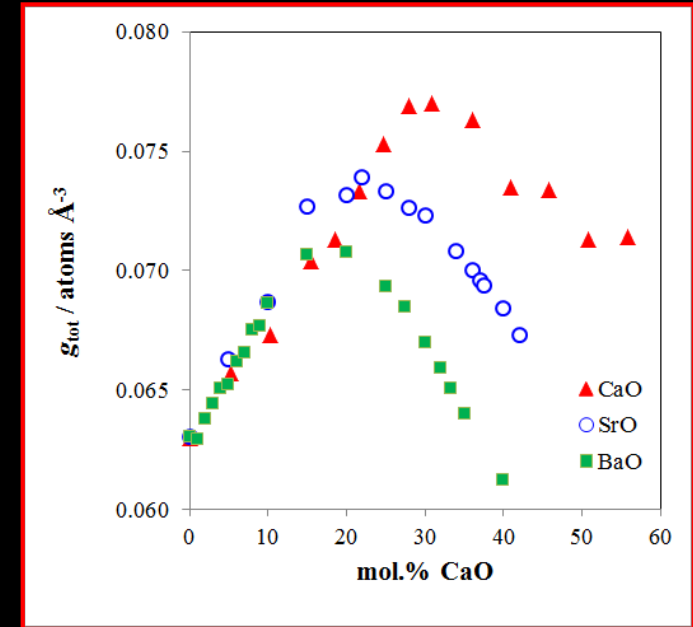
Ionic radius for 8-fold coordination:

$$R_{\text{Ca}} = 1.12\text{\AA}$$

$$R_{\text{Sr}} = 1.26\text{\AA}$$

$$R_{\text{Ba}} = 1.42\text{\AA}$$

- The dependence on Ae ion size suggests that packing is an important factor in the behaviour



(Alderman, *J Phys Chem C* 2017)

Ae=Alkaline earth

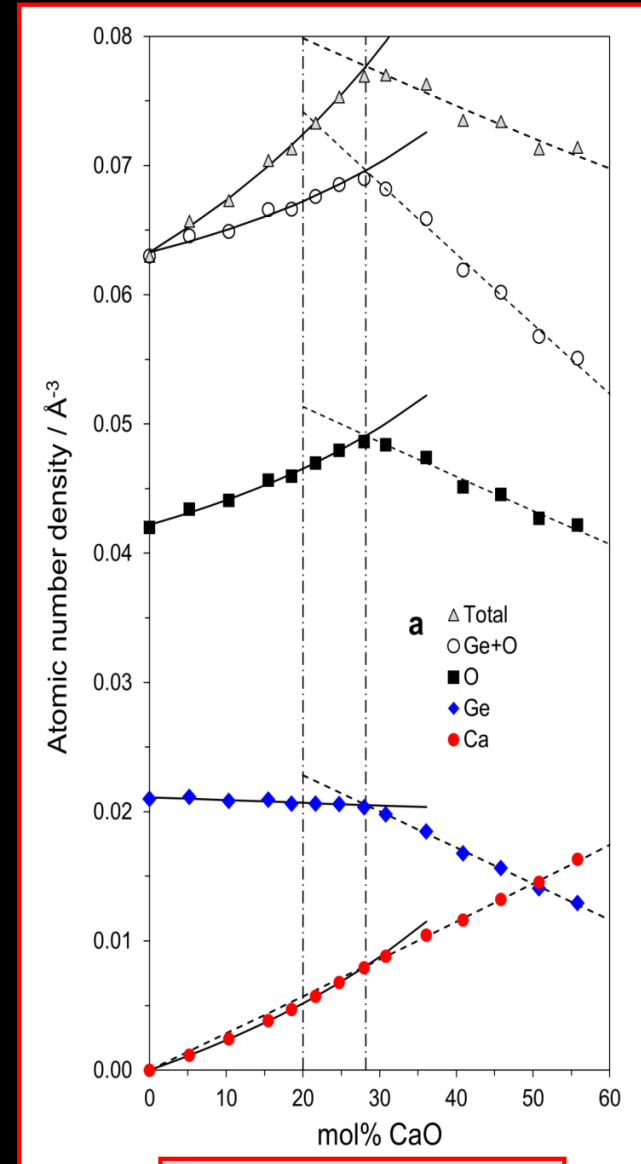
# Partial Atom Number Density

- We can also define a partial atomic number density for each element,  $g_l$

$$g_l = c_l g_{\text{tot}}$$

( $c_l$  = atomic fraction for the element  $l$ )

- $g_l$  is simply the number of atoms of element  $l$  per unit volume
- From one density measurement (plus known composition) we can determine three partial number densities!



Calcium germanates

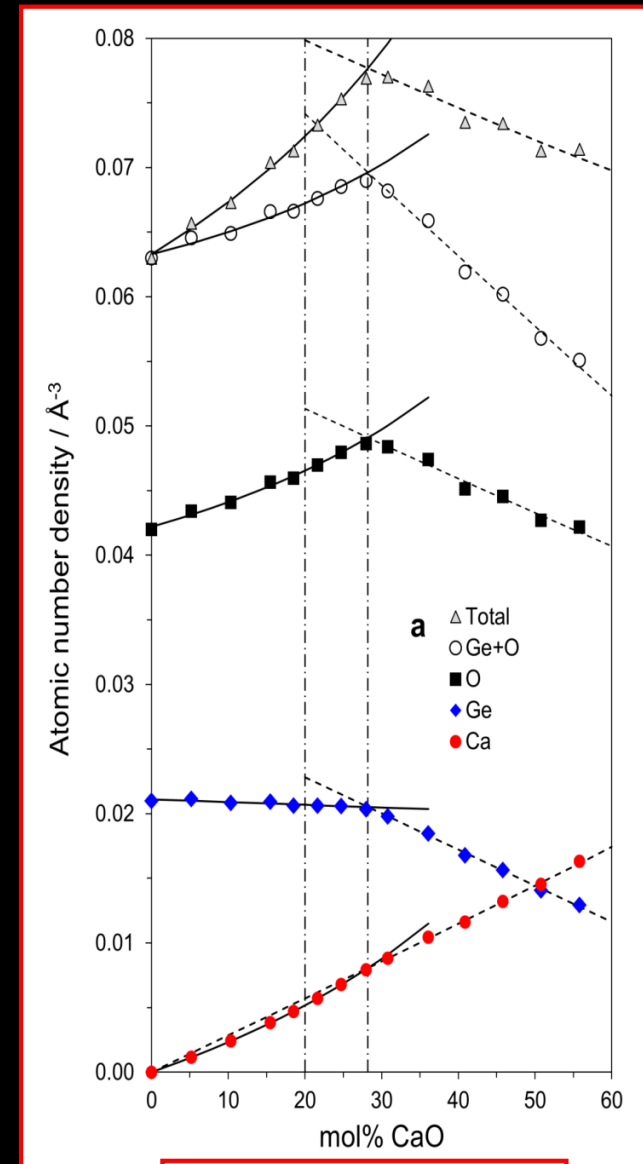
# Packing in Ca Germanates

- Ca number density is ~linear  
– the behaviour of ions going into holes in an inert matrix
- Ge number density has two linear regions:

Low CaO region –  $g_{\text{Ge}}$  is almost constant, the packing of the germanate network is unchanging

High CaO region –  $g_{\text{Ge}}$  declines more rapidly, the insertion of more  $\text{Ca}^{2+}$  is forcing apart the germanate network

Intersection is at 28.2 mol% CaO – the position of the number density maximum



Calcium germanates

# Sr and Ba Germanates

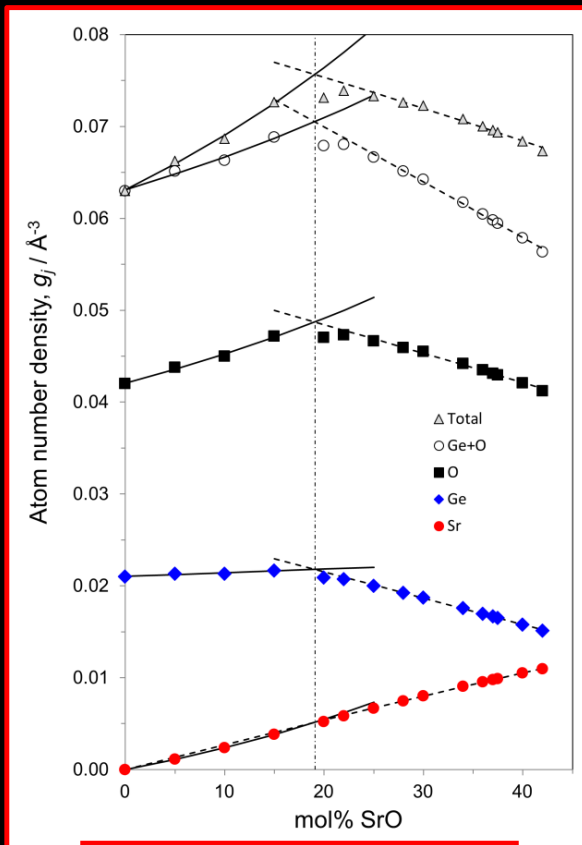
- Other alkaline earth germanates show the same partial number density behaviour as Ca germanates

- Ge number density change is at:

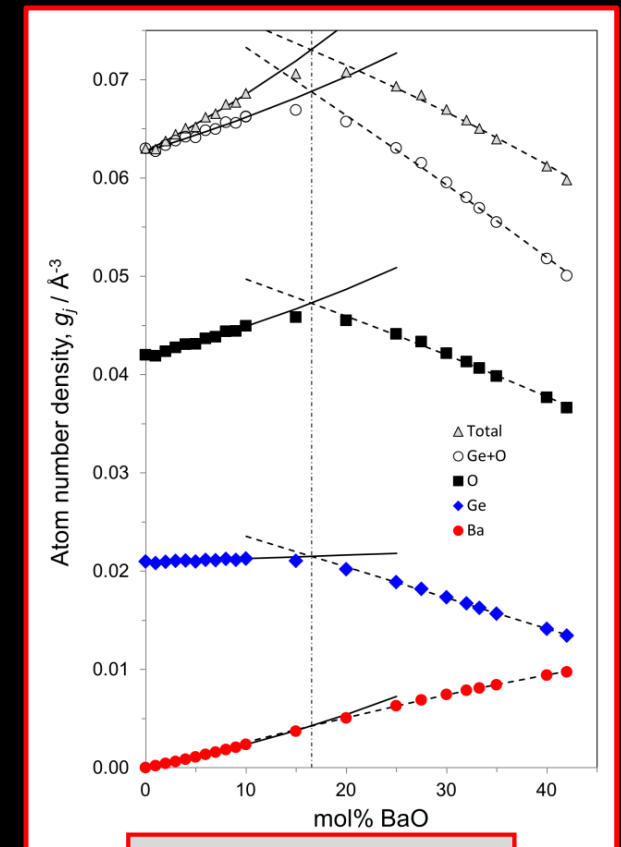
19.1 mol% SrO

16.5 mol% BaO

- Packing behaviour



Strontium germanates

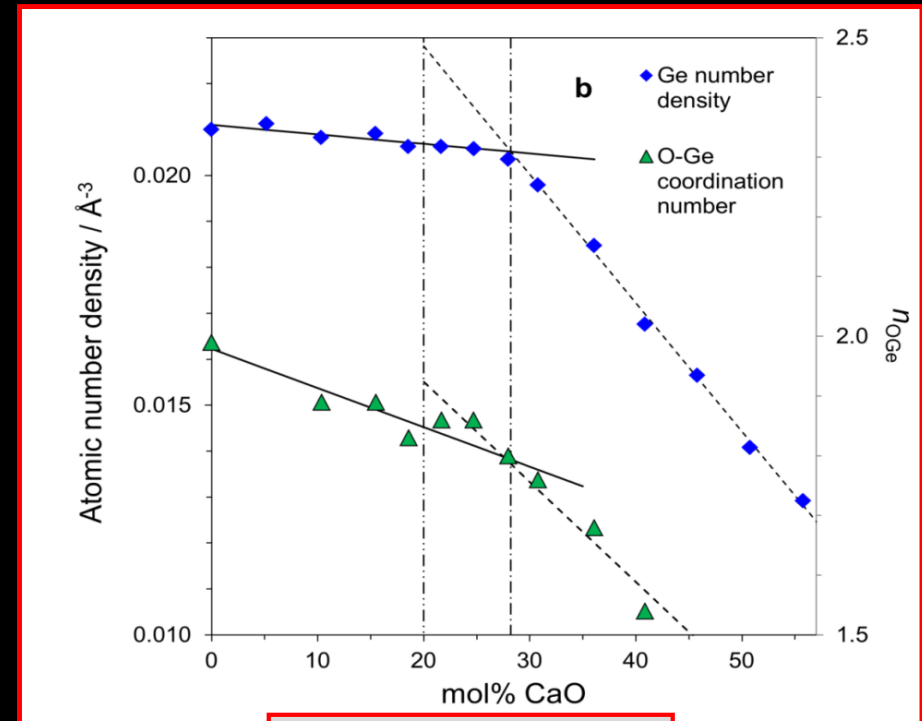


Barium germanates

# Coordination number / Number density Comparison

- The O-Ge coordination number,  $n_{\text{OGe}}$ , is a measure of the depolymerisation of the germanate network (appearance of NBOs)
- $n_{\text{OGe}}$  and Ge number density change behaviour at the same composition as the maximum of  $g_{\text{tot}}$

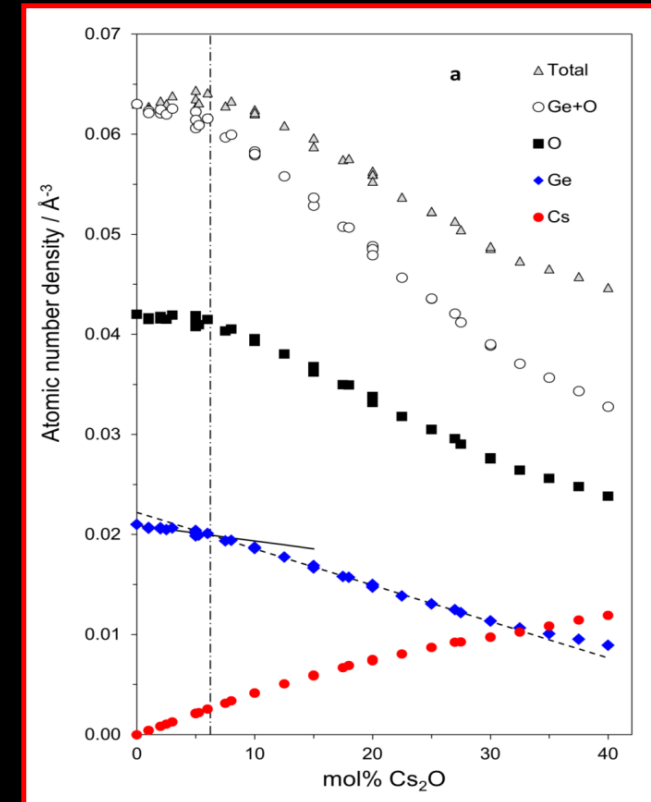
→ This means that the O-Ge coordination number decreases strongly at the same composition that  $\text{Ca}^{2+}$  ions start pushing the germanate network apart



Calcium germanates

# Caesium Germanates Number Density

- Partial number densities have similar behaviour to alkaline earth germanates, and...
- Maximum of  $g_{\text{tot}}$  and change in  $g_{\text{Ge}}$  behaviour occur at similar composition:
  - $g_{\text{tot}}$  maximum is at 4.7 mol%  $\text{Cs}_2\text{O}$
  - $g_{\text{Ge}}$  changes at 6.2 mol%  $\text{Cs}_2\text{O}$



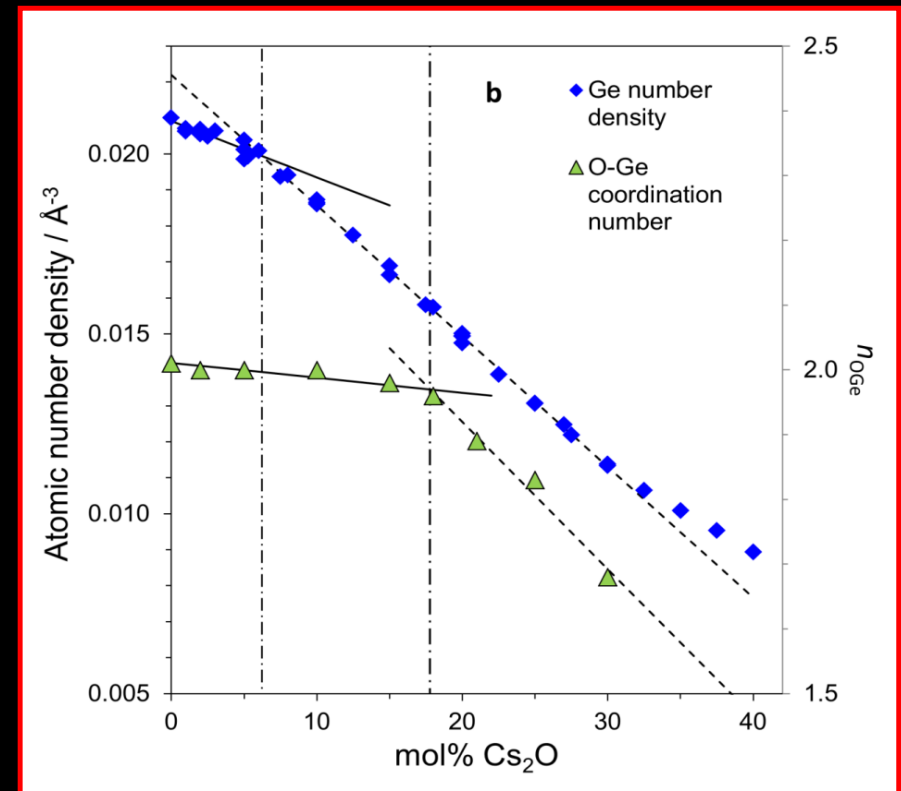


# Caesium Germanates Coordination Number

- Maximum of  $g_{\text{tot}}$  and change in  $g_{\text{Ge}}$  behaviour occur at similar composition:
  - $g_{\text{tot}}$  maximum is at 4.7 mol%  $\text{Cs}_2\text{O}$
  - $g_{\text{Ge}}$  changes at 6.2 mol%  $\text{Cs}_2\text{O}$
- But the O–Ge coordination number decline does not start until 17.8 mol%  $\text{Cs}_2\text{O}$

→ This means that the addition of  $\text{Cs}^+$  ions starts to push apart the germanate network, without causing it to depolymerise. But the coordination number behaviour seems not to be associated with other structural factors of the anomaly.

Neutron diffraction:  
(Hannon et al, *J Phys Chem B*, 2007)



# Germanates Summary

- Ge-O coordination number always grows above tetrahedral  $n_{\text{GeO}}=4$  and then declines, consistent with charge avoidance model
- For  $\text{Cs}_2\text{O-GeO}_2$  the higher  $n_{\text{GeO}}$  value is 5
- For  $\text{Li}_2\text{O-GeO}_2$  the higher  $n_{\text{GeO}}$  value is mostly 6
- Alkaline earth germanates ( $\text{CaO-GeO}_2$ ) are different, and the behaviour is consistent with a packing mechanism

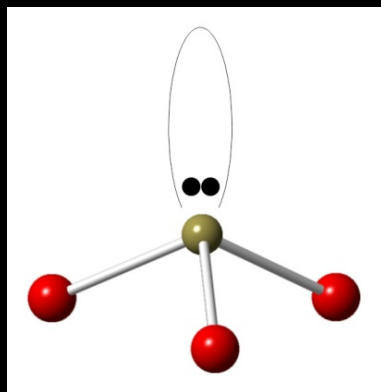
# Tellurite glasses

*e.g.*  $\text{K}_2\text{O}-\text{TeO}_2$

- Applications interest, *e.g.* optical devices
- Fundamental structural interest...

Many structural studies, but slow progress to a clear, quantitative structural understanding – Why?...

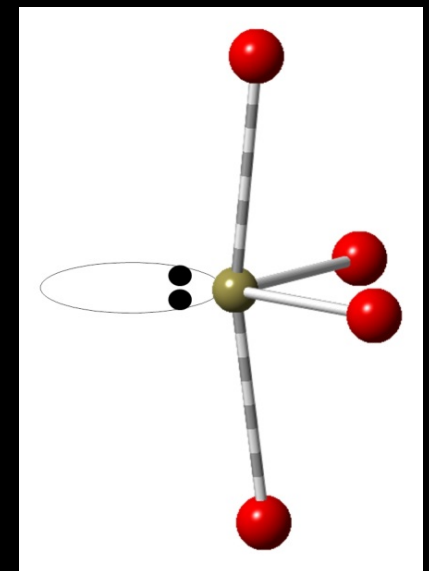
1. Difficulty of making the end-member: pure amorphous  $\text{TeO}_2$
2. Structure is complex and subtle, involving interconversion of  $\text{TeO}_4$  and  $\text{TeO}_3$  units



$\text{TeO}_3$



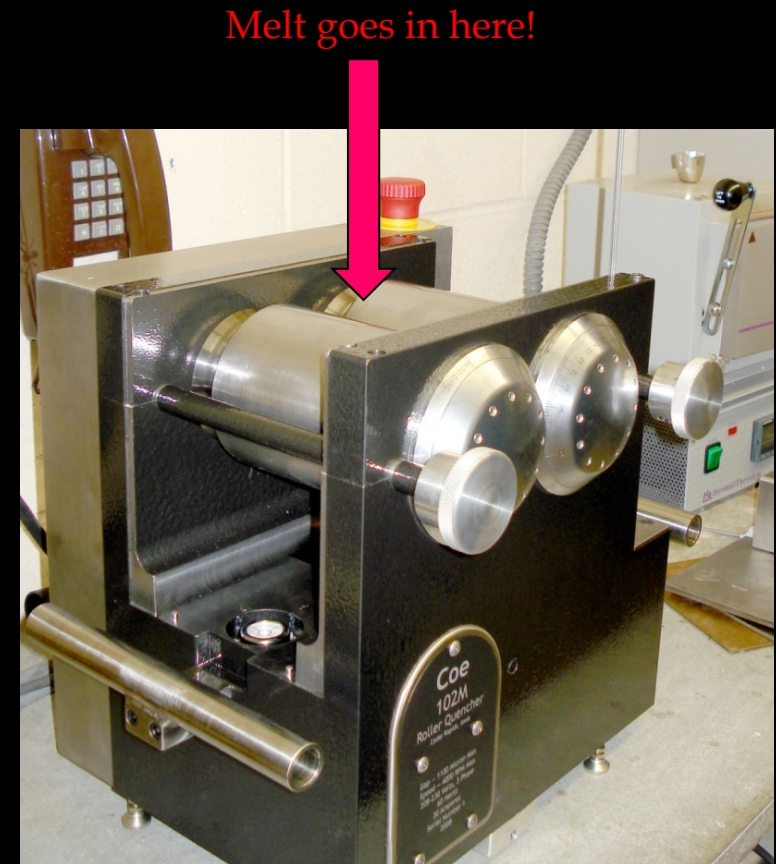
$\text{TeO}_4$



# Pure amorphous $\text{TeO}_2$ - rapid quenching

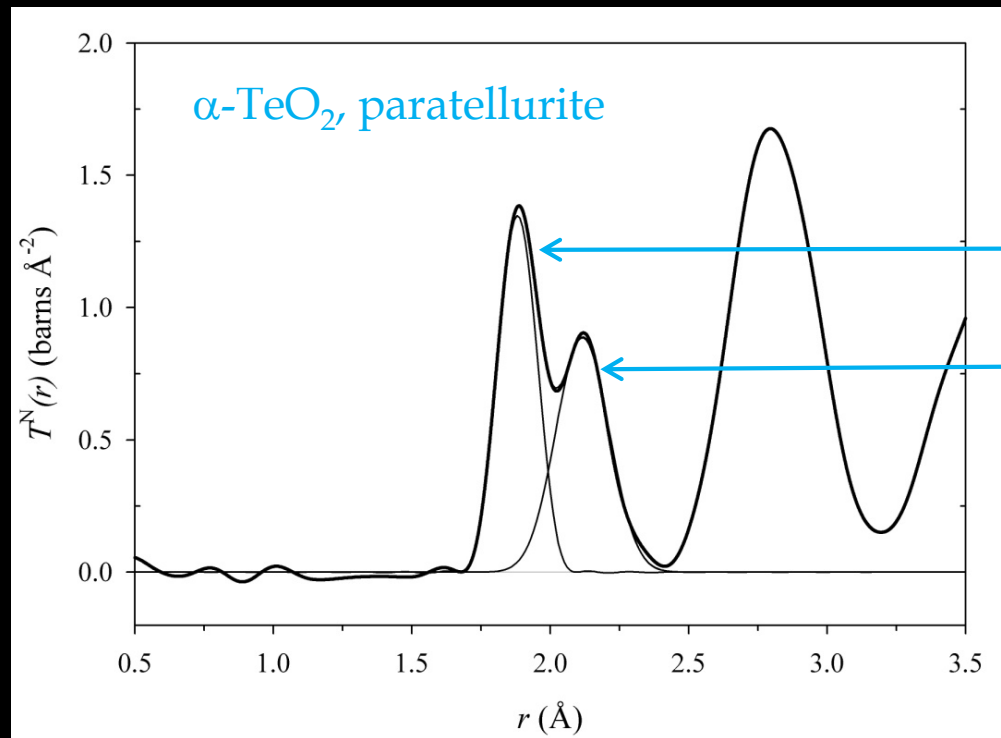
- Pure amorphous  $\text{TeO}_2$  is difficult to make, except in milli-gramme quantities  
(*Lambson et al, JNCS 1984*)
- Usually addition of modifier is required to stabilise the glass  
(*Lambson et al, JNCS 1984*)
- We made few gramme sample of pure amorphous  $\text{TeO}_2$  by twin-roller rapid quenching at Coe College  
(*Havel, Feller et al, Glass Technology 2009*)

(A crucible-quenching method has recently been perfected by Tagiara et al, J Non-Cryst Solids, 2017)



# Neutron diffraction (ND)

- ND can provide the most accurate coordination numbers
- Error can be ~1%
- e.g. for  $\text{GeO}_2$  glass we measured  $n_{\text{GeO}}=4.03$
- e.g. for crystalline  $\alpha\text{-TeO}_2$  we measured  $n_{\text{TeO}}=3.95$



Short Te-O 1.882Å 1.95 atoms

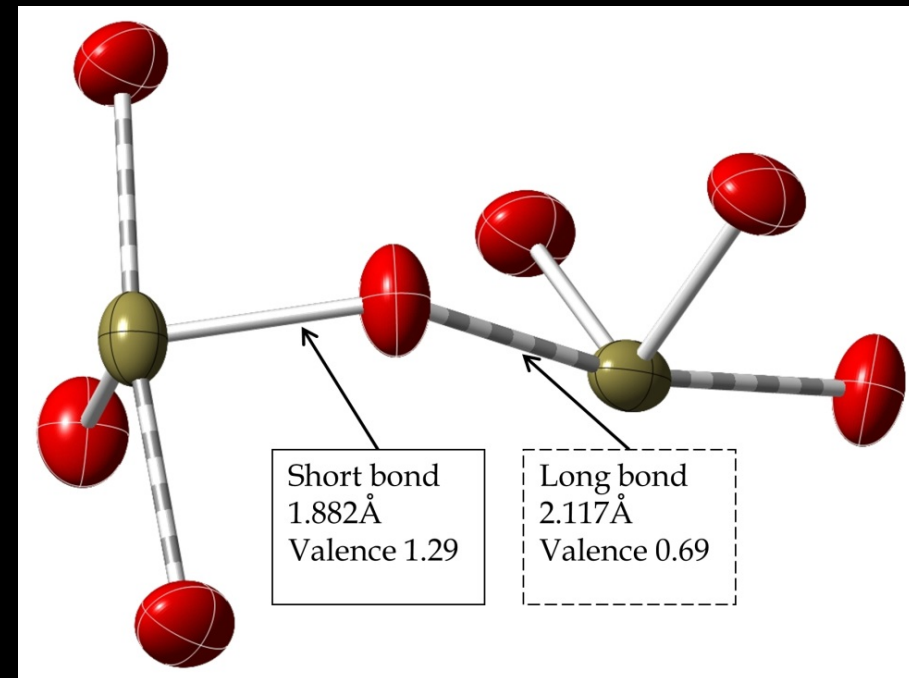
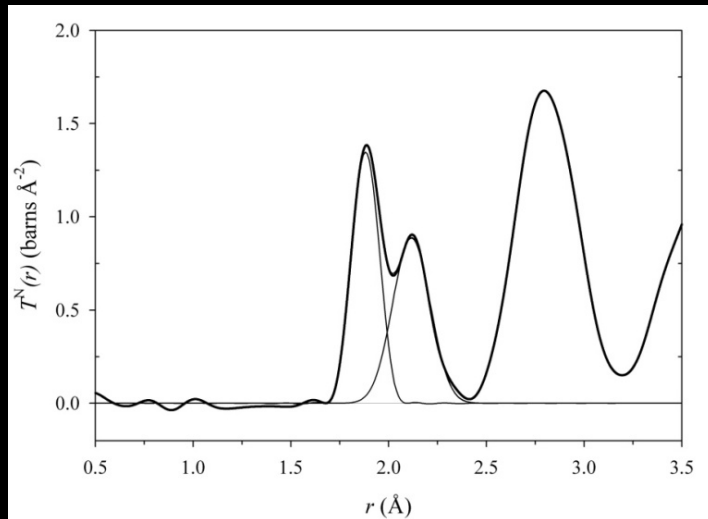
Long Te-O 2.117Å 2.00 atoms

Barney, Hannon, Holland,  
*J Phys Chem C* 2012

Hannon, *J Phys Chem B* 2007)

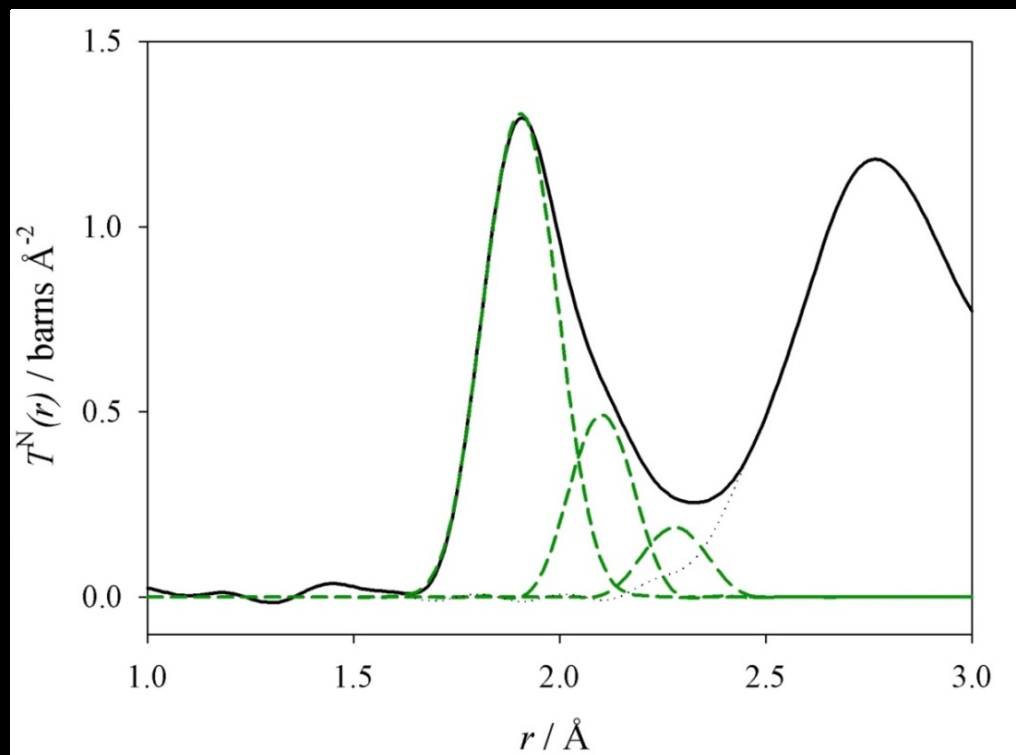
# $\alpha$ -TeO<sub>2</sub> Crystal Structure (paratellurite)

- Each bridge between two TeO<sub>4</sub> units has one short and one long Te-O bond
- It is often assumed that amorphous TeO<sub>2</sub> has a similar structure, based on TeO<sub>4</sub> units



*Barney, Hannon, Holland,  
J Phys Chem C 2012*

# Amorphous TeO<sub>2</sub> – Neutron Diffraction



If  $n_{\text{TeO}} < 4 \Rightarrow n_{\text{OTe}} < 2$   
*i.e.* if there are 3-coordinated Te,  
 there must be terminal oxygens

- Neutron diffraction at ISIS Facility neutron source
- Fitting gives Te-O coordination number  $n_{\text{TeO}} = 3.68(4)$  and then...
- 32% of Te are 3-coordinated
- $n_{\text{OTe}} = 1.84(1)$   
*i.e.* 16% of oxygens are terminal

# Terminal Oxygens

A terminal oxygen is bonded to only one cation.  
A non-bridging oxygen is bonded to one glass-former cation  
PLUS some modifier cations

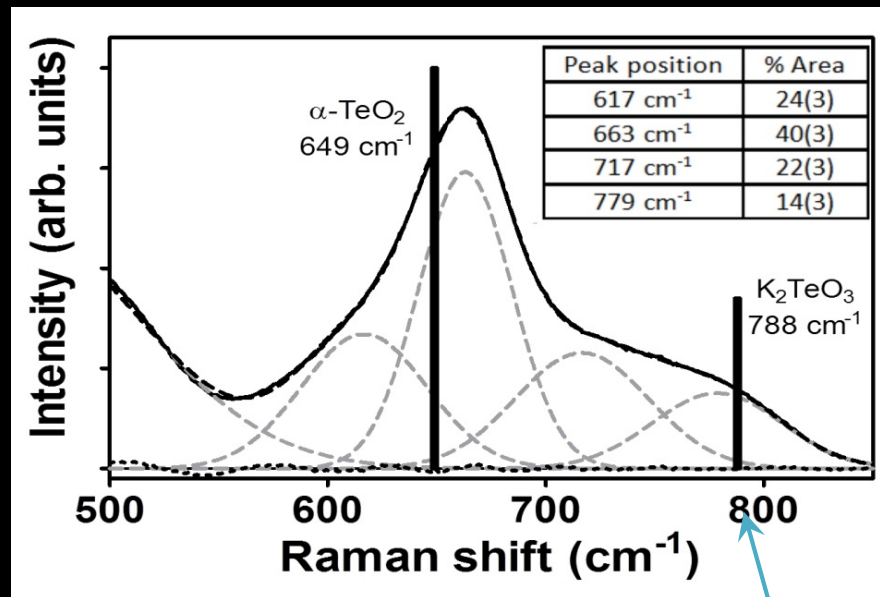
- A  $\text{TeO}_2$  molecule is known – it has two terminal  $\text{Te}=\text{O}$  bonds of length  $1.83\text{\AA}$   
(Zasorin et al, J Struct Chem 1974)
- Some workers consider  $\alpha\text{-TeO}_2$  to be a molecular crystal of  $\text{TeO}_2$  molecules  
(Gabuda, J Phys Chem B 2006)
- Molecular Dynamics for amorphous  $\text{TeO}_2$  gives  $n_{\text{TeO}}=3.69$  &  $n_{\text{TeO}}=1.85$   
(Piettrucci et al, Phys Rev B 2008)
- Raman spectrum of amorphous  $\text{TeO}_2$  recently interpreted to give  $n_{\text{TeO}}\sim 3.67$   
(Kalampounias, Vib Spec 2012)
- $5\text{V}_2\text{O}_5\cdot 95\text{TeO}_2$  glass – ND gives  $n_{\text{TeO}}=3.3\pm 0.2$   
(Sinclair et al, JNCS 1998)
- $\text{P}_2\text{O}_5$  glass is now well known to have terminal  $\text{P}=\text{O}$  bonds  
(Hoppe et al, J Phys Cond Matt 1998)



# TeO<sub>2</sub> Raman Spectrum

- $\alpha$ -TeO<sub>2</sub>: contains only TeO<sub>4</sub>, principal peak 649cm<sup>-1</sup>
- Crystalline K<sub>2</sub>TeO<sub>3</sub>: contains only TeO<sub>3</sub>, principal peak 788cm<sup>-1</sup>
- Amorphous TeO<sub>2</sub>: Areas of fitted peaks give  $n_{\text{TeO}}=3.64$

Following (Kalampounias, *Vib Spec* 2012)



Vibration at  $\sim 780\text{cm}^{-1}$  is associated with TeO<sub>3</sub> units  
Crystals containing only TeO<sub>4</sub> units have little or no intensity at  $\sim 780\text{cm}^{-1}$

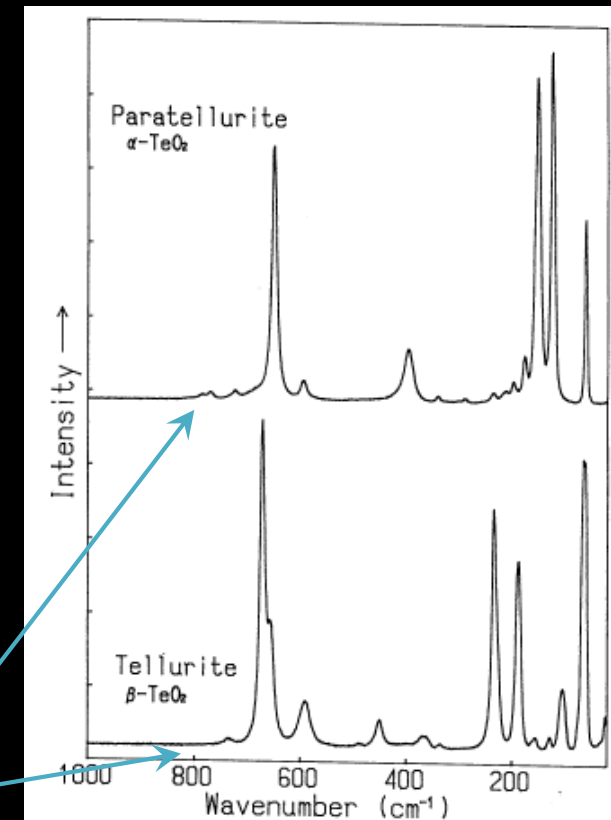
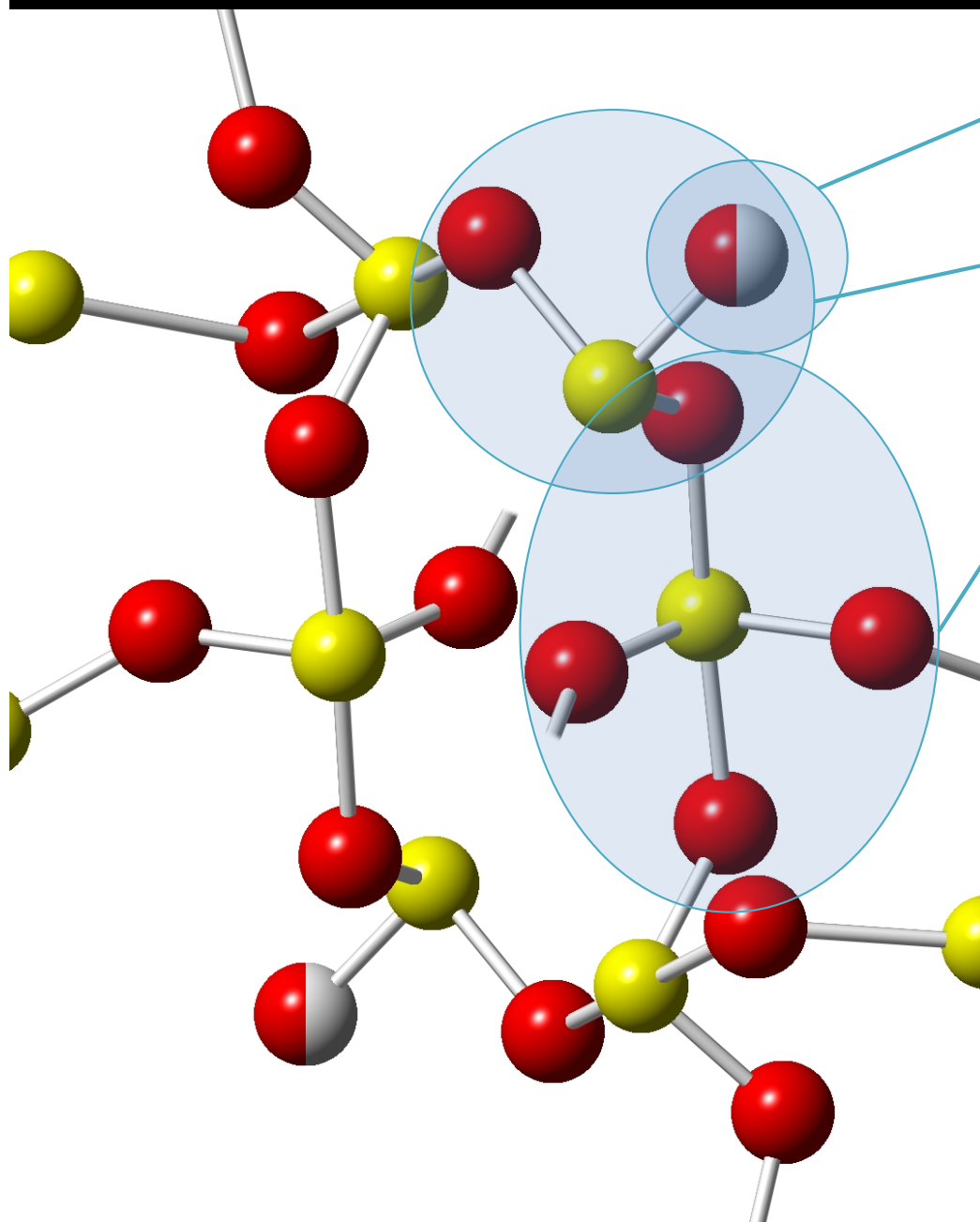


Fig. 1. Raman spectra of two polymorphic forms of TeO<sub>2</sub> crystals, paratellurite and tellurite.

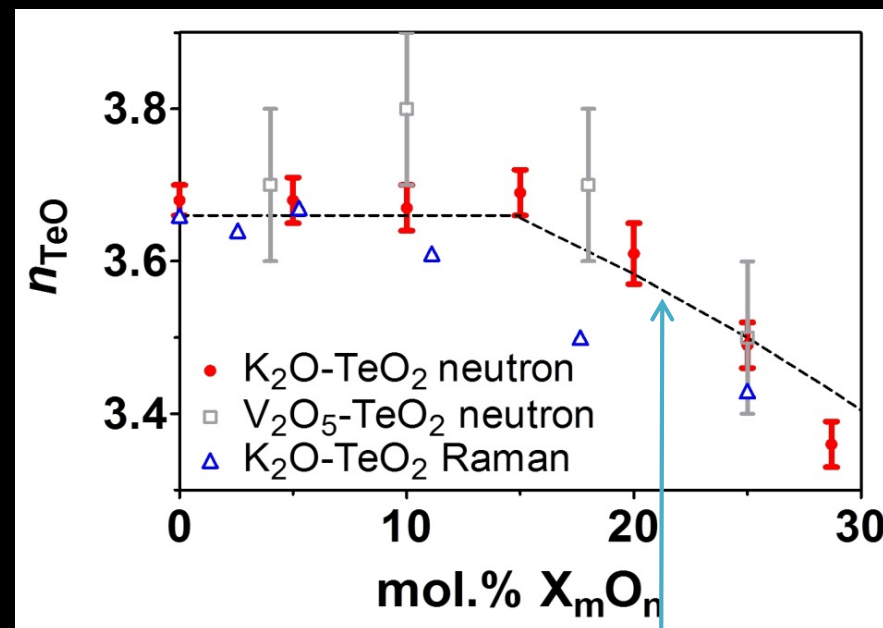
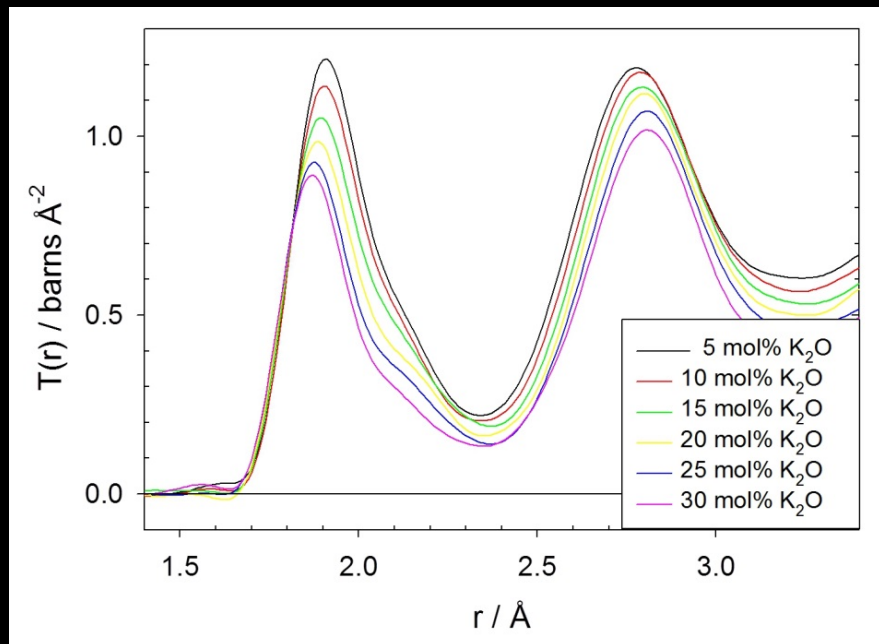
Sekiya et al, *J Cer Soc Jpn* 1989

# TeO<sub>2</sub> Structure



- Terminal oxygen
- TeO<sub>3</sub>
- TeO<sub>4</sub>
- Based on crystal structure of K<sub>2</sub>Te<sub>4</sub>O<sub>9</sub>  
(Becker et al, Inorg Chem 1997)

# $K_2O-TeO_2$ glasses – Neutron Diffraction

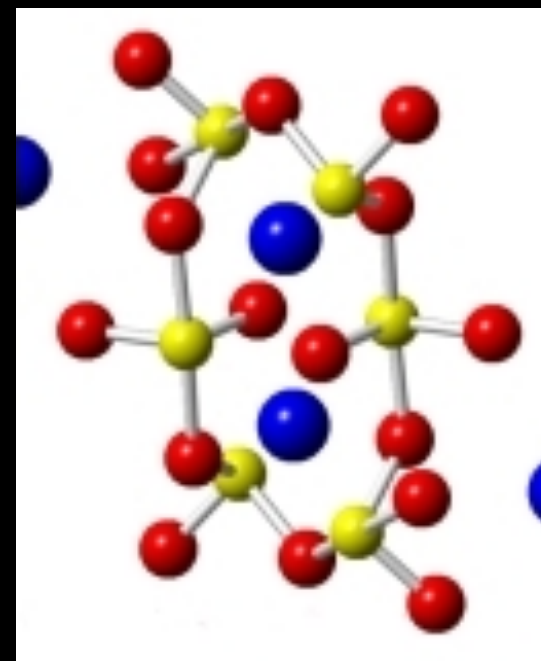
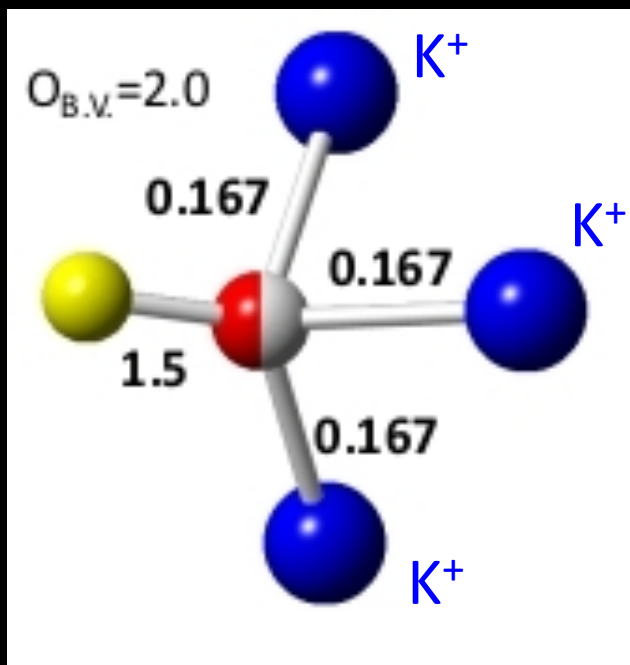


dashed line is model

- ND on series of  $K_2O-TeO_2$  glasses (roller quenched at Osaka Prefecture University)
- Te–O coordination number  $\sim$ constant below  $\sim 15$  mol%  $K_2O$ , decreases above  $\sim 15$  mol%  $K_2O$

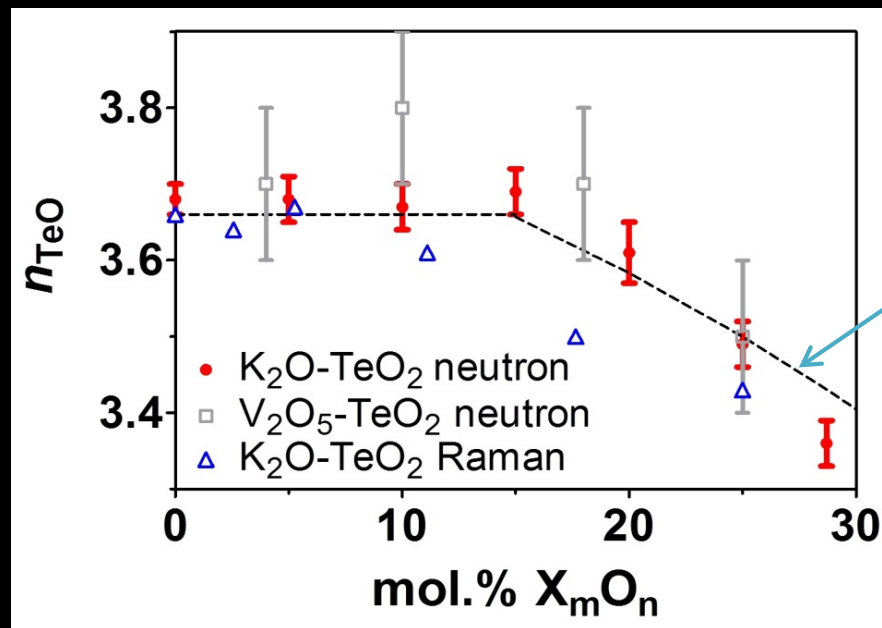
# Model for Tellurites

- Model is inspired by  $\text{K}_2\text{Te}_4\text{O}_9$  crystal (*Becker et al, Inorg Chem 1997*)
- $\text{K}_2\text{Te}_4\text{O}_9$  has both  $\text{TeO}_3$  and  $\text{TeO}_4$  units, and non-bridging oxygens
- Each NBO is coordinated by 3  $\text{K}^+$  ions
- Model is based on 6-membered ring in  $\text{K}_2\text{Te}_4\text{O}_9$  crystal



# Model for Tellurites

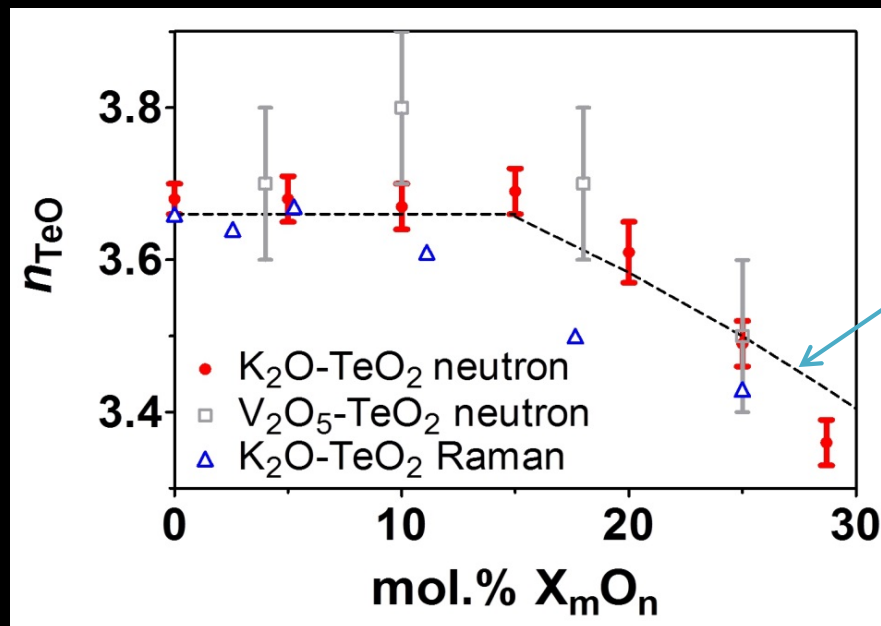
- Adding  $K_2O$  to pure  $TeO_2$  creates NBOs,  $n_{TeO}$  does not change
- Each  $K^+$  ion bonds to 6 oxygens, 3 new NBOs, and 3 previously terminal oxygens
- At composition 14.3 mol%  $K_2O$ , all terminal oxygens are used up – then adding more  $K_2O$  causes conversion of  $TeO_4$  to  $TeO_3$  ...



dashed line is model

# Model for Tellurites

- For more than 14.3 mol%  $K_2O$ , the addition of  $K_2O$  breaks one additional Te–BO bond, converting  $TeO_4$  to  $TeO_3$
- $K^+$  ions now bond to some BO as well as NBO
- For this model, limit of glass formation is 31.8 mol%  $K_2O$   
– we made glass up to 28.7 mol%  $K_2O$

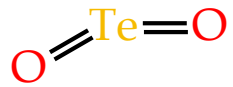


dashed line is model

# Glass Formation

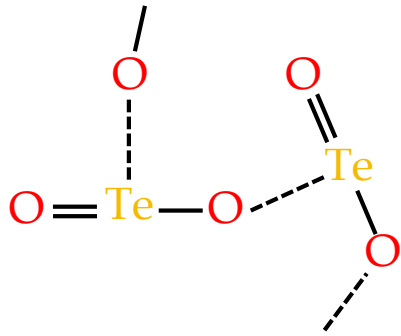
Gas

$$n_{\text{TeO}}=2$$



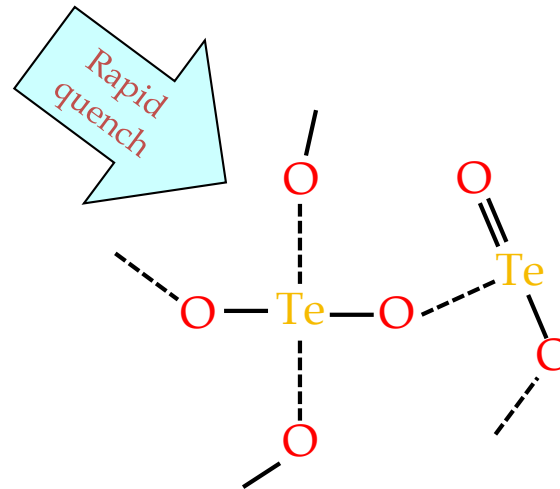
Liquid

$$n_{\text{TeO}}=2-4 \sim 3 ?$$



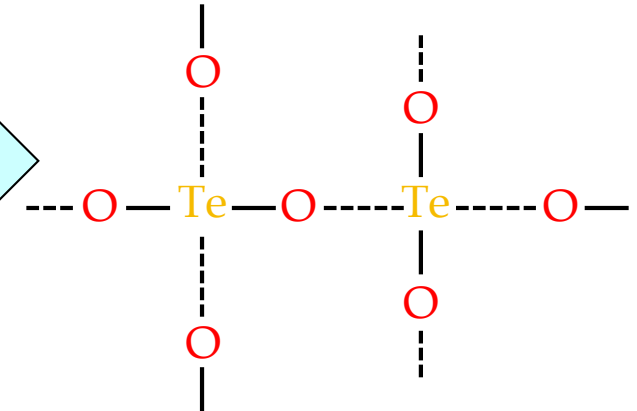
Glass

$$n_{\text{TeO}}=3.68$$



Crystal

$$n_{\text{TeO}}=4$$



Normal quench

Rapid quench

= Terminal bond  
 — Short strong bond  
 ----- Long weak bond

- Long weak bonds form when  $\text{TeO}_2$  is cooled

# Tellurites Summary

- Grammes of amorphous  $\text{TeO}_2$  can be made by roller quenching
- Te–O coordination number is  $n_{\text{TeO}}=3.68(4)$  ,  
one third of Te are 3-coordinated,  
16% of oxygens are TERMINAL
- In  $\text{K}_2\text{O}-\text{TeO}_2$  glasses, Te–O coordination number is unchanged for low  $\text{K}_2\text{O}$ , then decreases for more than  $\sim 15$  mol%  $\text{K}_2\text{O}$
- A model, based on discovery of terminal oxygens in pure  $\text{TeO}_2$ , accounts for the change in Te–O coordination number in tellurite glasses



Thanks for listening!  
Any questions?