

**Formation and evolution of bubbles in ascending magmas:
Insight from decompression experiments
in the systems rhyolite-H₂O and basalt-CO₂**

Didier LAPORTE

**In collaboration with: Ariel PROVOST, Nicolas CLUZEL, Mohirisa HAMADA,
Manon HARDIAGON, Catherine MOURTADA-BONNEFOI**

I. Introduction: Importance of the kinetics of magma degassing

II. Effect of ascent rate on homogeneous bubble nucleation in the system rhyolite-H₂O

III. Homogeneous bubble nucleation in the system basalt-CO₂

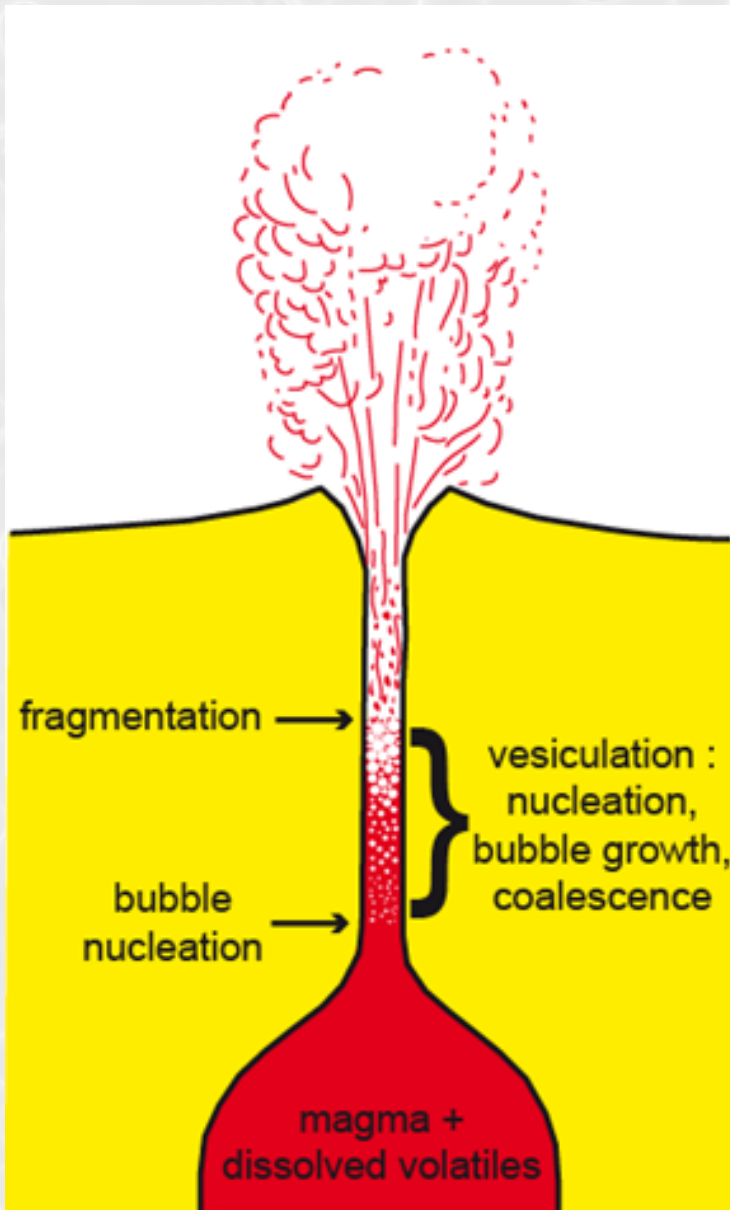
The importance of magma degassing:

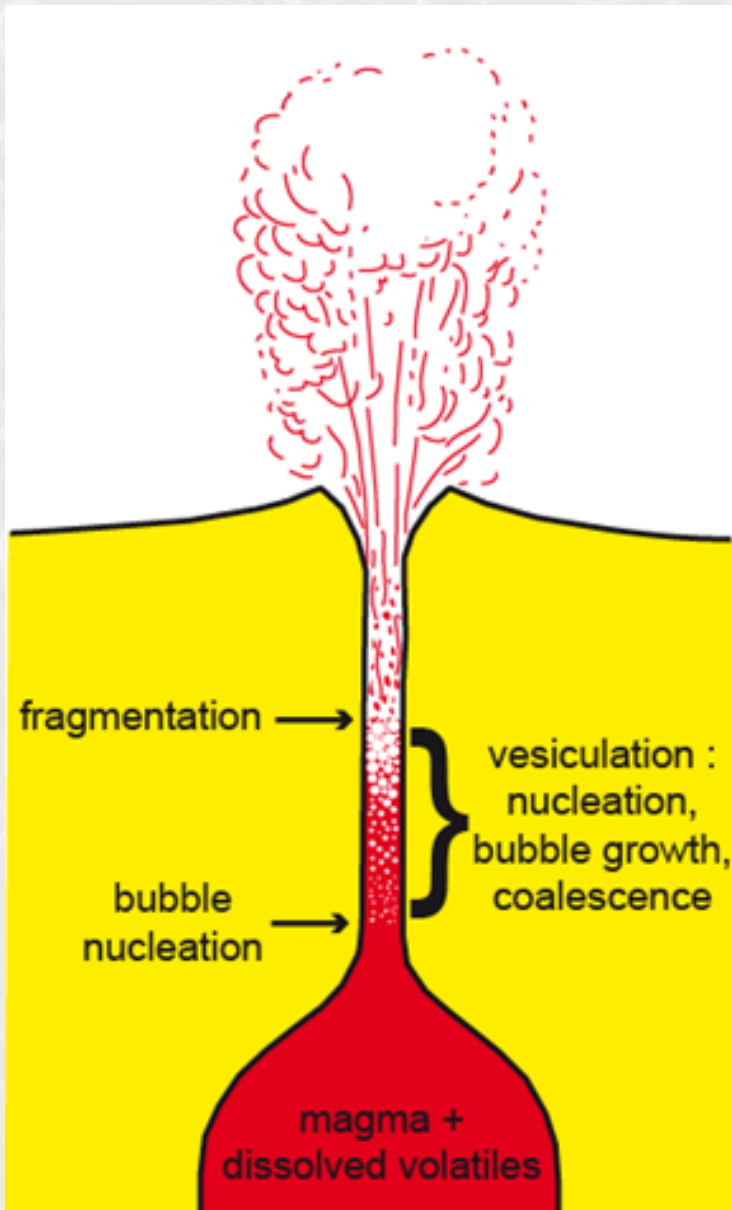
⇒ Exsolution + expansion of volatiles = the main driving forces for magma ascent and volcanic eruptions

⇒ Magmas release huge amounts of volatiles (H_2O , CO_2 , SO_2) into the atmosphere:

⇒ Impact on weather and long-term climate → mass extinctions...

⇒ Formation and composition of planetary atmospheres



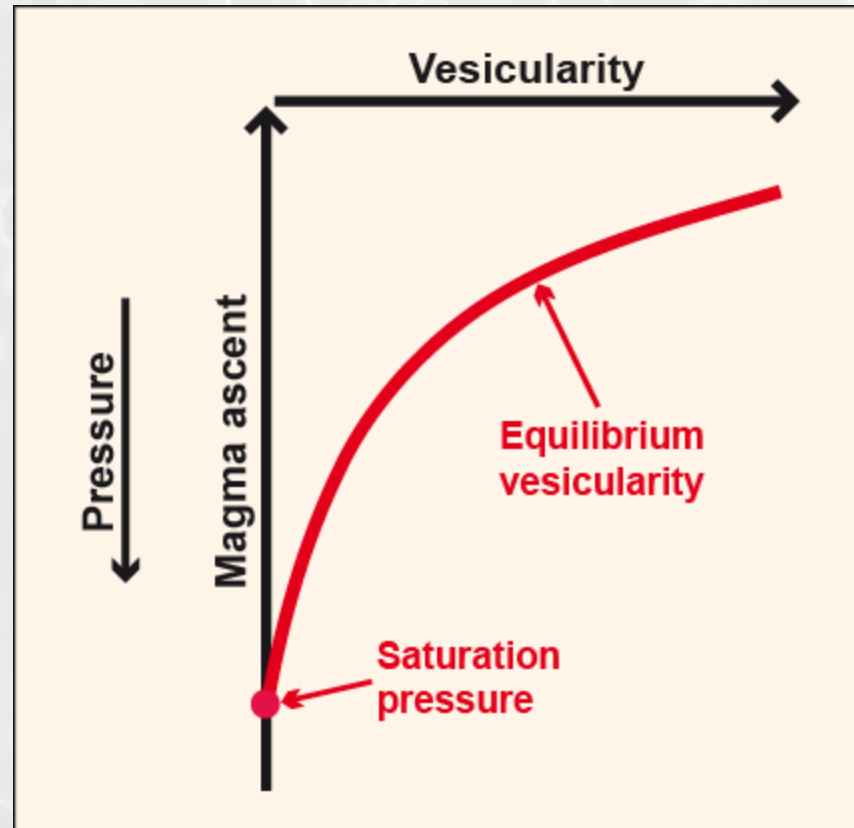


⇒ This talk will focus on processes occurring during magma ascent, specially on the first stage of degassing: **bubble nucleation**

⇒ Pressures of bubble nucleation, P_N ?

⇒ Bubble number densities, BND (numbers of bubbles formed per unit volume of liquid)?

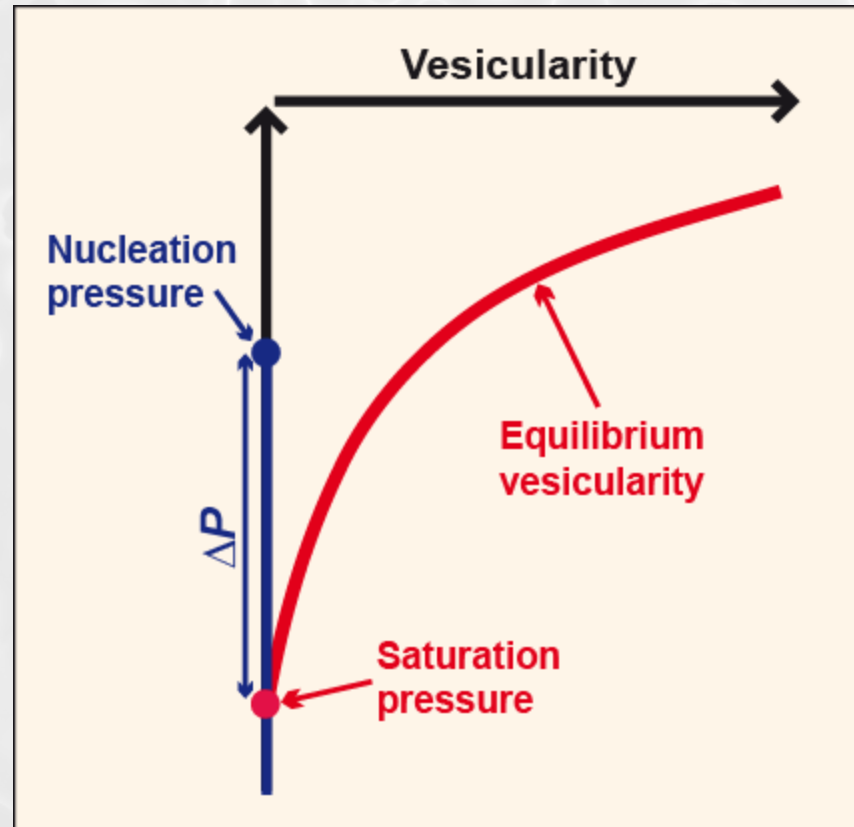
P_N and BND: control the kinetics of degassing



**Equilibrium
degassing**

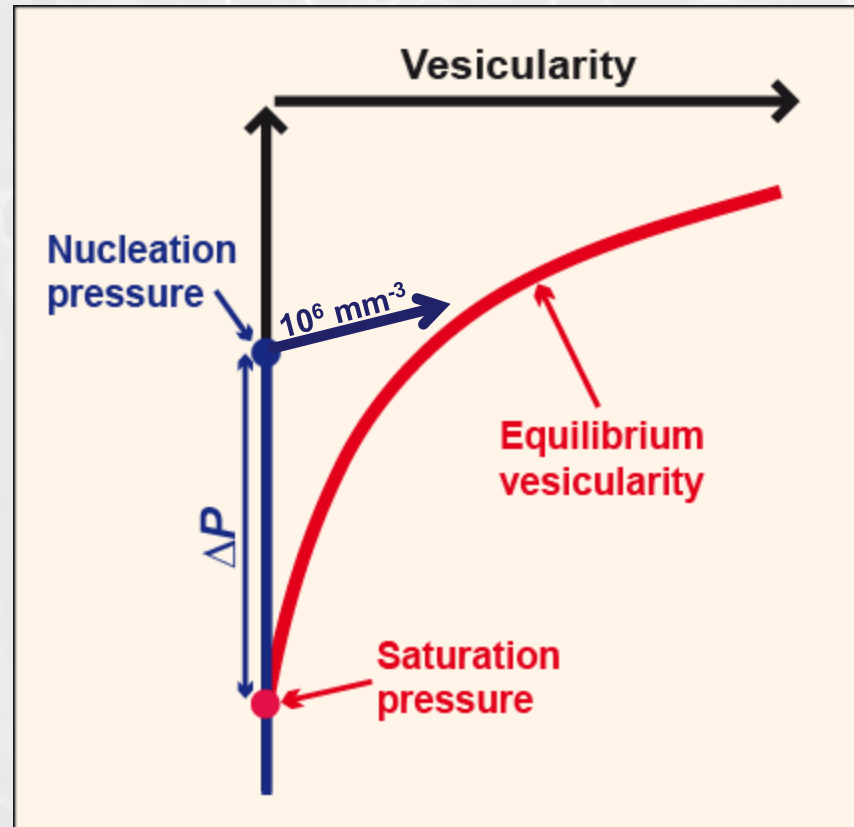
$$\text{Vesicularity} = \frac{\text{Volume of bubbles}}{\text{Total volume}}$$

P_N and BND: control the kinetics of degassing



1) Delayed bubble nucleation due to the effect of surface tension

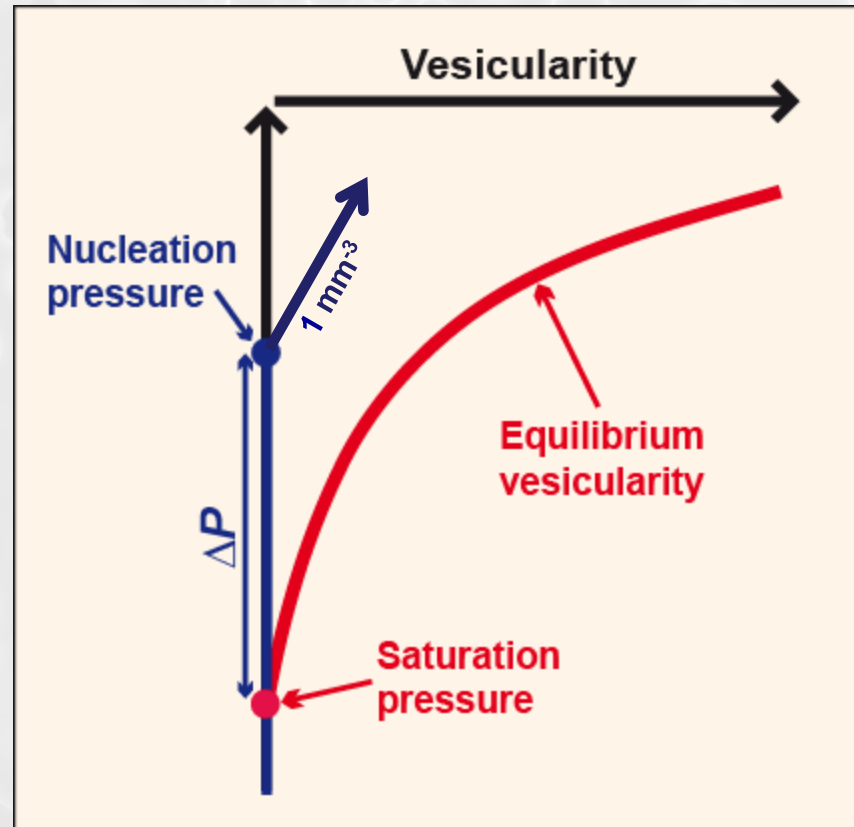
P_N and BND: control the kinetics of degassing



2) BND controls the efficiency of degassing:

Large BND \Rightarrow degassing close to equilibrium

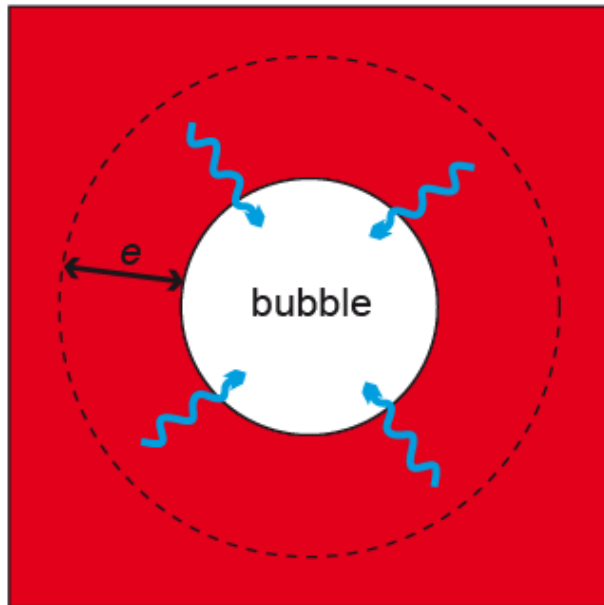
P_N and BND: control the kinetics of degassing



2) BND controls the efficiency of degassing:

Small BND \Rightarrow disequilibrium degassing

Importance of the number density of bubbles, N : diffusion length scale e vs. mean bubble-to-bubble distance d

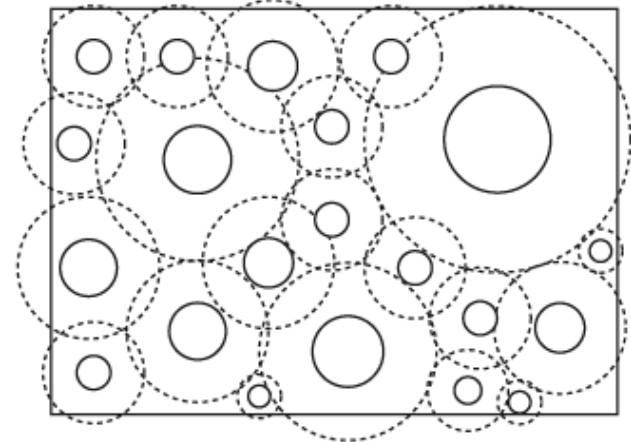


$$e = \sqrt{2Dt}$$

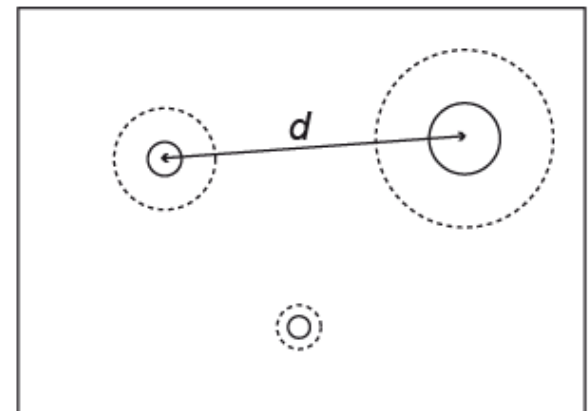
e : length scale of diffusion of volatile components
 D : diffusion coefficient (for water : 10^{-11} m²/s)
 t : time scale of vesiculation ($t = 100$ - 10000 s)

$$e = 0.05\text{-}0.5 \text{ mm}$$

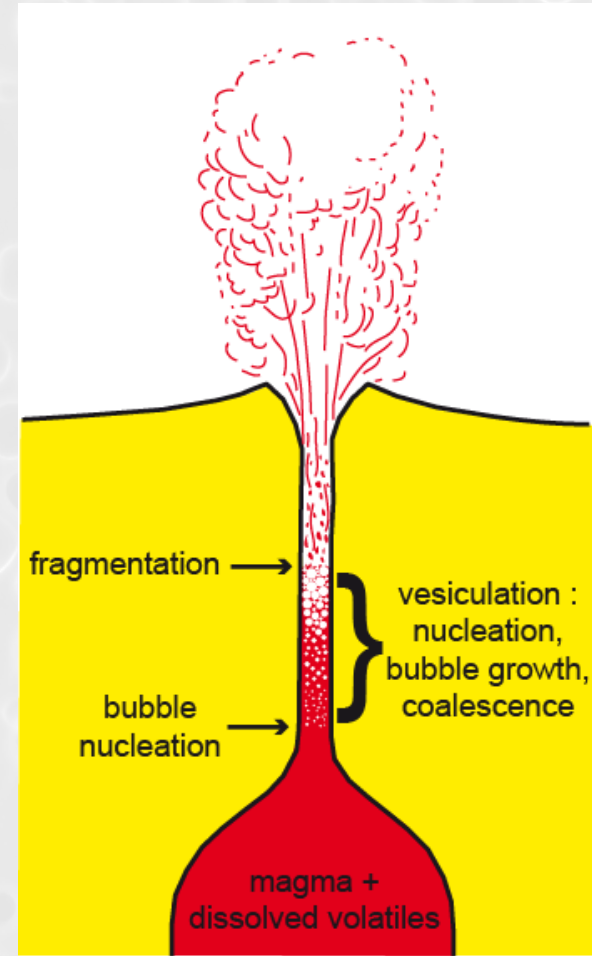
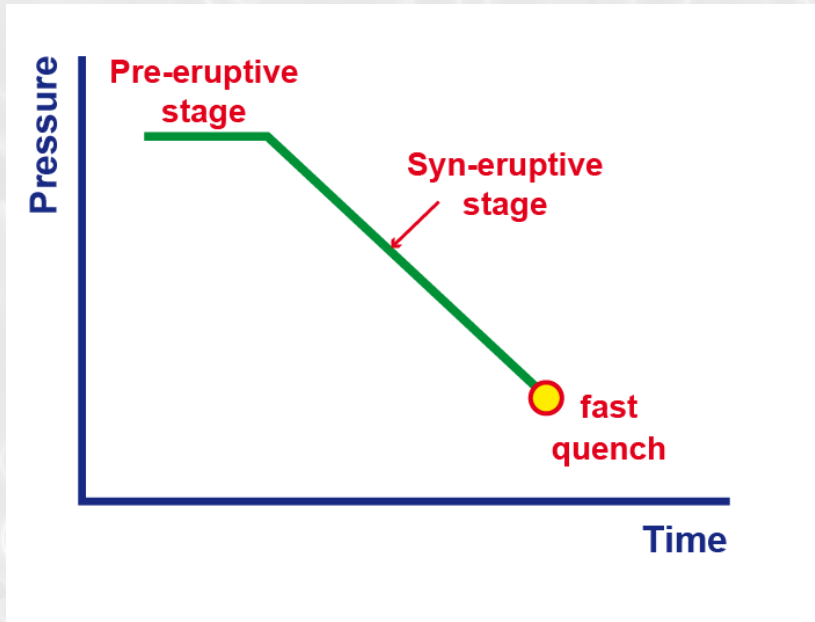
Large N : $d \ll 2e$
equilibrium degassing



Small N : $d \gg 2e$
disequilibrium degassing



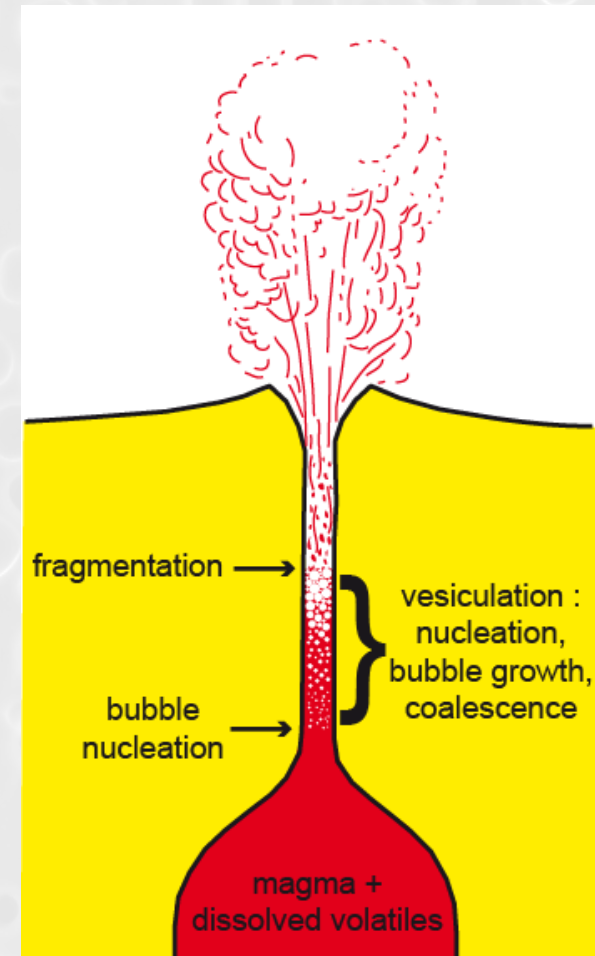
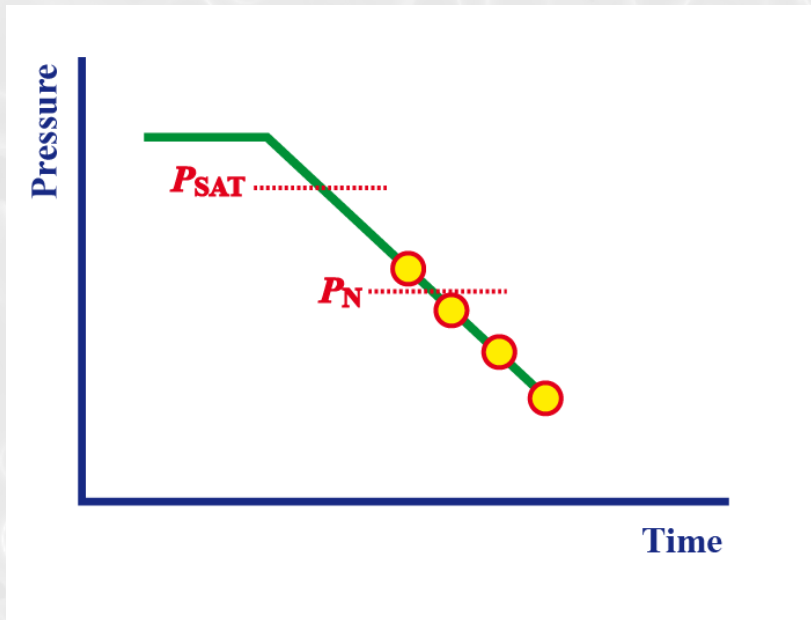
Magma ascent and degassing can be simulated in the laboratory by running decompression experiments at high pressure and temperature



Experiments quenched at different P :

⇒ bracket the nucleation pressure

⇒ follow the evolution of the main textural and chemical parameters



I. Introduction: Importance of the kinetics of magma degassing

II. Effect of ascent rate on homogeneous bubble nucleation in the system rhyolite-H₂O

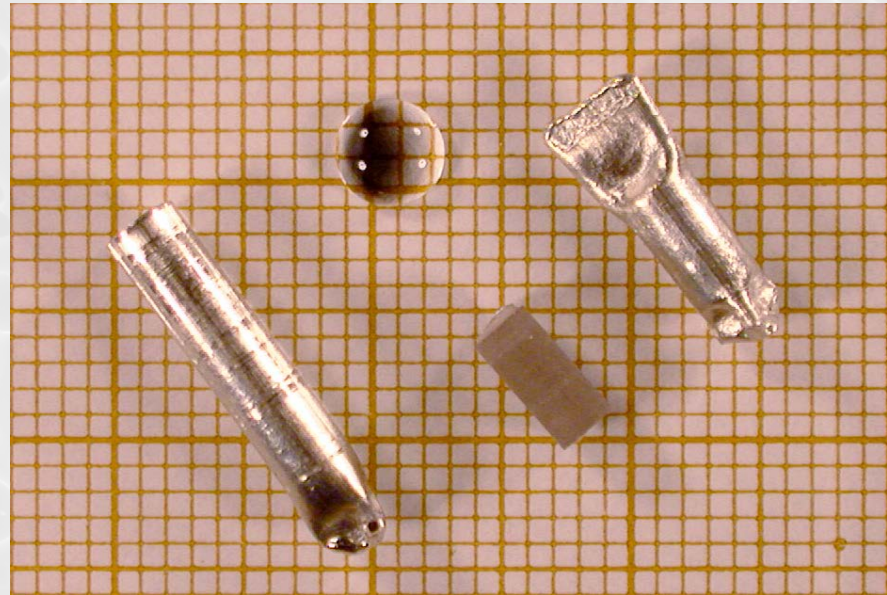
III. Homogeneous bubble nucleation in the system basalt-CO₂

⇒ Starting material = cores drilled into a rhyolitic obsidian

⇒ Saturated in water before decompression

SiO₂	76.51
Al₂O₃	12.56
Fe₂O₃	0.78
MgO	0.01
CaO	0.25
Na₂O	4.47
K₂O	4.24
TiO₂	0.03
MnO	0.07
H₂O	1.39
CO₂	200 ppm
Cl	634 ppm
F	710 ppm
S	< 100 ppm

⇒ 2.5 mm O.D. cylinder



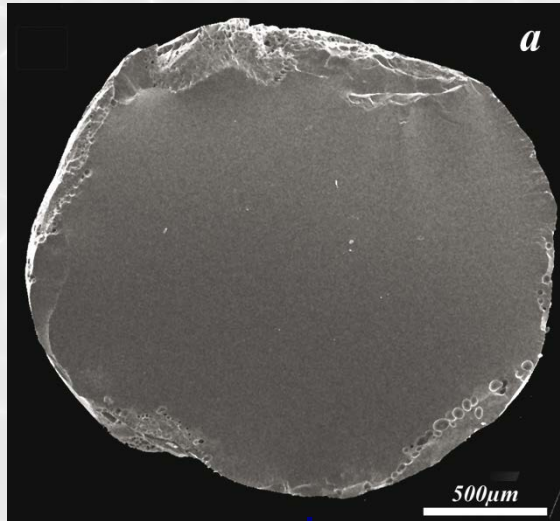
⇒ System: rhyolite + $\approx 7\%$ H₂O; $T = 800^\circ\text{C}$; $P_{\text{SAT}} \square 240$ MPa (Mourtada-Bonnefoi and Laporte, 2004; Hamada et al., 2010)

⇒ Decompression rates from 0.0278 to 90 MPa/s to quantify the effect of ascent rate on the kinetics of homogeneous bubble nucleation

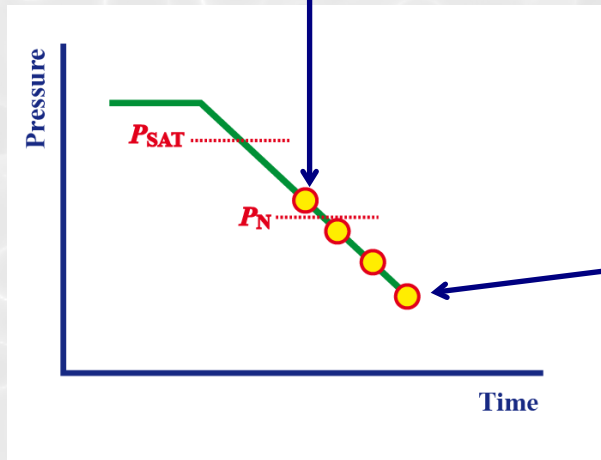
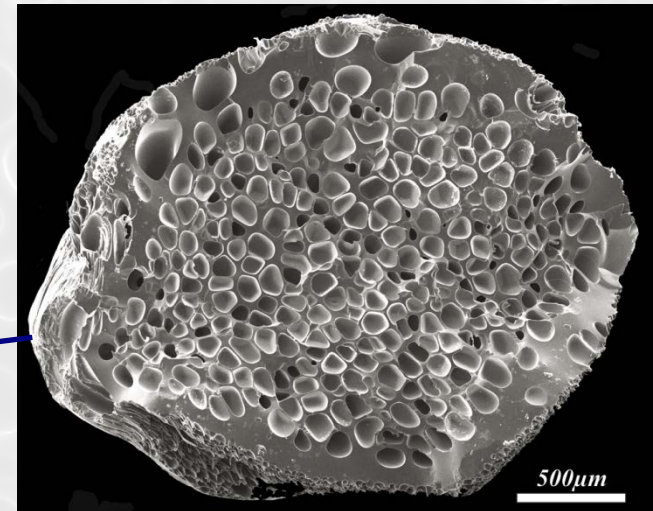
⇒ 1 MPa/s (10 bar/s) is equivalent to an ascent rate of 40 m/s (for a liquid density of 2500 kg/m³)

Nucleation pressures

No bubbles : $P > P_N$



Bubbly core : $P \leq P_N$



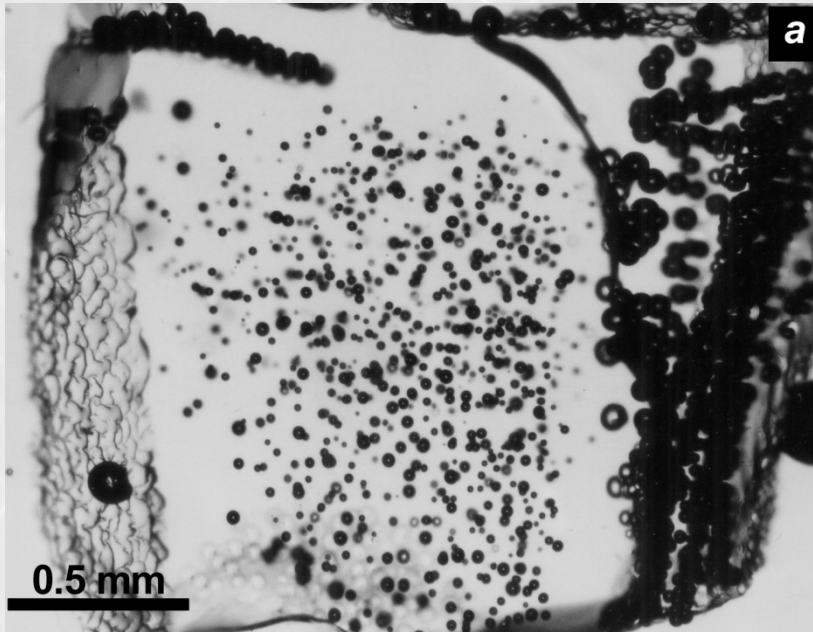
- $P_N = 90 \pm 2$ MPa in all series $\Rightarrow \Delta P (= P_{SAT} - P_N) = 150$ MPa
- ΔP very large in the case of homogeneous bubble nucleation, and only very slightly dependent of decompression rate

Textural parameters

#A2

1 MPa/s

$P_f = 79.2$ MPa

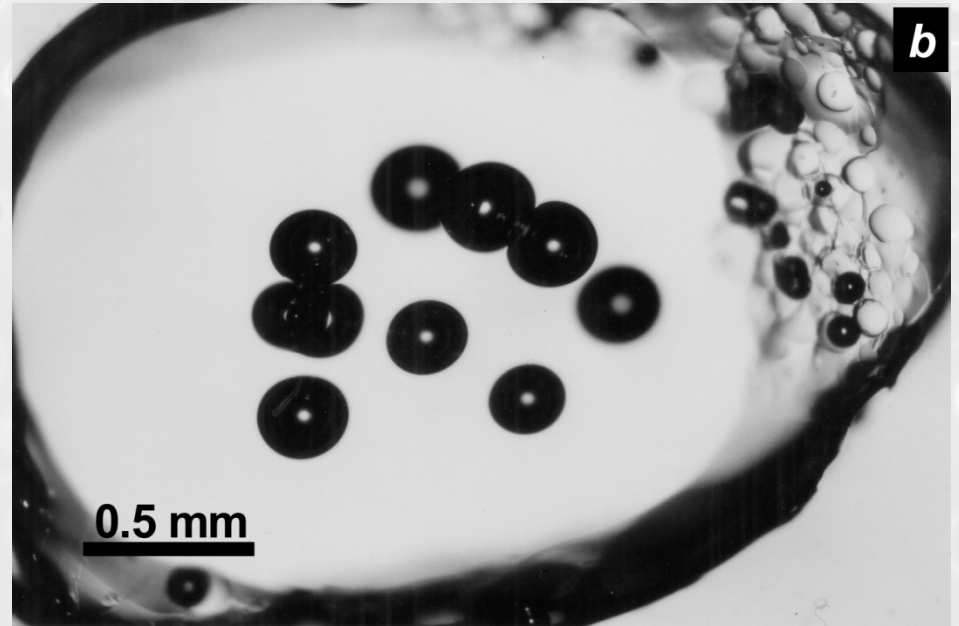


$d = 23.1 \mu\text{m}$, $N = 2300 \text{ mm}^{-3}$

#C8

0.0278 MPa/s

$P_f = 79.5$ MPa

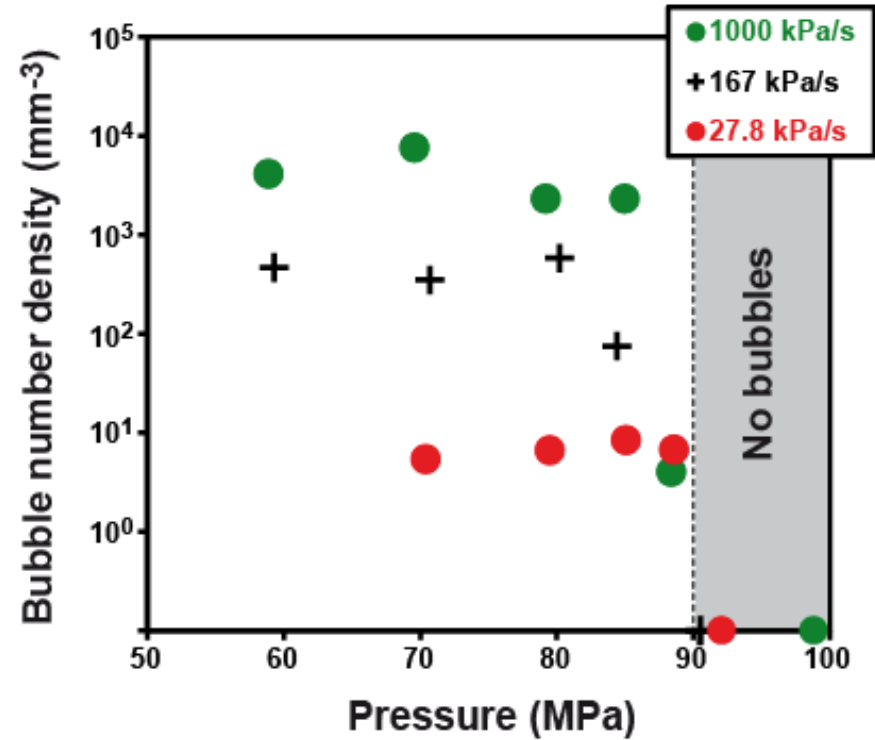


$d = 258 \mu\text{m}$, $N = 6.6 \text{ mm}^{-3}$

Strong variations of bubble number density N and mean bubble diameter d as a function of decompression rate

Textural parameters

⇒ Below P_N , BND rapidly reaches a stationary value very sensitive to $|dP/dt|$.



Classical theory of nucleation:

Calculation of surface tension coefficient, σ_{LG} (N/m), from the nucleation pressure P_N

Hirth et al., 1970; Hurwitz and Navon, 1994; Cluzel et al., 2008

$$J = J_0 e^{-\frac{16\pi\sigma_{LG}^3}{3kT(P_G^* - P_L)^2}}$$

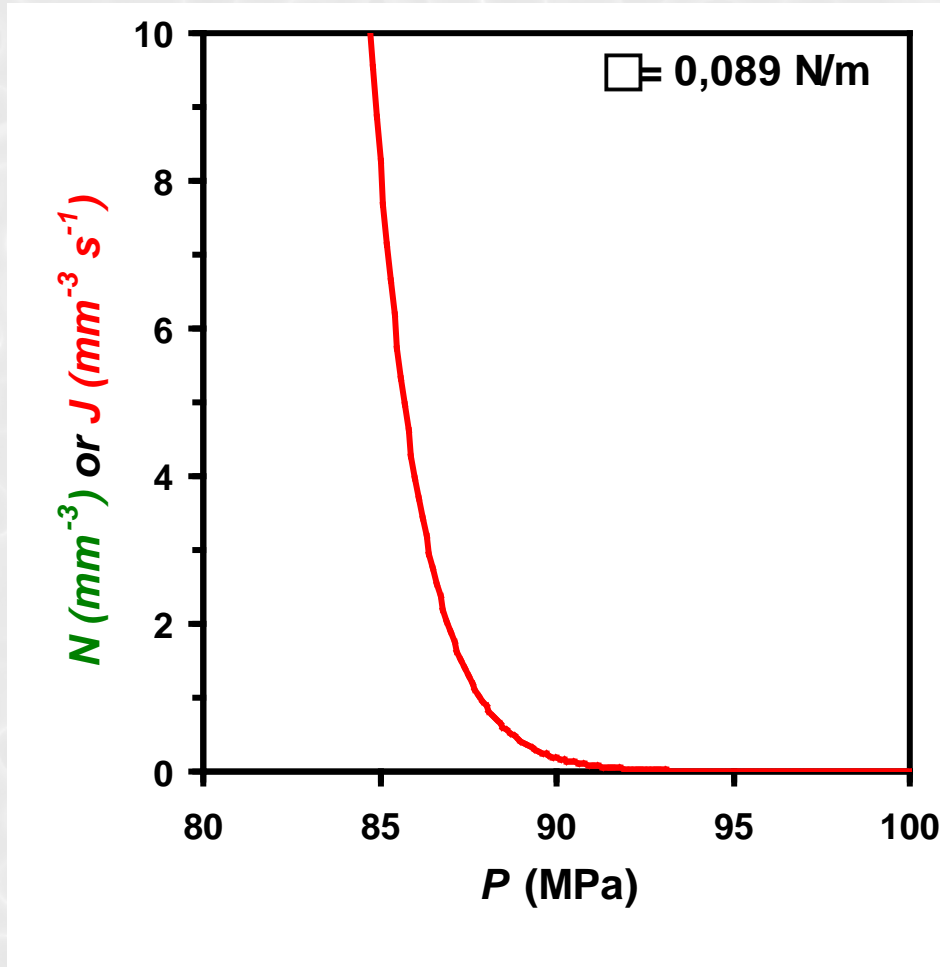
$$J_0 = \frac{2\Omega_L n_0^2 D_{H_2O}}{a_0} \sqrt{\frac{\sigma_{LG}}{kT}}$$

- Temperature
- Ω_L : volume of a H₂O molecule in the liquid (0.8 to 3.4×10^{-29} m⁻³)
- n_0 : number of H₂O molecules per m³ of liquid
- a_0 : distance between H₂O molecules
- D_{H_2O} : diffusion coefficient (1.5×10^{-11} m²/s)
- σ_{LG} : the unknown parameter (0.03-0.13 N/m)

Classical theory of nucleation:

Calculation of surface tension coefficient, σ_{LG} (N/m), from the nucleation pressure P_N

Hirth et al., 1970; Hurwitz and Navon, 1994; Cluzel et al., 2008



(1) Compute J as a function of P_L for a given σ_{LG}

(2) Integrate J over time to obtain the BND, N , for a given $|dP/dt|$

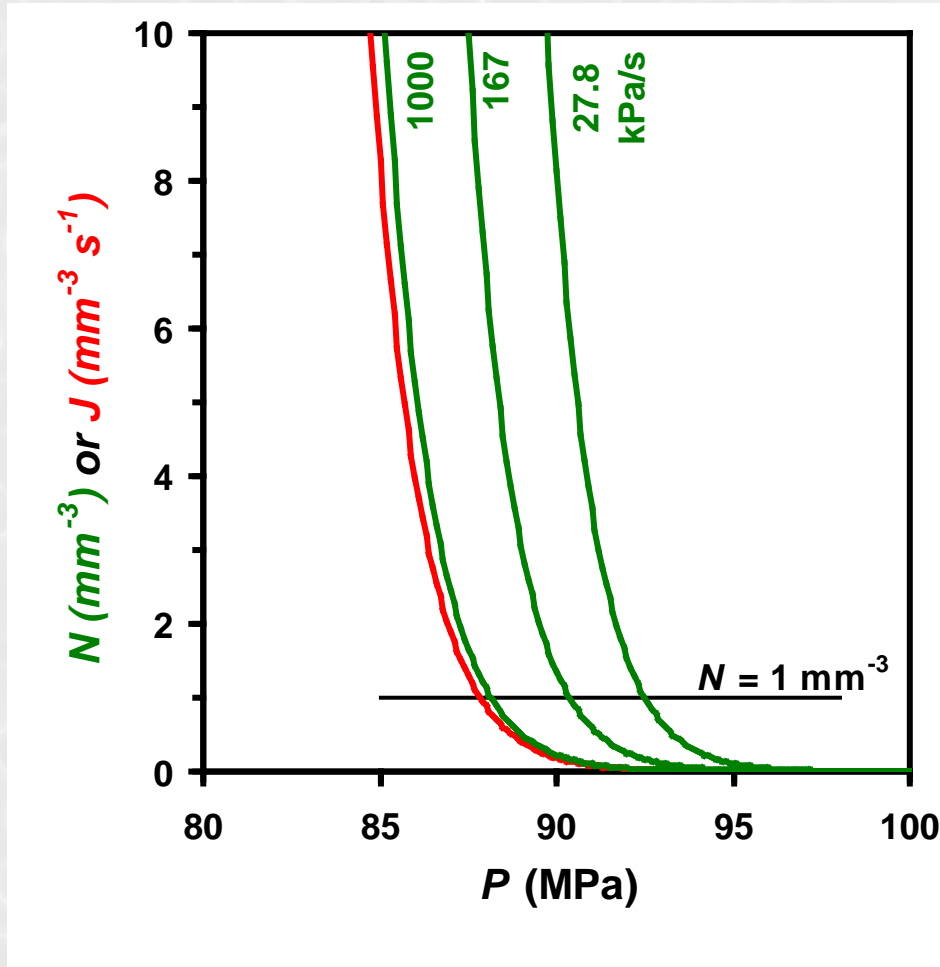
(3) Compute P_N (assuming that nucleation is detected when the BND exceeds 1 mm^{-3})

(4) Adjust σ_{LG} until the P_N computed matches the experimental value

Classical theory of nucleation:

Calculation of surface tension coefficient, σ_{LG} (N/m), from the nucleation pressure P_N

Hirth et al., 1970; Hurwitz and Navon, 1994; Cluzel et al., 2008

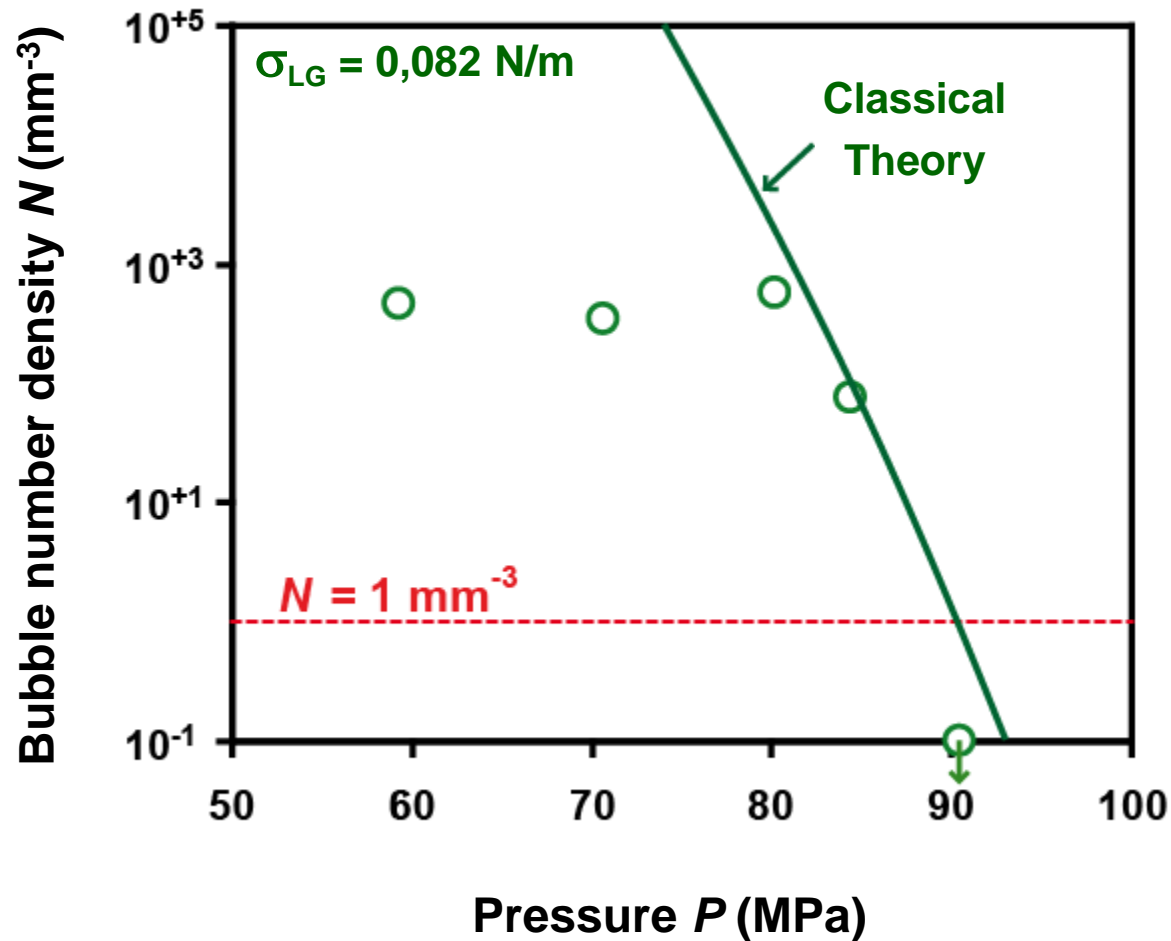


(1) Compute J as a function of P_L for a given σ_{LG}

(2) Integrate J over time to obtain the BND, N , for a given $|dP/dt|$

(3) Compute P_N (assuming that nucleation is detected when the BND exceeds 1 mm^{-3})

(4) Adjust σ_{LG} until the P_N computed matches the experimental value



⇒ We compute $P_N \approx 90 \text{ MPa}$ for $\sigma_{LG} = 0.082 \text{ N/m}$

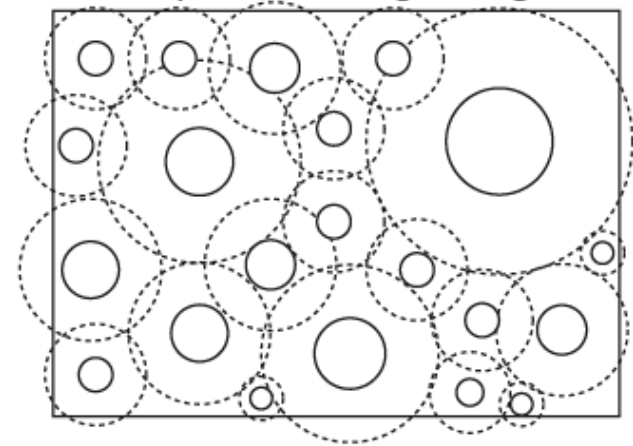
⇒ In good agreement with direct measurement of σ_{LG} : 0.087 N/m (Bagdassarov et al., 2000)

⇒ At some point, the nucleation rate drops...

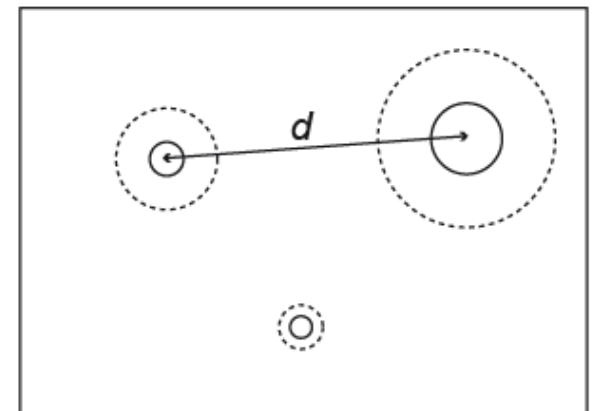
**Importance of the number density of bubbles, N :
diffusion length scale e vs. mean bubble-to-bubble distance d**

**Diffusive bubble
growth dominates:
 N stationary**

Large N : $d \ll 2e$
equilibrium degassing



Small N : $d \gg 2e$
disequilibrium degassing



Nucleation dominates

Competition between nucleation and diffusive growth of bubbles (Toramaru 1995, 2006) :

⇒ numerical simulation of the ascent and vesiculation of magmas ⇒ 2 steps:

(1) a nucleation step of very short duration

(2) a step dominated by diffusive bubble growth, in which BND is stationary = N_{STAT}

$$N_{\text{STAT}} \approx 34 \cdot C_0 \left(\frac{16\pi\gamma_{\text{LG}}^3}{3kTP_{\text{SAT}}^2} \right)^{-2} \left(\frac{\Omega_{\text{L}}P_{\text{SAT}}}{kT} \right)^{-1/4} \left(\frac{kTC_0D_{\text{H2O}}P_{\text{SAT}}^2}{4\gamma_{\text{LG}}^2 |dP/dt|} \right)^{-3/2}$$

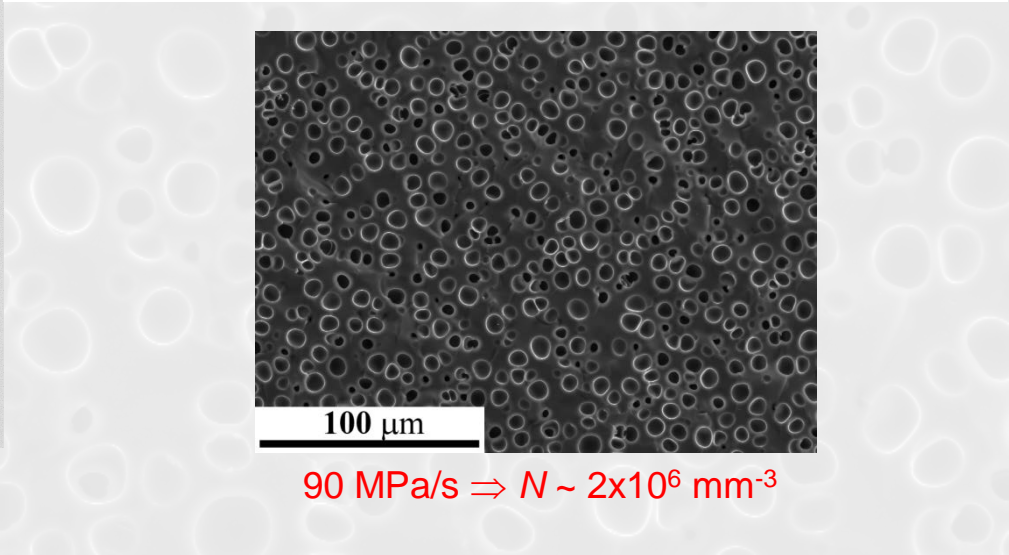
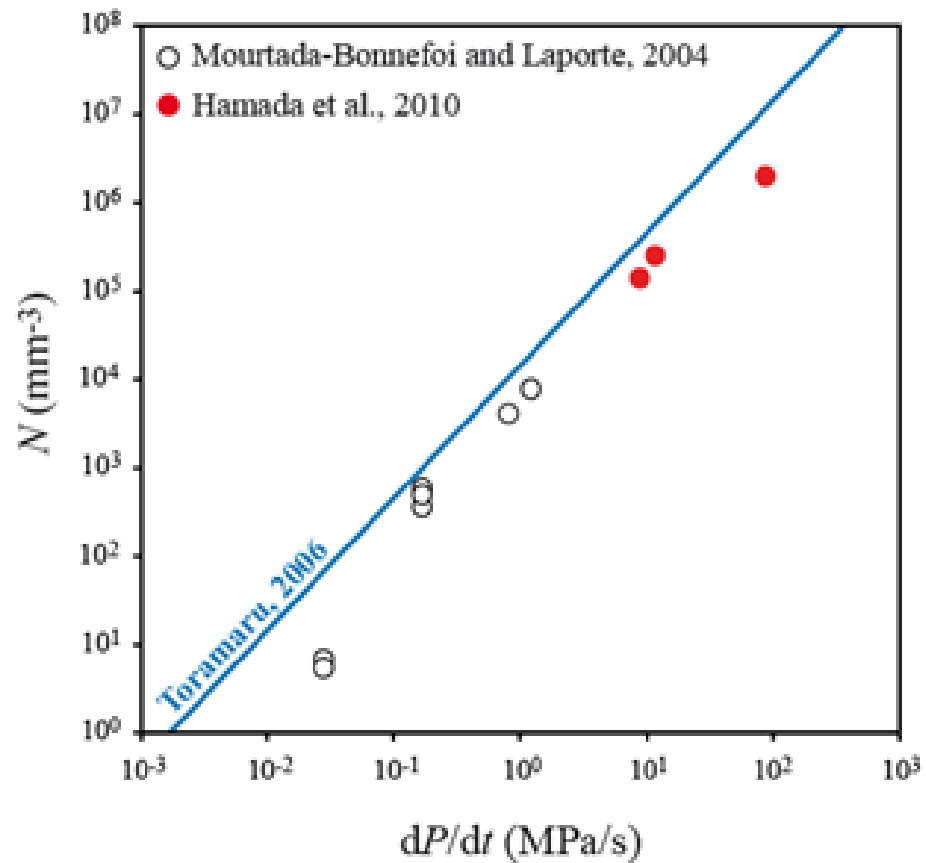
N_{STAT} is strongly sensitive to decompression rate = the Bubble Number Density

Decompression Ratemeter (Toramaru, 2006)



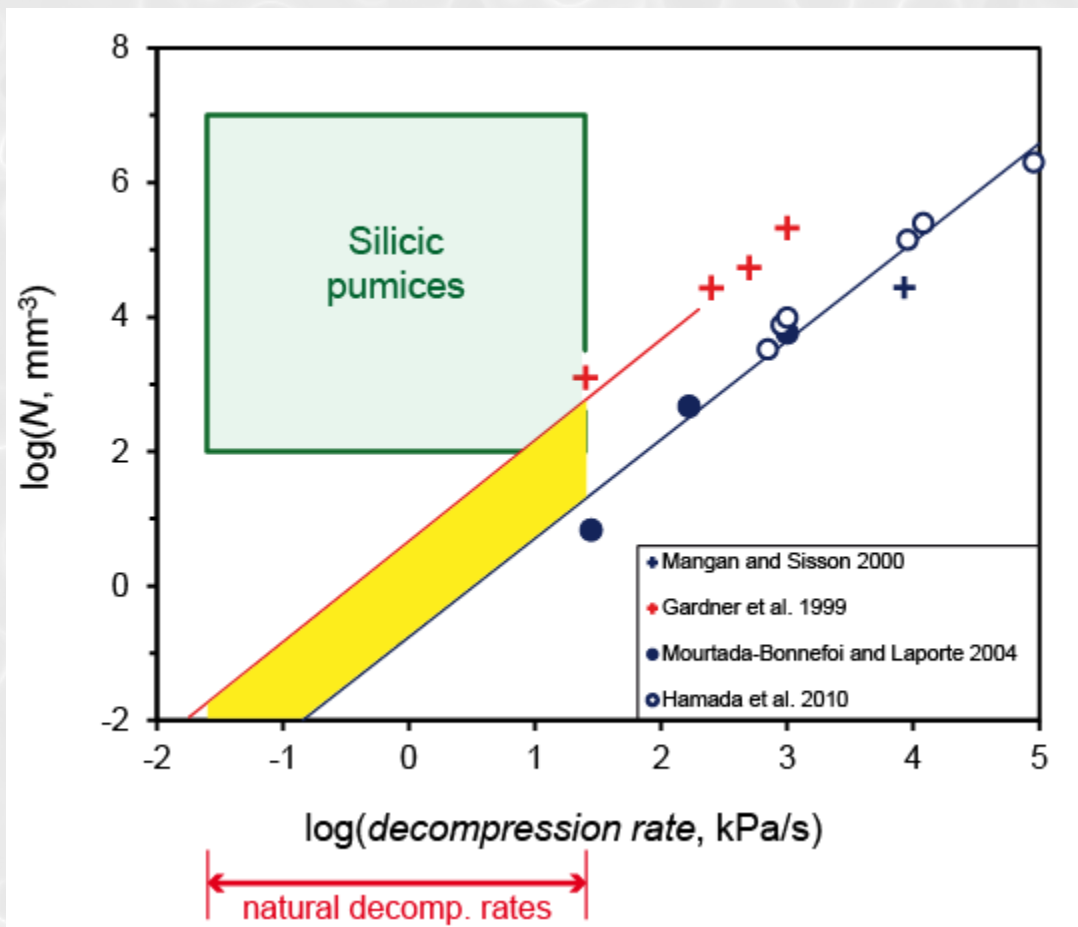
0.5 mm

0.0278 MPa/s $\Rightarrow N \sim 7 \text{ mm}^{-3}$

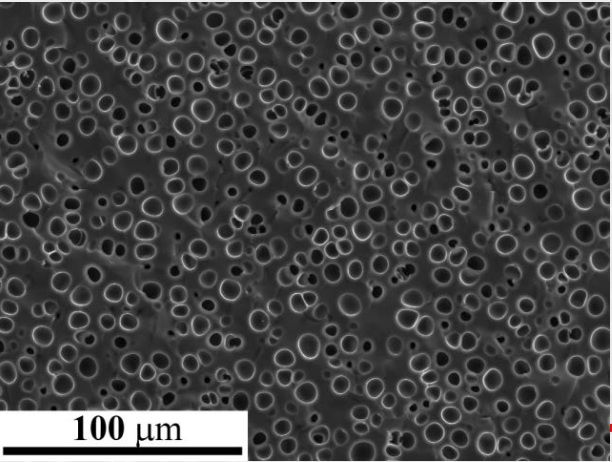


100 μm

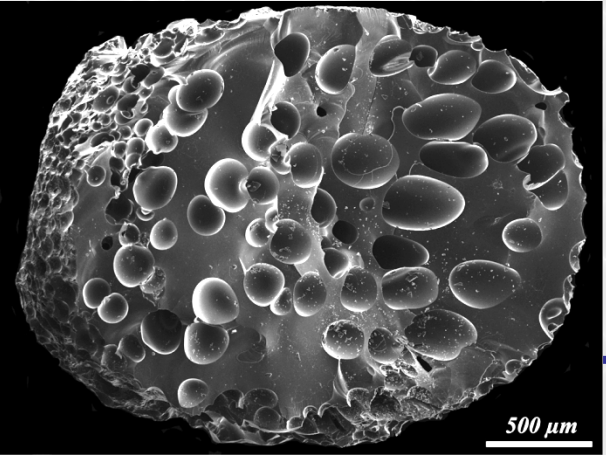
90 MPa/s $\Rightarrow N \sim 2 \times 10^6 \text{ mm}^{-3}$



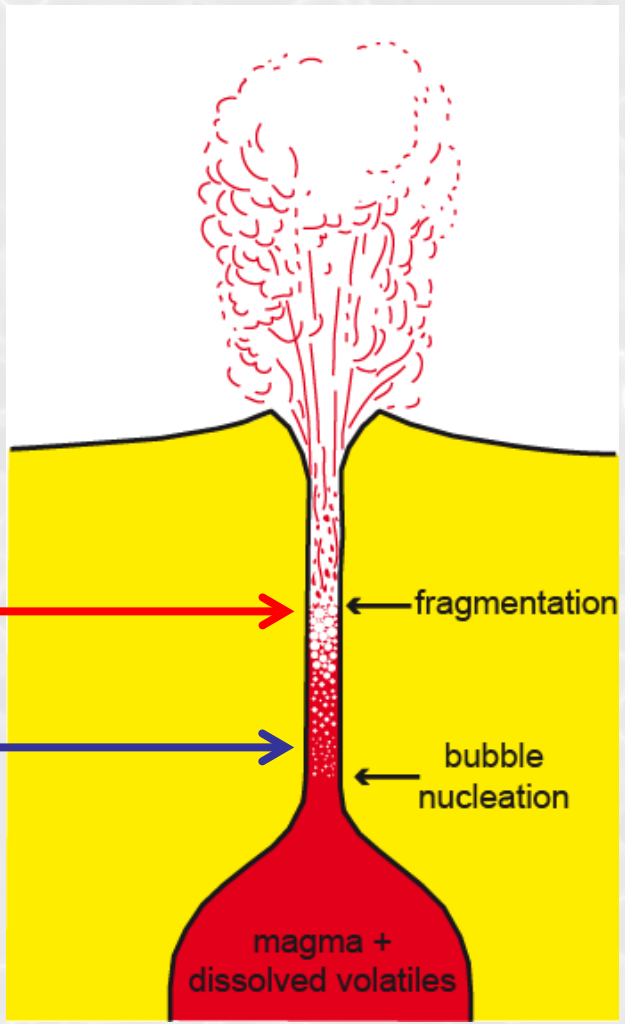
- Application: interpretation of BNDs in natural volcanic pumices
- Bubble number densities in natural pumices are orders of magnitude above extrapolated BNDs: 10^2 - 10^7 mm^{-3} (= 10^{11} to 10^{16} bubbles / m^3).



2nd nucleation event under extreme decompression rates at the fragmentation level ($\geq 10 \text{ MPa/s}$) \Rightarrow BND up to 10^6 mm^{-3} .



Deep nucleation in the conduit at low $|dP/dt| \Rightarrow$ BND $\leq 100 \text{ mm}^{-3}$



Homogeneous bubble nucleation in rhyolitic liquids: Summary

- ❑ Only one nucleation event of short duration marked by a fast increase of bubble number density; then BND is nearly stationary.
- ❑ Homogeneous bubble nucleation strongly delayed ($P_{\text{SAT}} - P_{\text{N}} = 150 \text{ MPa}$)
- ❑ Early stages of nucleation well described by the classical theory.
- ❑ Very strong correlation between bubble number density and decompression rate: **the measurement of bubble number density in natural pumice samples is a potential tool to estimate the ascent rate of magmas.**

I. Introduction: Importance of the kinetics of magma degassing

II. Effect of ascent rate on homogeneous bubble nucleation in the system rhyolite-H₂O

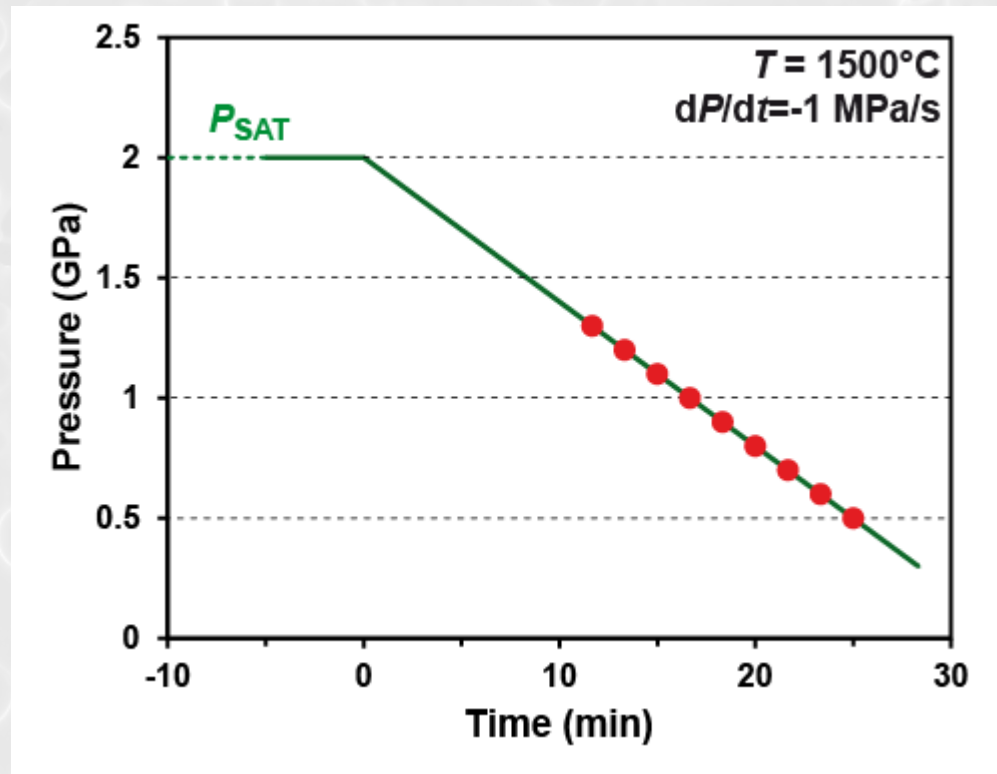
III. Homogeneous bubble nucleation in the system basalt-CO₂

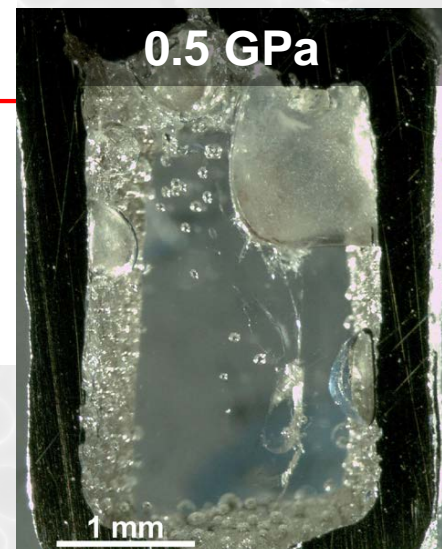
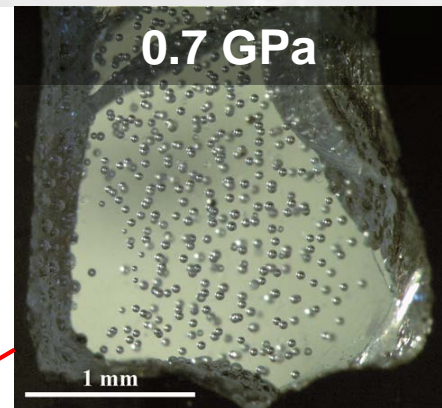
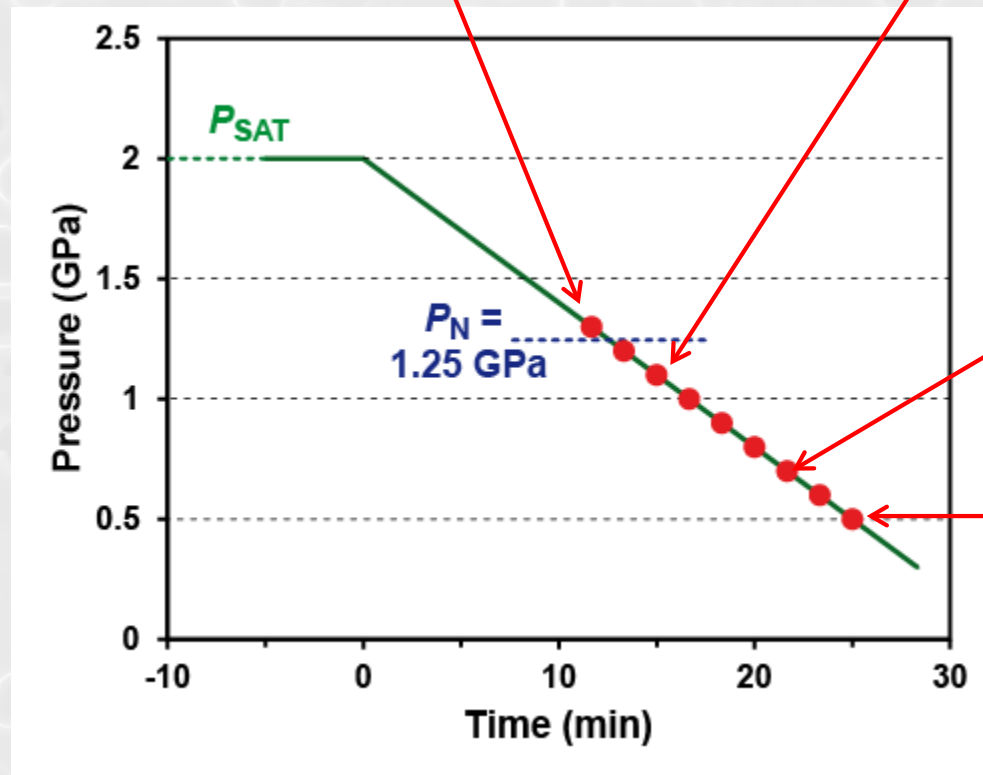
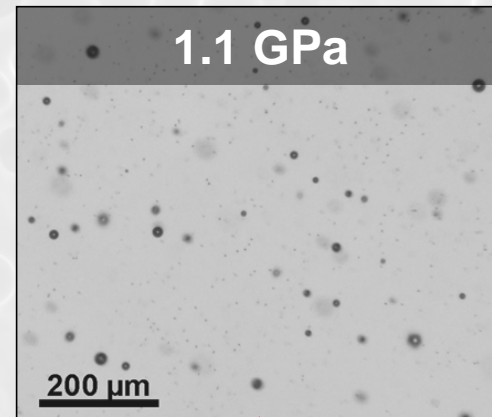
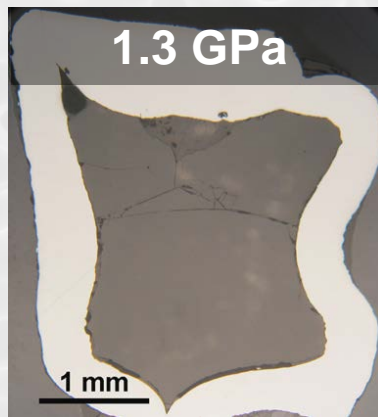
System: synthetic basalt (CMAS-Na) saturated in CO₂ at 2 GPa-1500°C

$C_0 = 1.6$ wt. % CO₂

$|dP/dt| = 1$ MPa/s, with quench pressures down to 0.5 GPa

CMAS-Na (wt %)	
SiO ₂	49.25
Al ₂ O ₃	19.41
MgO	16.40
CaO	12.83
Na ₂ O	2.11

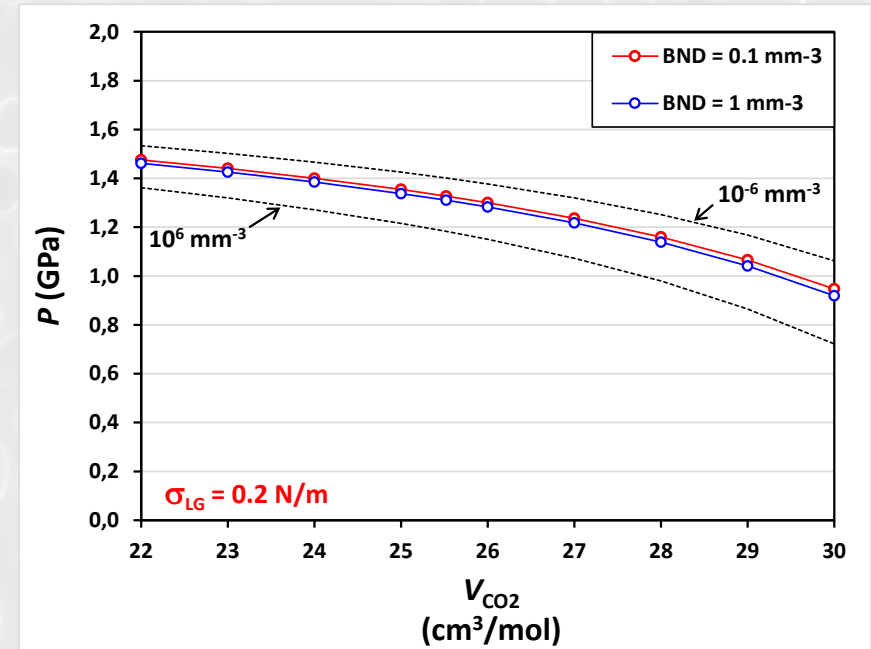




⇒ High supersaturation required for homogeneous bubble nucleation in the system basalt- CO_2 : $\Delta P = 0,75 \text{ GPa}$

Calculation of surface tension coefficient σ_{LG} (N/m) from nucleation pressure ($P_N = 1.25 \pm 0,05$ GPa) using classical nucleation theory

- Temperature: 1773 K; $P_{SAT} = 2$ GPa
- CO_2 solubility at P_{SAT} (1.6 wt %) and CO_2 speciation (% molecular CO_2 ; Guillot & Sator, 2011; Korschak & Keppler, 2014)
- D_{CO_2} : diffusion coefficient (1×10^{-10} m²/s; Guillot & Sator, 2011)
- V_{CO_2} : molar volume of CO_2 in the liquid (23-28 cm³/mol: Liu & Lange, 2003)



P_N decreases from 1.43 GPa (@ 23 cm³/mol) to 1.14 GPa (@ 28 cm³/mol)

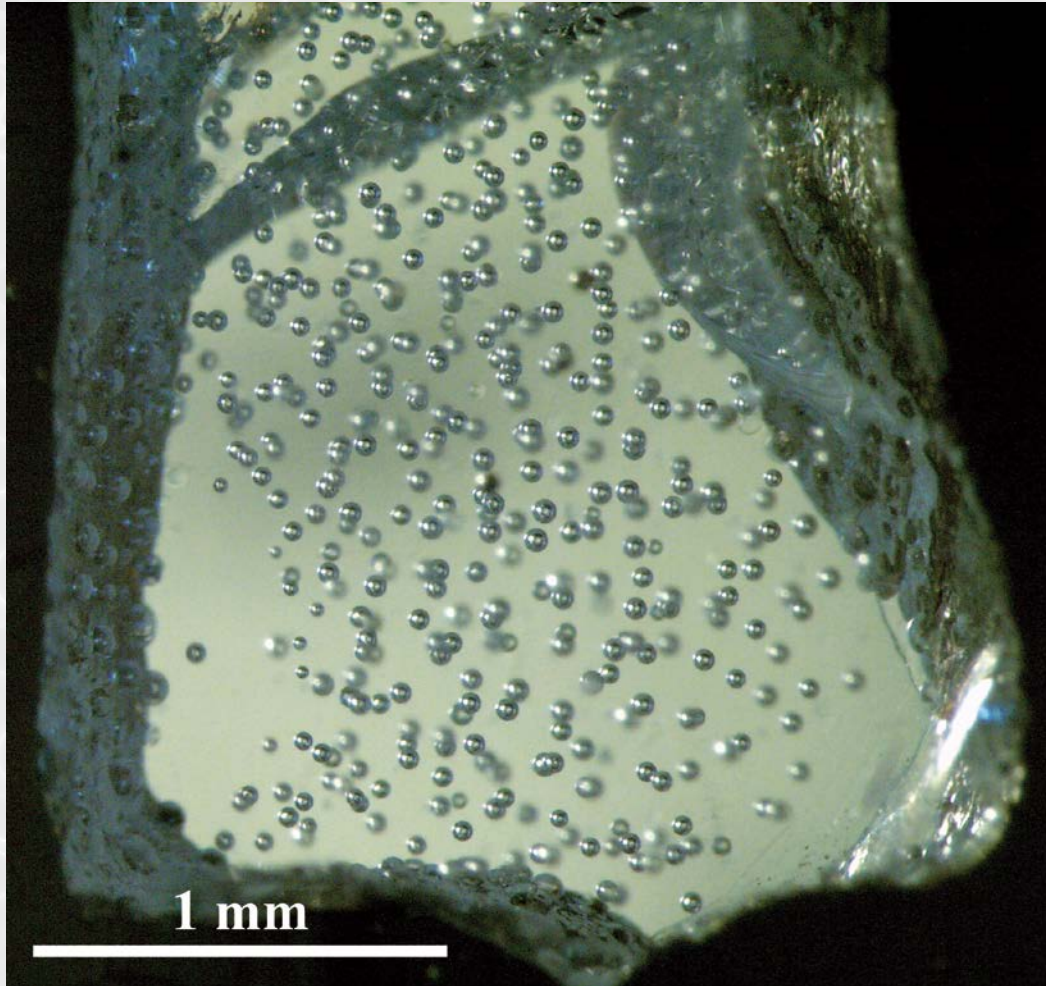
Calculation of surface tension coefficient σ_{LG} (N/m) from nucleation pressure ($P_N = 1.25 \pm 0,05$ GPa) using classical nucleation theory

- Temperature: 1773 K; $P_{SAT} = 2$ GPa
- CO_2 solubility at P_{SAT} (1.6 wt %) and CO_2 speciation (% molecular CO_2 ; Guillot & Sator, 2011; Korschak & Keppler, 2014)
- D_{CO_2} : diffusion coefficient (1×10^{-10} m²/s; Guillot & Sator, 2011)
- V_{CO_2} : molar volume of CO_2 in the liquid (23-28 cm³/mol: Liu & Lange, 2003)

Taking into account uncertainties on V_{CO_2} and P_N , we obtain:

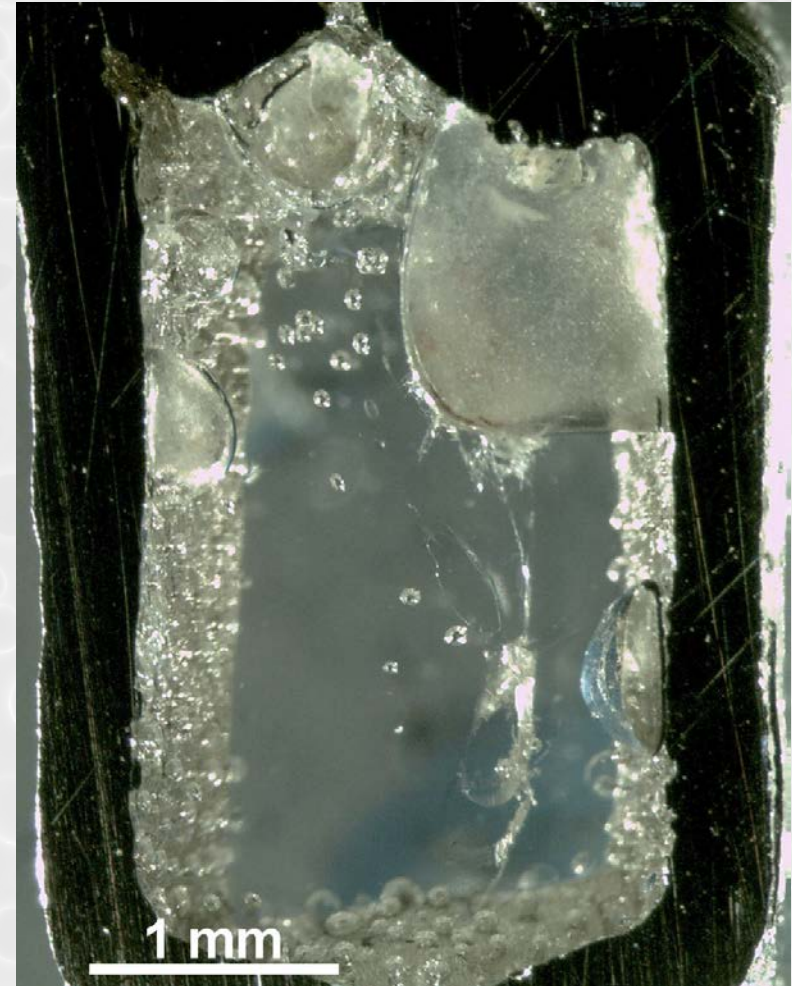
$$\sigma_{LG} = 0.21 \pm 0.03 \text{ N/m}$$

$P = 0.7 \text{ GPa}$



Homogeneous nucleation texture: bubbles of uniform size (30 to 60 μm) with a uniform spatial distribution

$P = 0.5 \text{ GPa}$



Bubble accumulation and coalescence at the top due to buoyancy-driven bubble rise

Hadamard-Rybcynski law: velocity V of a bubble of radius R in a liquid of viscosity μ
(Bottinga and Javoy, 1990):

$$V = \frac{(\rho_M - \rho_G)R^2 g}{3\mu}$$

Distance traveled by a bubble
between $P = 0.7$ GPa and $P =$
 0.5 GPa ($\Delta t = 200$ s)

Bubble diameter (μm)	Distance (mm)
10	0.08
30	0.74
60	2.94
100	8.18

$$\rho_M = 2600 \text{ kg/m}^3; \rho_G = 1400 \text{ kg/m}^3; \mu = 0.24 \text{ Pa}\cdot\text{s}; g = 9.81 \text{ m/s}^2$$

Application to natural systems:

Bubble diameter (cm)	Velocity (m/s)
0.1	1.5×10^{-4}
1	1.5×10^{-2}
10	1.5

In basalts, bubbles rise at velocities that are not negligible in comparison to magma ascent rates (0.1-1 m/s for MORBs), specially for diameters > 1 cm:

open-system degassing...

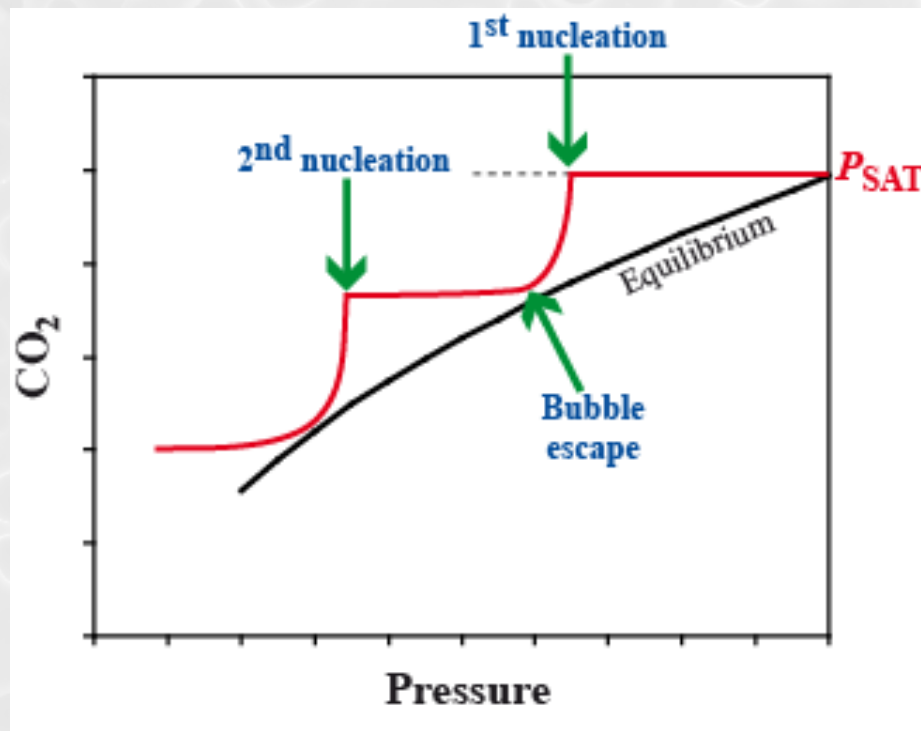
$$\rho_M = 2800 \text{ kg/m}^3; \rho_G = 1000 \text{ kg/m}^3; \mu = 10 \text{ Pa}\cdot\text{s}; g = 9.81 \text{ m/s}^2$$

Homogeneous bubble nucleation in the system basalt-CO₂: Summary

- ❑ Bubble nucleation in the system basalt-CO₂ is strongly delayed ($\Delta P = 0.75$ GPa) due to high surface tension coefficient (0.21 ± 0.03 N/m).
- ❑ Vesiculation of basaltic magmas is affected by bubble buoyancy even at the early stages.

❑ After bubble escape, CO₂ supersaturation will increase and may lead to a second nucleation event.

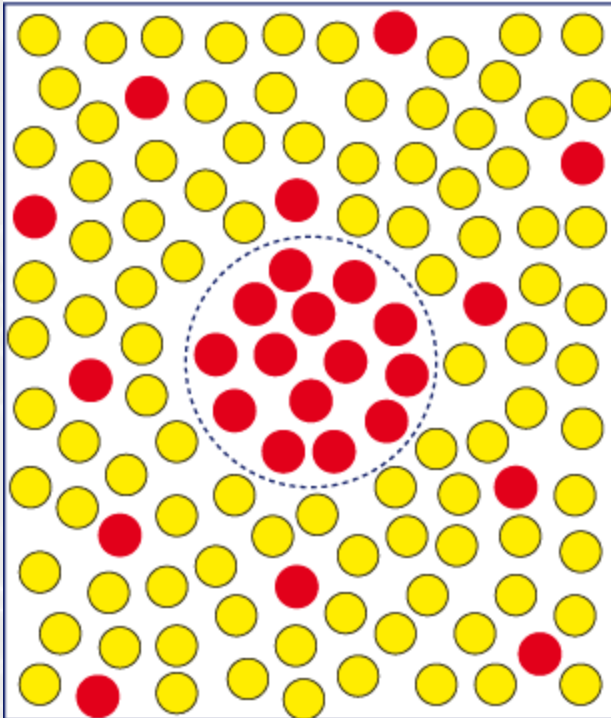
❑ Correlation between BND and ascent rate at the nucleation stage presumably erased by bubble rise.



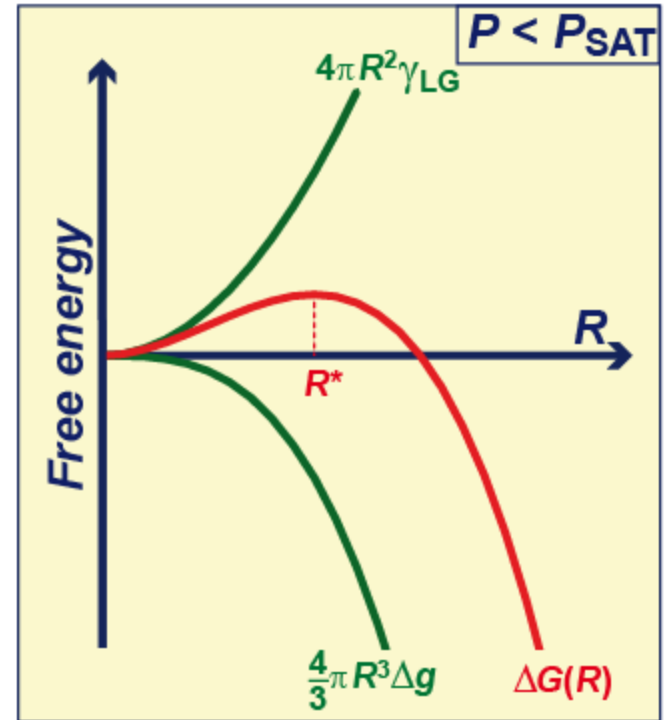
Some research perspectives

- ❑ Only very few experimental studies on basalt degassing (Le Gall, 2015): need for more work in this direction.
- ❑ Theoretical and experimental studies on bubble nucleation and growth in silicate liquids with two or more volatile components (H_2O , CO_2 , SO_2 , noble gases, etc.):
 - ❑ models of bubble nucleation in the presence of two volatiles.
 - ❑ diffusive fractionation of volatile components during bubble growth.

Homogeneous bubble nucleation: Classical theory



Bubble nucleus of radius R



Δg : free energy of vaporization (J/m^3)
 γ_{LG} : coefficient of interfacial energy (J/m^2)
(γ_{LG} is equivalent to surface tension)

Classical theory of nucleation:

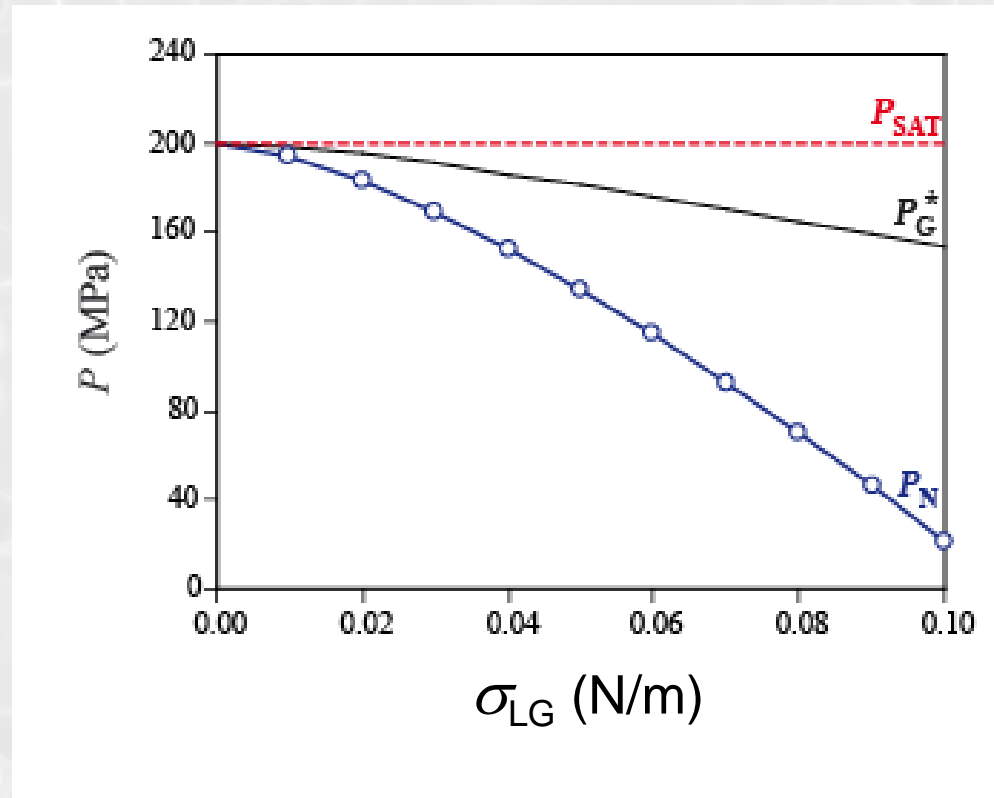
Calculation of surface tension coefficient, σ_{LG} (N/m), from the nucleation pressure P_N

Hirth et al., 1970; Hurwitz and Navon, 1994; Cluzel et al., 2008

$$P_{SAT} = 200 \text{ MPa}$$

$$T = 800^\circ\text{C}$$

$$|dP/dt| = 1 \text{ kPa/s}$$

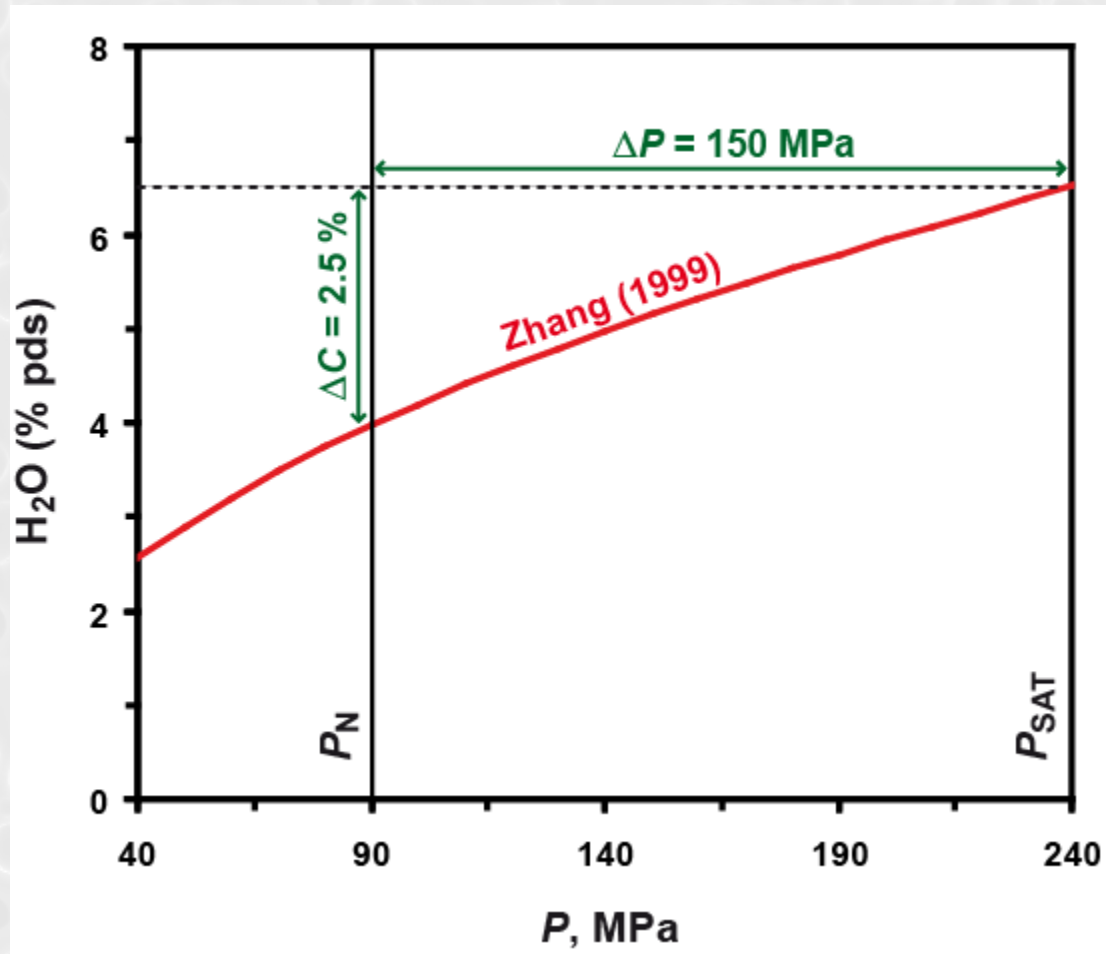




- Externally-heated pressure vessel for automatic decompression
- P and T up to 200-300 MPa, 800-900°C
- Possible to simulate the ascent of silicic magmas in volcanic conduits: 1 mm/s to 10 m/s, that is 0.025 kPa/s to 250 kPa/s (\approx 1 bar/hr to 2.5 bar/s)



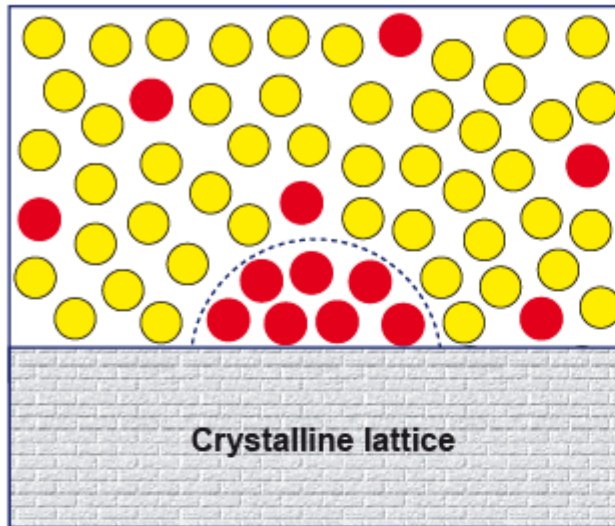
- Internally-heated pressure vessel for automatic decompression:
- P and T up to 1 GPa-1450°C \Rightarrow Ascent and degassing of basaltic magmas



Nucleation occurs when the liquid contains 2.5 wt. % H₂O in excess of the solubility value: very large degree of volatile supersaturation ΔC

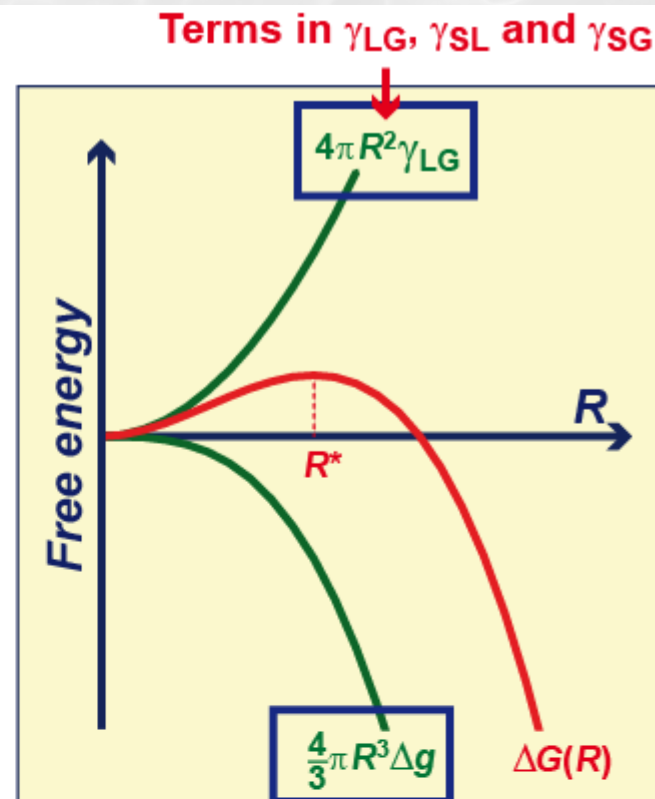
**III. The effect of crystals:
Heterogeneous bubble nucleation
in silicic melts**

□ Nucleation on a substrate (« heterogeneous ») easier than in the liquid (« homogeneous »): Bubble nucleation on **Fe-Ti oxides** requires a supersaturation pressure of only 5-10 MPa (Hurwitz and Navon, 1994)



Bubble nucleus on a crystal face

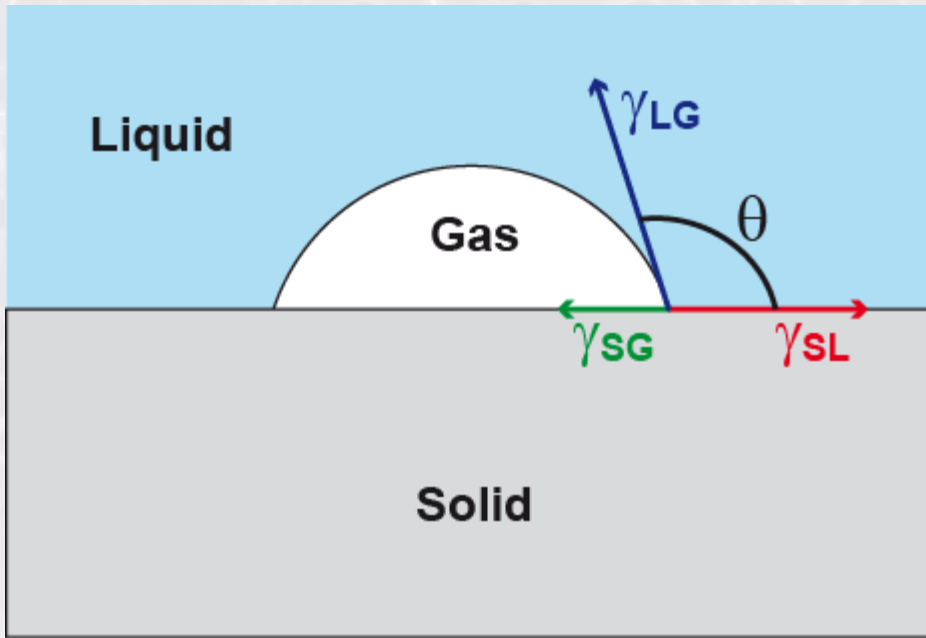
Low γ_{SG} = good substrate



❑ Nucleation on a substrate (« heterogeneous ») easier than in the liquid (« homogeneous »): Bubble nucleation on **Fe-Ti oxides** requires a supersaturation pressure of only 5-10 MPa (Hurwitz and Navon, 1994)

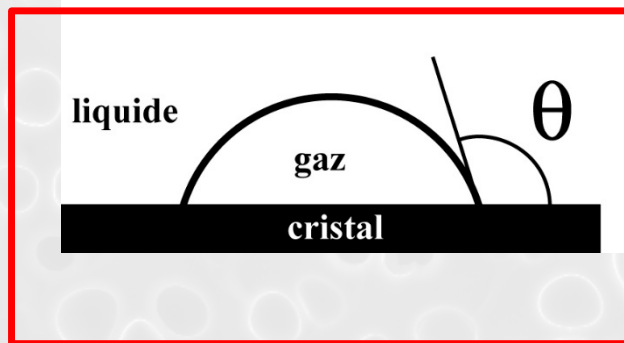
❑ What are the good mineral substrates for heterogeneous bubble nucleation?

❑ What are the parameters controlling the number density of bubbles in the case of heterogeneous nucleation?



Theory: contact angle of a nucleus on a crystal face

$$\gamma_{SG} - \gamma_{SL} = \gamma_{LG} \cdot \cos \theta$$



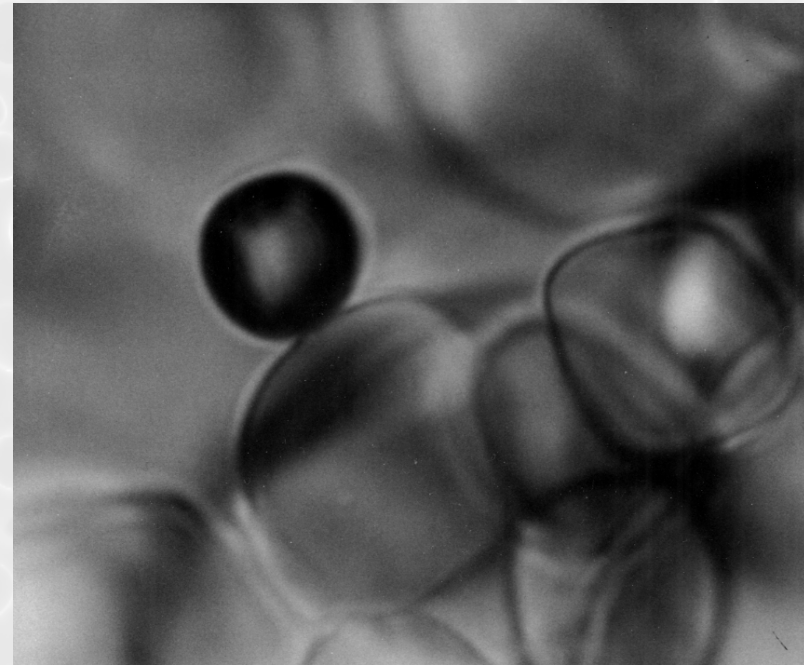
$\theta \gg 90^\circ \Rightarrow \gamma_{SG}$ small relative to $\gamma_{SL} \Rightarrow$ good for bubble nucleation

$$\Delta P_{\text{Heterogeneous}} = \sqrt{\phi} \cdot \Delta P_{\text{Homogeneous}}$$

$$\phi = \frac{(2 - \cos \theta)(1 + \cos \theta)^2}{4}$$

Exercise no. 3

Compute the nucleation pressure for a rhyolitic liquid saturated in water at $P = 240$ MPa and $T = 800^\circ\text{C}$ in the presence of quartz ($\theta = 24^\circ$; photo) or in the presence of magnetite ($\theta = 150^\circ$). The nucleation pressure in the absence of crystals is equal to $P_N = 90$ MPa.



Water bubble on quartz

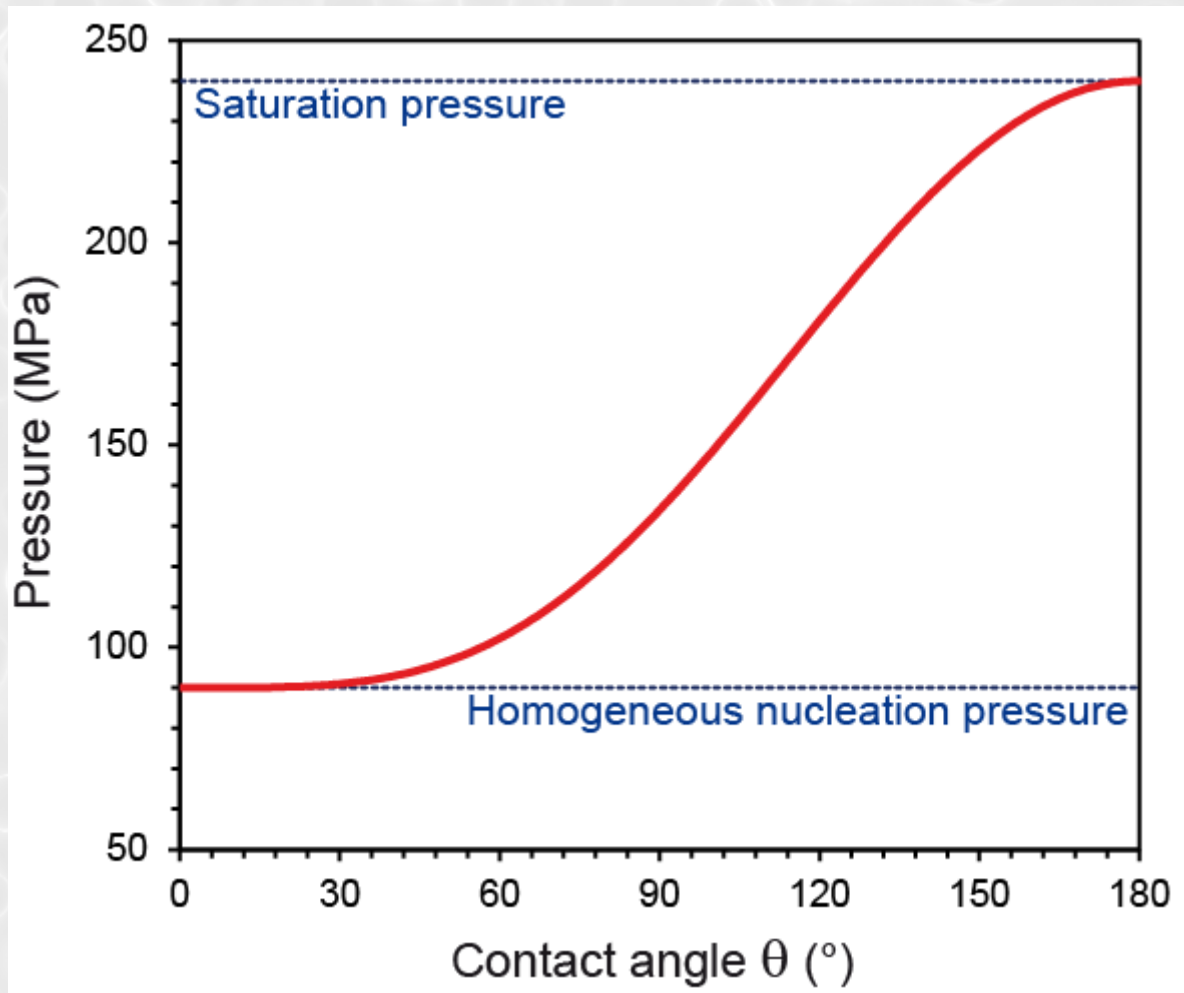
$$\Rightarrow \Delta P_{\text{homogeneous}} = P_{\text{SAT}} - P_{\text{N}} = 240 - 90 = 150 \text{ MPa}$$

\Rightarrow Case of quartz:

- $\theta = 24^\circ \Rightarrow \sqrt{\phi} = 0,997$
- $\Delta P_{\text{quartz}} = 0,997 \times 150 = 149,6 \text{ MPa}$
- **the nucleation pressure on quartz is 90,4 MPa:** almost equal to the pressure of homogeneous nucleation!

\Rightarrow Case of magnetite:

- $\theta = 150^\circ \Rightarrow \sqrt{\phi} = 0,113$
- $\Delta P_{\text{magnetite}} = 0,113 \times 150 = 17 \text{ MPa}$
- **The nucleation pressure on magnetite is 223 MPa:** just slightly less than the saturation pressure.



Strong reduction of the nucleation pressure only for $\theta \gg 90^\circ$

$$\Delta P_{\text{Heterogeneous}} = \sqrt{\phi} \cdot \Delta P_{\text{Homogeneous}}$$

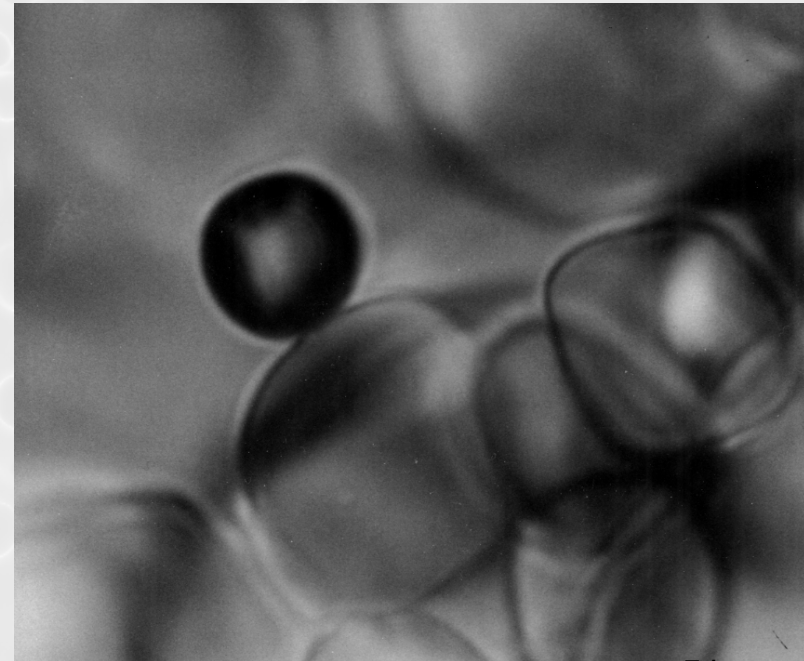
$$\phi = \frac{(2 - \cos \theta)(1 + \cos \theta)^2}{4}$$

For most species: $\theta \ll 90^\circ$

For instance quartz: $\theta = 24^\circ \rightarrow \sqrt{\phi} = 0,997$

⇒ During magma ascent, heterogeneous bubble nucleation on quartz would occur just a few MPa before homogeneous nucleation.

⇒ The same holds for plagioclase (Mangan and Sisson, 2005; Gardner, 2007)



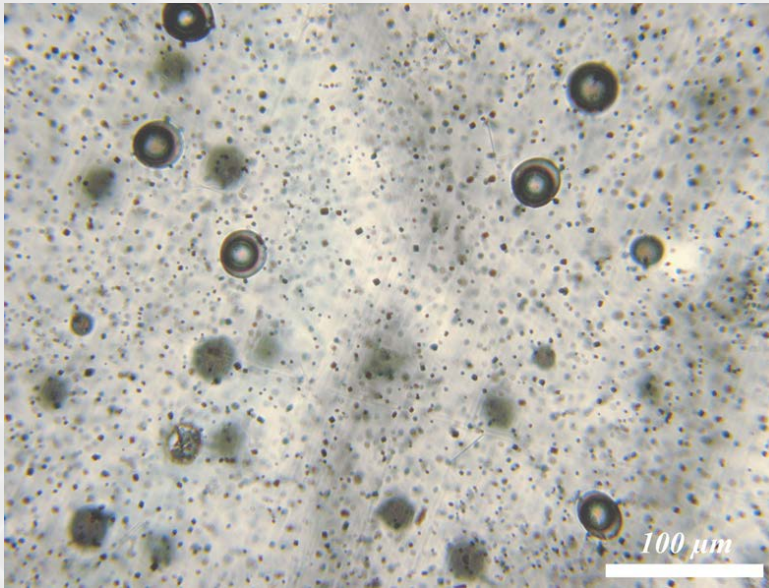
Water bubble on quartz

$$\Delta P_{\text{Heterogeneous}} = \sqrt{\phi} \cdot \Delta P_{\text{Homogeneous}}$$

$$\phi = \frac{(2 - \cos \theta)(1 + \cos \theta)^2}{4}$$

- ⇒ Only magnetite has a contact angle $\theta \gg 90^\circ$: from 140° (Cluzel, 2007) to 160° (Hurwitz and Navon, 1994)
- ⇒ Very low ΔP in the presence of magnetite: down to 5-10 MPa (Hurwitz and Navon, 1994; Gardner and Denis, 2004...)
- ⇒ Contact angles θ not known for many mineral species...

□ Case 1: large number of crystals N_{XL}



⇒ System rhyolite-magnetite- H_2O
saturated with water at 200 MPa-825°C
(Cluzel, 2007)

⇒ Heterogeneous bubble nucleation at
 $\Delta P = 30\text{-}40$ MPa

⇒ 2800 bulles/ mm^3 versus $N_{XL} = 2 \cdot 10^5$
magnetites/ mm^3 ⇒ Bubble number
density is not controlled by crystal number
density.

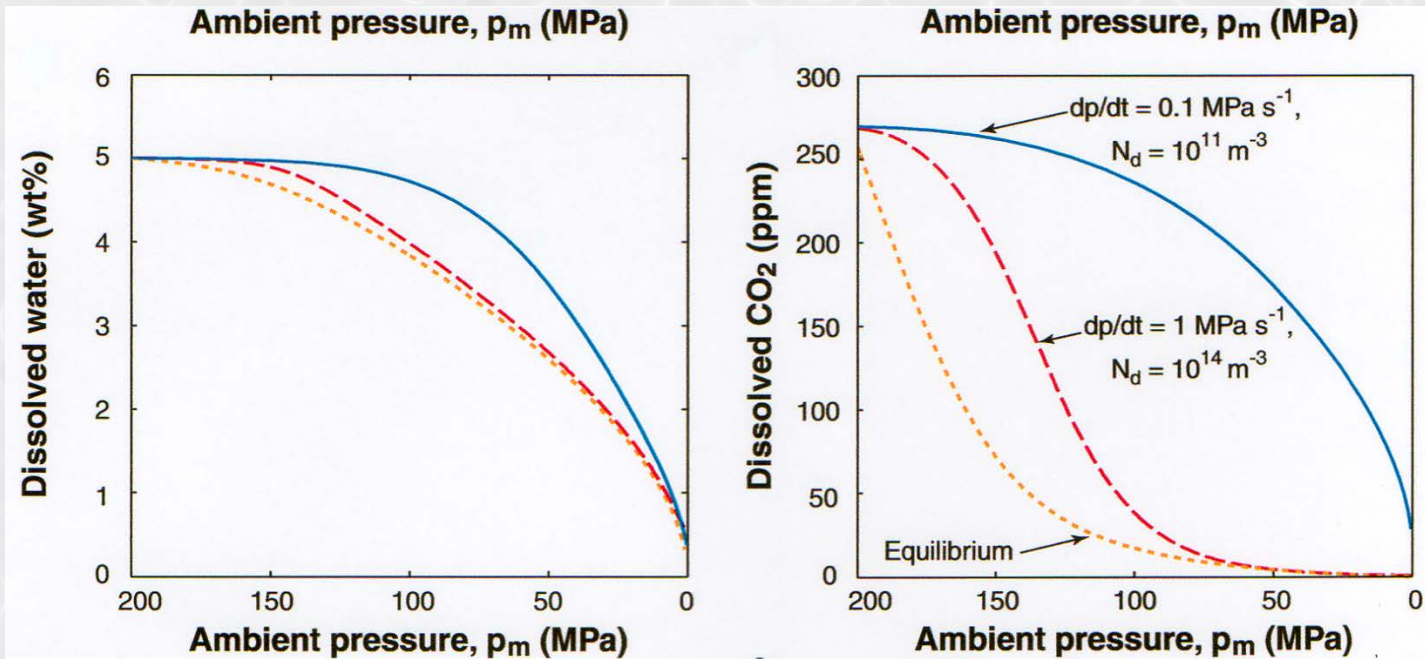
Run ATHO#14: $P_L = 100$ MPa

Heterogeneous bubble nucleation in rhyolitic liquids: Summary

- ❑ Possible to have deep bubble nucleation (at low ΔP) on magnetite. For many other minerals, heterogeneous nucleation requires a large ΔP .
- ❑ Importance of deep nucleation depends on the abundance of magnetite microphenocrysts at the pre-eruptive stage:
 - ⇒ 1-100 mm⁻³ (Cashman, 1988; Gualda and Rivers, 2006)?
- ❑ If N_{XL} is large, same kinetics as for homogeneous bubble nucleation with a strong correlation between bubble number density and decompression rate:
BND in natural pumice samples can be used as a decompression ratemeter.
- ❑ Need to better know the abundance of crystals at the onset of magma ascent (that is, before degassing-induced crystallization).

Diffusive fractionation of H₂O and CO₂ in ascending rhyolitic melt

$$D_{\text{H}_2\text{O}} \approx 10^{-11} \text{ m}^2/\text{s} \approx 10 \cdot D_{\text{CO}_2}$$



Initial state:

$T = 850^\circ\text{C}$

$P_{\text{SAT}} = 200 \text{ MPa}$

$\text{H}_2\text{O} = 5 \text{ wt. \%}$

$\text{CO}_2 = 268 \text{ ppm}$

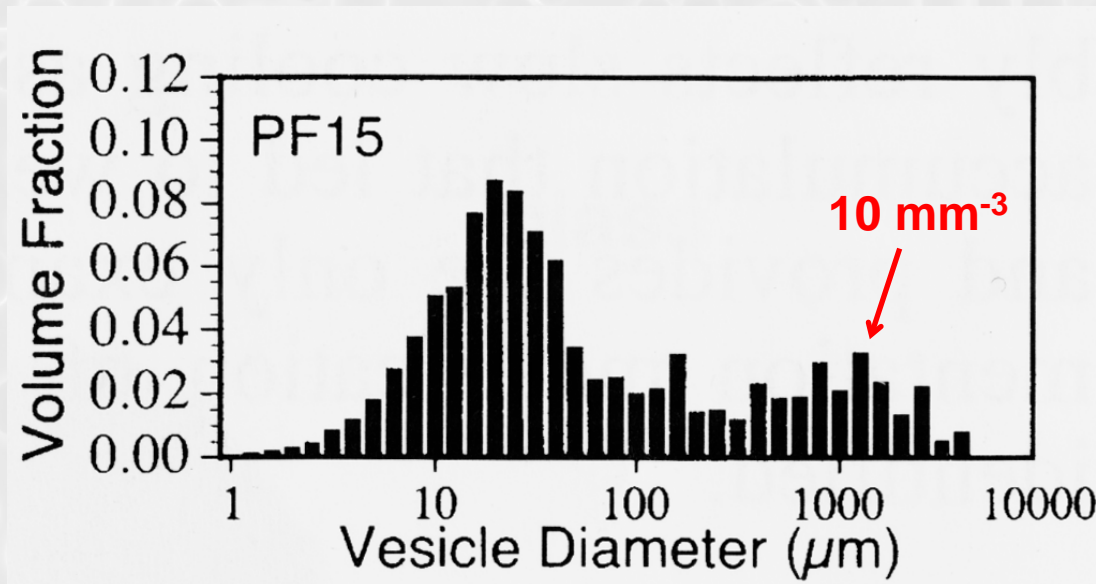
Evolution of H₂O (left) and CO₂ (right) dissolved into the melt with decreasing P (from Gonnermann and Manga, 2007):

⇒ both CO₂ and H₂O in the liquid (blue curves) are above their equilibrium values (orange)

⇒ the liquid is strongly enriched in CO₂ (the slow diffusing species) relative to H₂O.

Diffusive fractionation between slow and fast diffusing volatile species
= a tool to estimate the time-scale of degassing

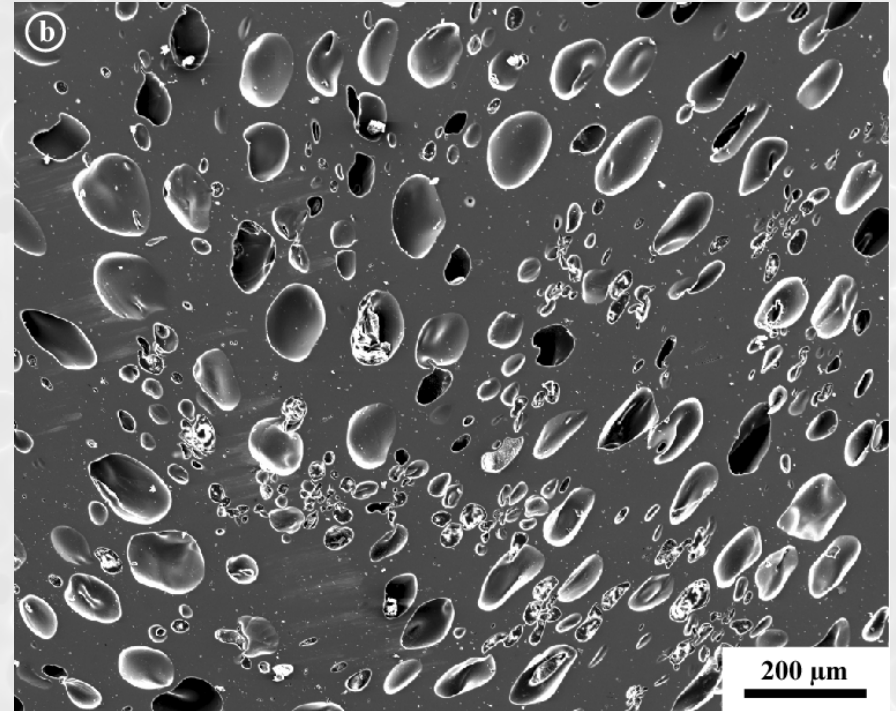
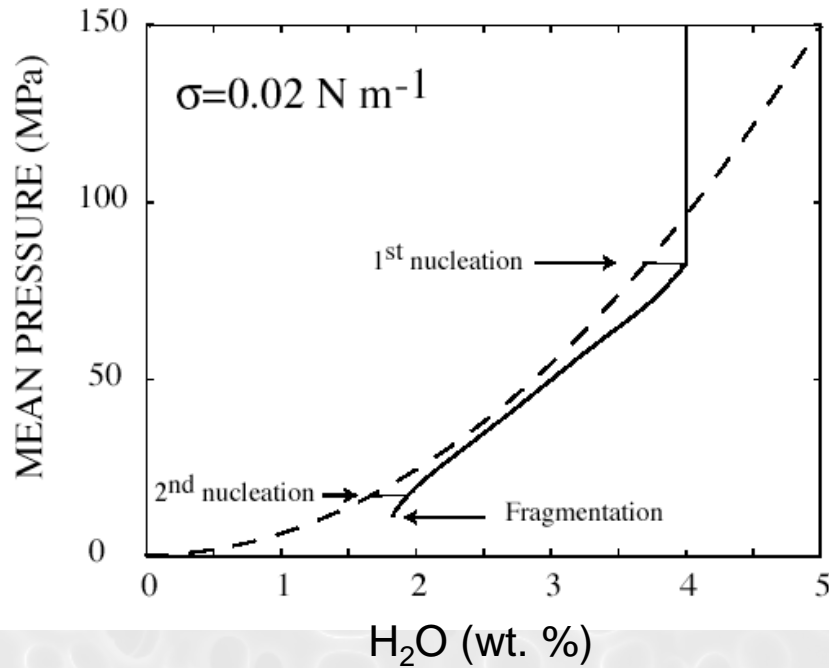
	FAST	SLOW
Major volatiles	H ₂ O	CO ₂
	H ₂ O	S
	H ₂ O	F, Cl
Noble gases	He	Ar
Light elements	Li	B
Isotopes	⁶ Li	⁷ Li
	¹² C	¹³ C



Bubble size distribution in a pumice from Mount Mazama (Crater Lake), Oregon (Klug et al., 2002):

⇒ total bubble number density $\approx 10^7 \text{ mm}^{-3}$ (mostly $< 100 \text{ } \mu\text{m}$)

⇒ number density of large bubbles ($300\text{-}4000 \text{ } \mu\text{m}$) $\approx 10 \text{ mm}^{-3}$



Massol and Koyaguchi (2005) :

- ⇒ Numerical simulations of ascent and vesiculation of magmas
- ⇒ Decompression rates $> 10 \text{ MPa/s}$ close to the fragmentation level
- ⇒ Increase of the degree of water supersaturation at low $P \Rightarrow 2^{\text{nd}}$ nucleation

Cluzel (PhD 2007) :

- ⇒ System rhyolite-magnetite-H₂O with $P_{\text{SAT}} = 200 \text{ MPa}$ and $T = 825^{\circ}\text{C}$
- ⇒ Textural record of a 2nd nucleation event in the run quenched at 40.2 MPa