

# Introduction to X-ray Emission spectroscopy (XES, RXES, RIXS, IXS)

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Some acronyms for photon spectroscopy used in literature

XAS – x-ray absorption spectroscopy XAFS – x-ray absorption fine structure XANES – x-ray absorption near edge structure NEXAFS – near edge x-ray absorption fine structure EXAFS – extended x-ray absorption fine structure AXAFS – atomic x-ray absorption fine structure SEXAFS – surface extended x-ray absorption fine structure DEXAFS – dispersive extended x-ray absorption fine structure

XES – x-ray emission spectroscopy RXES – resonant x-ray emission spectroscopy IXS – inelastic x-ray scattering RIXS – resonant inelastic x-ray scattering NRIXS or NIXS – non-resonant inelastic x-ray scattering NIXS - nuclear inelastic scattering XRS – x-ray Raman scattering (N,R)XRS – (non-)resonant x-ray Raman scattering

Not all acronyms actually distinguish different processes...

## X-ray core level configurations and transitions

Absorption



## Why x-ray spectroscopy?





Moseley's law

$$\sqrt{\frac{1}{\lambda}} = k_1^{"}(Z - k_2^{"})$$

 $K\alpha$  and  $K\beta$  lines



X-ray lines depend on atomic charge Z and not atomic mass A!



#### X-ray spectroscopy on Mars



Curium (Cm) decays radioactively emitting  $\alpha$ particles and  $\gamma$ -rays. They excite the atoms in the rocks on Mars and the resulting fluorescence spectrum is recorded.

MER-A Spirit APXS X-Ray

The fluorescence spectrum gives information about elemental composition. For a hydrogen-like atom Z with screening s:

$$\Delta E = 13.6(Z-s)^2 \left(\frac{1}{n_i^2} - \frac{1}{n_f^2}\right)$$





One-electron diagrams for X-ray absorption and (photo)emission.

## **Transition schemes**

Two ways of describing the same process.



Some examples for core-to-core (c2c, ctc) X-ray emission lines

Study the oxidation states in Sulfur



## The Sulfur K-edge in Minerals



Study the oxidation states in Sulfur



## The Klpha fluorescence lines



23'06

2304

2308

23'10

Energy (eV)

2306

23'08

23'10

2312

magnitude as compared to XANES.

## Why is K $\alpha$ emission chemically sensitive?

Radial wavefunction



The 3p electrons contribute to the effective nuclear charge experienced by the 2p electrons.

Screening gives rise to chemical sensitivity.

J. C. Slater. *Phys. Rev.*, 36:57 – 64, (1930)

## Many body diagram to explain energy shift



Total energy diagram assuming that the 1s shell is not affected by the screening by the valence electrons. The binding energy of a 2p electron increases when removing valence electrons

## Calculate S K $\!\alpha$ shift due to screening



Atomic orbitals  $\rightarrow$  Shift exaggerated

#### S 2p XPS and K $\alpha$ XES



2308

23'10

Energy (eV)

2308

2306

2312

2310

23'06

2304

In both cases, the chemical shift arises from changes of nuclear screening.

## Summary S XAS-XES



Quantitative analysis in heterogeneous compounds possible.

Analytical Chemistry (2009) 81 6516

## The K $\beta$ lines in 3d transition metals

## The K fluorescence lines in 3d transition metals



#### K $\beta$ spectroscopy in 1959

JOURNAL OF THE PHYSICAL SOCIETY OF JAPAN, Vol. 14, No. 12, DECEMBER 1959

## The X-ray Non-diagram Lines $K\beta'$ of Some Compounds of the Iron Group

By Kenjiro TSUTSUMI

Department of Physics, Faculty of Science, Osaka University

(Received August 1, 1959)





#### Multiplets and core holes



XES measures the electron-electron interactions in the final state!

Multiplets and core holes



XES measures the electron-electron interactions in the final state! The strong (3p,3d) exchange interaction splits the final states into <sup>5</sup>P and <sup>7</sup>P.

## Spin-selectivity in the K $\beta$ line



## Multi-electron excitation in the Mn K $\beta$ line



Spin flip in 3d shell induced by the strong (3p,3d) interaction. This can be referred to as "multi-electron" transition because more than one electron changes its quantum numbers. The selection rules for the total spin are maintained (<sup>5,7</sup>P are final states).

Spin-selectivity in the K $\beta$  line



## The exchange interaction

The K fluorescence lines in 3d transition metals are very sensitive to the spin in the valence shell. This holds for K $\beta$  and K $\alpha$  but the effect is 2-3 weaker for K $\alpha$  (see slide with Slater integrals in lecture 12/02/2019). As the spin changes with a change of oxidation state, the lines are sensitive to the oxidation state.



## Chemical sensitivity of K $\beta$ Emission

Screening effect very small (unlike Sulfur – see below). (3p,3d) interactions are dominating.







## $\ensuremath{\mathsf{K}\beta}\xspace$ XES and 3p XPS



Hamburg university, 1997

## $\ensuremath{\mathsf{K}\beta}$ XES and 3p XPS



Experiments on free metal atoms confirm the interpretation in terms of intra-atomic interactions



A. von dem Borne, PhD thesis[v9] [eV] Binding Energy [eV] 1997

## Effect of covalency on the K $\beta$ line in 3d transition metals





Covalency can be considered by

- Scaling of the electron-electron interaction: Empirically or using DFT (see Pollock et al. JACS 136 (2014) 9453-9463)
- Configuration interaction calculation

Glatzel and Bergmann Cord. Chem. Rev. 249 (2005) 65-95

 $K\beta$  Emission in the Charge Transfer Model



**Ground State** 

## Term dependent lifetime broadening.



In order to analyze fine details of the K fluorescence lines in 3d TM, the final state lifetime has to be calculated



## $K\beta$ lines in Mn compounds



Non-resonant Kβ XES in earth science (Badro et al.), biology (Bergmann et al.), materials science (Rueff et al.), Ultra-fast spin transitions (Vanko et al.) Mn-Mg<sub>k</sub> complexes in GaN

## Magnetic anisotropy (SQUID)





# Functional impurities in wide-gap semiconductors: spin/charge control

Mn in GaN as active center for IR PL Co-doping with Mg increases PL – why?


### Mn-Mg pairs in GaN



Th. Devillers, M. Rovezzi, et al. Scientific Reports 2 722 (2012)

#### Density functional theory spin densities



Th. Devillers, M. Rovezzi, et al. Scientific Reports 2 722 (2012)

# If a leaf can do it, we can do it too!



Lubitz and Messinger, Energy and Environmental Science, 2008

## $K\beta$ as a diagnostic tool to support XRD



Kern et al. Nature 563 421-425 (2018)

#### The La<sub>1-x</sub>Sr<sub>1+x</sub>MnO<sub>4</sub> series: doping dependence



#### The La<sub>1-x</sub>Sr<sub>1+x</sub>MnO<sub>4</sub> series: doping dependence





J. Herrero-Martín et al, Phys. Rev. B 72, 085106 (2005)

#### The La<sub>1-x</sub>Sr<sub>1+x</sub>MnO<sub>4</sub> series: doping dependence



MnO<sub>6</sub> local **anisotropy** is large and inversely proportional to hole content

	<u>N</u>	r (Mn-O) (Å)	
LaSrMnO <sub>4</sub>	4	1.90(1)	x=0
	2	2.27(3)	
La <sub>0.7</sub> Sr <sub>1.3</sub> MnO <sub>4</sub>	4	1.92(1)	x=0.3
	2	2.05(2)	
La <sub>0.5</sub> Sr <sub>1.5</sub> MnO <sub>4</sub>	4	1.92(1)	x=0.5
	2	1.98(1)	

J. Herrero-Martín et al, Phys. Rev. B 72, 085106 (2005)

The La<sub>1-x</sub>Sr<sub>1+x</sub>MnO<sub>4</sub> series: doping dependence in <u>powders</u>



XANES shift due to structural changes! Angle-integrated electron density unchanged.

## Linear Dichroism in XES



Even without polarization analysis in the emission a dichroism can be observed because of the transversal character of electro-magnetic radiation (one component is always missing).

## K $\beta$ Linear Dichroism in D<sub>4h</sub> symmetry





## Linear Dichroism in La<sub>1-x</sub>Sr<sub>1+x</sub>MnO4



## Valence-to-core (vtc or v2c) emission lines



#### XES and XAS: Complementary Techniques



### Orbital mixing – Molecular orbitals



The electronic states in matter have the symmetry of the system.

Within a one-electron picture, this applies to the valence orbitals.

Using a "linear combination of atomic orbitals" approach, we can picture the valence orbitals as sums of atomic orbitals.

NOTE: Any point group symmetry (including SO(3) for atomic orbitals is relative to a point, i.e. a center.

An example, s-orbitals on ligands may have p-like symmetry when choosing the metal as center

### Molecular orbitals of a 3d TM complex in Oh



A 1s vacancy will be filled by electrons in the  $t_{1u}$  bonding orbitals.

Copyright ©1998 Beverly J. Volicer and Steven F. Tello, UMass Lowell.

#### Fine structure of valence-to-core emission lines

#### Mainly sensitive to orbitals that are centered on ligands.

**Transitions from:** 



O.V. Safonova et al. / Electrochimica Acta 56 145 (2010)

Photoelectron spectroscopy and XES



J. Mater. Chem. C, 2013,1, 4527-4535

**Electrochemical Chrome Plating** 



How does Cr(III) behave chemically in electrolytes with organic substances? In what chemical state is Cr electroplated ?

### Valence-to-Core XES of electroplated Cr in organic electrolyte

5965



□ Formation of Cr<sub>3</sub>C<sub>2</sub> in nanocrystalline Cr Coatings

#### □ No O ligand found

Safonov et al., J. Phys. Chem. B 110 23192 (2006) Sample: nanocrystalline Cr thin film deposited electrochemically from organic solution

5985

Emission energy / eV

5995

29%  $Cr_{3}C_{2}$  and 71% Cr

5975

## Calculation of vtc XES

Ground state DFT calculations work surprisingly well.

This approach neglects:

$$I(E_i) \propto |\langle \Psi_{1s} | \hat{\boldsymbol{\varepsilon}} \cdot \boldsymbol{r} | \varphi_{MO} \rangle|^2$$

- Multi-electron excitations

- The core hole potential

Some codes for inner-shell spectroscopy with XES:

- ORCA by Frank Neese (MPI Muelheim)
- FDMNES by Yves Joly (CNRS Grenoble)
- StoBe (Lars Petterson, Klaus Hermann, Stockholm/Berliln)
- FEFF (John Rehr, Washington)

#### Valence-to-Core XES of Mn<sup>2+</sup> in Solution



P1 and P3 probably due to dynamical disorder and distant H<sub>2</sub>O molecules.

Smolentsev et al. JACS 131 12451 (2009)

#### **Detection of Ligand Protonation**



Smolentsev et al. JACS 131 12451 (2009)

#### Ligand Protonation in a Zn coordination complex



Pennerhahn et al., unpublished

Degree of ligand protonation



## vtc in metalloproteins: understanding nitrogen fixation ( $N_2 \rightarrow NH_3$ )







(B) Comparison of the normalized V2C XES data for FeMod (red), the MoFe protein (gray), and the  $\Delta$ nifB MoFe protein (black). (Inset) V2C satellite region for Fe<sub>2</sub>O<sub>3</sub> (red), Fe<sub>3</sub>N (blue), and MoFe protein (gray).

Lancaster et al., Science 334 974 (2011)

Orange, Fe; yellow, S; light blue, Mo; black, C<sup>4</sup>-, N<sup>3-</sup>, or O<sup>2-</sup>; dark blue, nitrogen; gray, carbon.

### Titanium in Silicate – TS-1





DFT calculations of vtc XES of Ti in TS-1



### Different chemical sensitivities in S K $\!\alpha$ and v2c



### Valence Shell Molecular Orbitals



Valence-to-core XES in S compounds with DFT calculations using different cluster sizes.

The atomic contributions to the molecular orbitals are give.

Inorg. Chem. 2010, 49, 6468–6473

Resonant inelastic X-ray scattering

### Interaction of X-rays with matter



Describe photon with vector field:

$$\boldsymbol{A}(z,t) = A_0(\boldsymbol{\varepsilon}_{\boldsymbol{\chi}} e^{i(kz-\omega t)} + \boldsymbol{\varepsilon}_{\boldsymbol{\chi}} e^{-i(kz-\omega t)})$$

Treat the interaction of **A** with sample within perturbation theory. We neglect interaction of the magnetic field with the electron spin (magnetic scattering).

In first order, a term in  $A^2$  is retained.

In second order, a term in **A**·**p** is retained.

#### Two scattering terms

The perturbative contributions to the scattering amplitude can be shown as 'Feynman' diagrams:



### What is a resonance?

One may think of using the definition that all **p**·**A** processes are resonant. However, that would cover EXAFS and even XPS.

Often, resonances are defined as excitations close to an absorption edge. But what is special about a resonance?

Two aspects are important:

- 1) A "resonance" shows a distinct (isolated) change in transition rate. This may be indicated by a peak in the density of states.
- 2) The scattering process is coherent, that means the phase of the scattered photon is preserved and we can observed interference effects.

Energy diagram in photon-in/photon-out spectroscopy

$$F^{KH}(\omega_{in}, \omega_{out}) = \frac{\omega_{out}}{\omega_{in}} \sum_{f} \left| \sum_{n} \frac{\langle f | \hat{O}'^{\dagger} | n \rangle \langle n | \hat{O} | g \rangle}{E_{n} - E_{g} - \hbar \omega_{in} - i\Gamma_{n}} \right|^{2} \delta(E_{f} - E_{g} - \hbar(\omega_{in} - \omega_{out}))$$

$$\prod_{\substack{\text{Incident Energy XAS}}} \left| | \langle f | \hat{O} | n \rangle |^{2} \right| \left| \langle n | \hat{O} | g \rangle |^{2} \right|$$

$$= \frac{|\langle n | \hat{O} | g \rangle|^{2}}{\text{Ground State}}$$

Energy diagram in photon-in/photon-out spectroscopy

$$F^{KH}(\omega_{in}, \omega_{out}) = \frac{\omega_{out}}{\omega_{in}} \sum_{f} \left| \sum_{n} \frac{\langle f | \hat{O}'^{\dagger} | n \rangle \langle n | \hat{O} | g \rangle}{E_{n} - E_{g} - \hbar \omega_{in} - i\Gamma_{n}} \right|^{2} \delta(E_{f} - E_{g} - \hbar(\omega_{in} - \omega_{out}))$$
Intermediate State
Incident Energy
XAS
$$\left| \langle n | \hat{O} | g \rangle \right|^{2}$$
Energy
transfer
Ground State
Valence band final state
## Different kinds of RIXS



The scheme above shows the RIXS process in a one-electron picture. Note that the final state in valence-to-core RIXS could also be observed in optical spectroscopy.

Inelastic X-ray scattering



X-ray scattering allows studying low energy excitations element-selectively!

## Photon-in/photon-out spectroscopy



# Photon-in/photon-out spectroscopy at the ESRF



# Hard X-ray Photon-in/Photon-out spectroscopy



## Hard X-ray Photon-in/Photon-out spectroscopy



## Hard X-ray Photon-in/Photon-out spectroscopy





## Energy diagram in photon-in/photon-out spectroscopy



**Ground State** 

# The RIXS plane



Incident Energy

# The RIXS/RXES plane



Incident Energy

#### **High Resolution Fluorescence Detection**



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. . . . . . . .
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Incident Energy (eV)

#### Hämäläinen et al., PRL 67 2850 (1991)

Carra et al. PRL 74 3700 (1995)

# $CeO_2 XAS$



# $CeO_2 XAS$



2p3d (L $\alpha$ ) RIXS plane in CeO<sub>2</sub>



The 3d and 2p core hole potentials are similar.
Weak interaction of core hole with photoexcited electron

Spectral features appear along diagonal streak.



Hämäläinen et al., Phys. Rev. Lett. 67 2850 (1991) Carra et al. PRL 74 3700 (1995) Glatzel and Bergmann, Coord. Chem. Rev. 249 65 (2005) Kotani et al., J. Electr. Spectr. Relat. Phenomena 184 (2011) 210–215 2p3d (L $\alpha$ ) RIXS plane in CeO<sub>2</sub>



#### Direct study of the valence shell



#### Another parameter for your energy calibration



## Keep E<sub>XES</sub> constant !!

#### **HERFD-XANES** in Pt and W compounds



# **HERFD-XANES** in Hg



# Actinides





## High energy resolution XANES at the U M4 edge



K. Kvashnina et al. PRL **111** 253002 (2013)K. Kvashnina et al. Ang. Chemie, in press (2019)

Resonant inelastic X-ray scattering including the valence orbitals

Energy diagram in photon-in/photon-out spectroscopy

$$F^{KH}(\omega_{in}, \omega_{out}) = \frac{\omega_{out}}{\omega_{in}} \sum_{f} \left| \sum_{n} \frac{\langle f | \hat{O}'^{\dagger} | n \rangle \langle n | \hat{O} | g \rangle}{E_{n} - E_{g} - \hbar \omega_{in} - i\Gamma_{n}} \right|^{2} \delta(E_{f} - E_{g} - \hbar(\omega_{in} - \omega_{out}))$$
Intermediate State
Incident Energy
XAS
$$\left| \langle n | \hat{O} | g \rangle \right|^{2}$$
Energy
transfer
Ground State
Valence band final state

## Valence band UPS and surface chemistry



Fig. 2. UPS He II spectra of CO adsorbed on: (1) rhenium; (2) Pt-Re "alloy"; (3) platinum. The dashed curves are characteristic of the clean surfaces before exposition to CO.

# CO oxidation over supported Pt nanoparticles



P. Glatzel, J. Singh, K. Kvashnina, J. van Bokhoven, JACS, 132, 2555-2557 (2010)

# Simplifying the Kramers-Heisenberg Formula

$$F^{KH}(\omega_{in},\omega_{out}) = \frac{\omega_{out}}{\omega_{in}} \sum_{f} \sum_{n} \frac{\langle f | \hat{O}^{f\dagger} | n \rangle \langle n | \hat{O} | g \rangle}{E_{n} - E_{g} - \hbar \omega_{in} - i\Gamma_{n}} \Big|^{2} \delta \left( E_{f} - E_{g} - \hbar \left( \omega_{in} - \omega_{out} \right) \right)$$
  
Interference changes intensities.  
$$|n\rangle, E_{n} \qquad |n\rangle, E_{n} \qquad |n\rangle, E_{f}$$
  
Ignore Interference and simplify:  
$$Does the scattered photon forget?$$
$$F^{KH}(\omega_{in},\omega_{out}) = \frac{\omega_{out}}{\omega_{in}} \sum_{f} \sum_{n} \frac{XES}{(E_{n} - E_{g} - \hbar \omega_{in})^{2} + \Gamma_{n}^{2}} \delta \left( E_{f} - E_{g} - \hbar \left( \omega_{in} - \omega_{out} \right) \right)$$

## Using the density of states

$$F^{KH}(\omega_{in},\omega_{out}) = \frac{\omega_{out}}{\omega_{in}} \sum_{f} \sum_{n} \frac{\left| \left\langle f \left| \hat{O}'^{\dagger} \right| n \right\rangle \right|^{2} \left| \left\langle n \left| \hat{O} \right| g \right\rangle \right|^{2}}{\left( E_{n} - E_{g} - \hbar \omega_{in} \right)^{2} + \Gamma_{n}^{2}} \delta \left( E_{f} - E_{g} - \hbar \left( \omega_{in} - \omega_{out} \right) \right)$$

Approximate with density of states:

Unoccupied:

$$n|\hat{O}|g\rangle|^2 \rightarrow \rho'(\varepsilon_u)$$

Occupied:

$$\left|\left\langle f\left|\hat{O}'\right|n\right\rangle\right|^{2} \rightarrow \rho(\varepsilon_{o})$$

$$F(\Omega,\omega) = \int_{\varepsilon} d\varepsilon \frac{\rho(\varepsilon)\rho'(\varepsilon + \Omega - \omega)}{(\varepsilon - \omega)^2 + \frac{\Gamma_n^2}{4}}$$

Jimenez-Mier, J. et al. Phys. Rev. B 1999, 59, 2649.

# DOS calculations using FEFF84



# RIXS planes using FEFF d-DOS



$$F(\Omega,\omega) = \int_{\varepsilon} d\varepsilon \frac{\rho(\varepsilon)\rho'(\varepsilon + \Omega - \omega)}{(\varepsilon - \omega)^2 + \frac{\Gamma_n^2}{4}}$$

**Comparison with Experiment** 



Direct probe of Pt d-DOS under in situ conditions

#### Improved instrumental resolution



# How to build a zeolitic lattice



# Titanium in Silicate – TS-1





# Titanium in Silicate – TS-1


Valence Band RIXS



E. Gallo, C. Lamberti, et al. in preparation

## **Comparison UV-Vis and valence band RIXS**





degased

 $H_2O$ 

 $NH_3$ 

Incident Energy / eV

## DFT calculations using ORCA



