

Machine learning in glass science, with examples of applications

Charles Le Losq

Géomatériaux, Institut de physique du globe de Paris

Collaborations:

IPGP: Daniel Neuville, Roberto Moretti

ANU-RSES: Matt Valetich, Richard Arculus, John Mavrogenes, Hugh O'Neill, Andrew Berry, Malcolm Sambridge

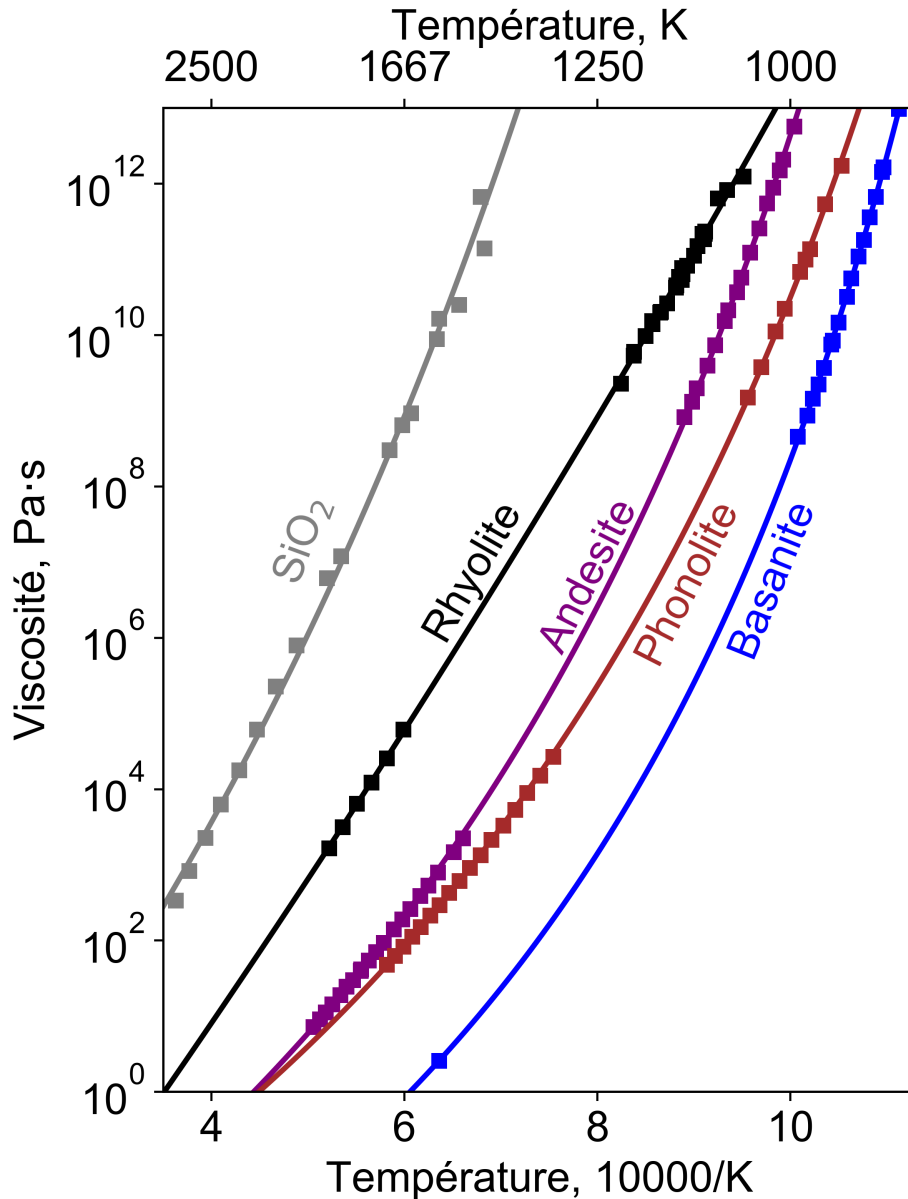
Durham University: Andrew Valentine

Geophysical Lab: Bjorn Mysen, George Cody

Merci à l'ANR IDEX Université de Paris, 18-IDEX-0001

Journées USTV 2021

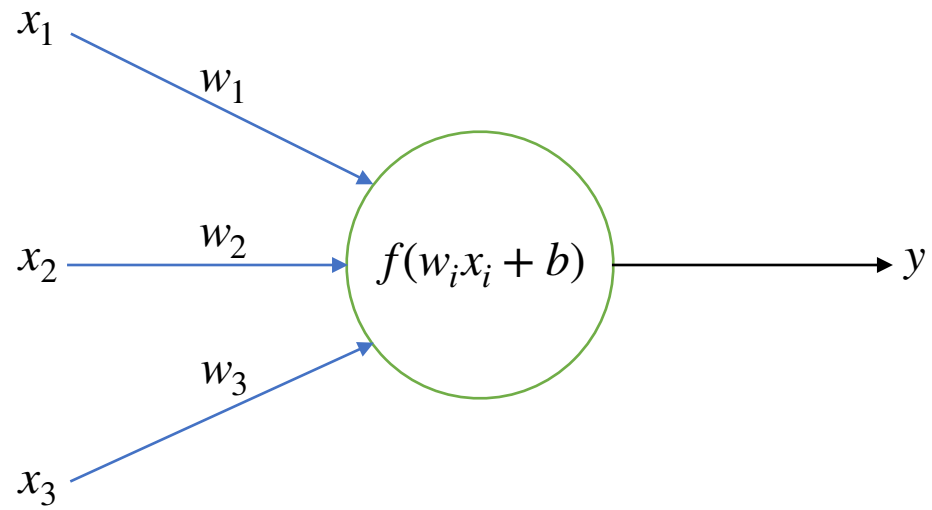
The viscosity of silicate melts



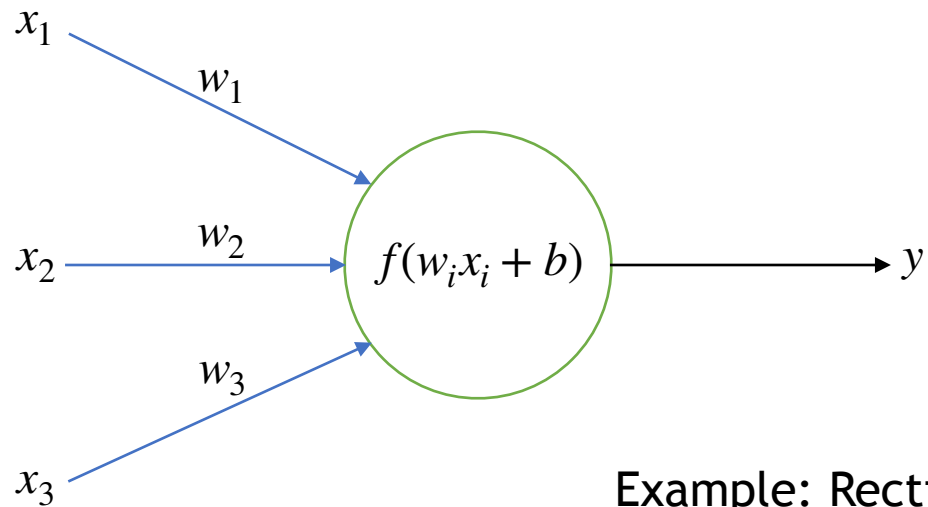
- Chemistry > structure > properties
- Volatiles, iron redox...
- Also crystals and bubbles

No general (precise) model that bring a true understanding of the flow process

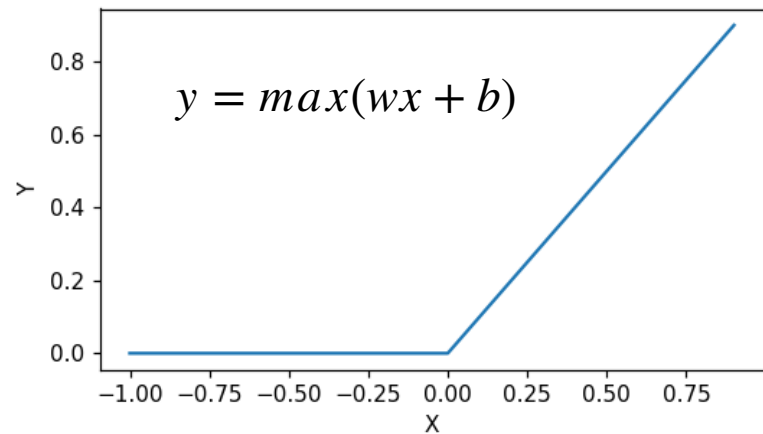
Perceptron Model



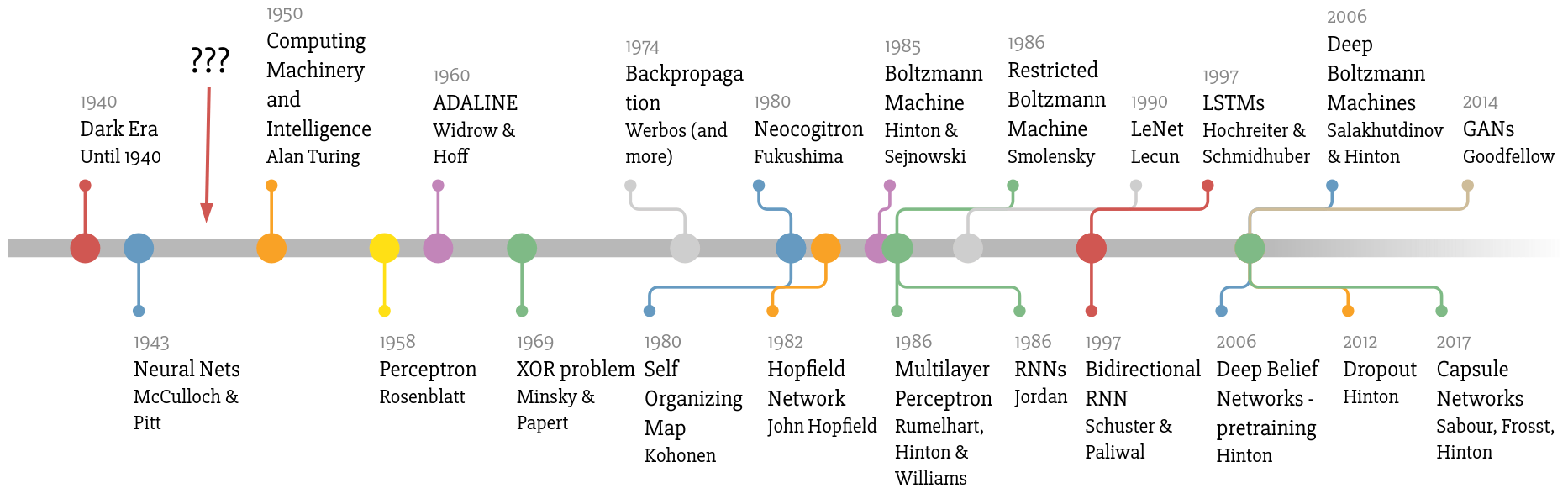
Perceptron Model



Example: Rectifier function



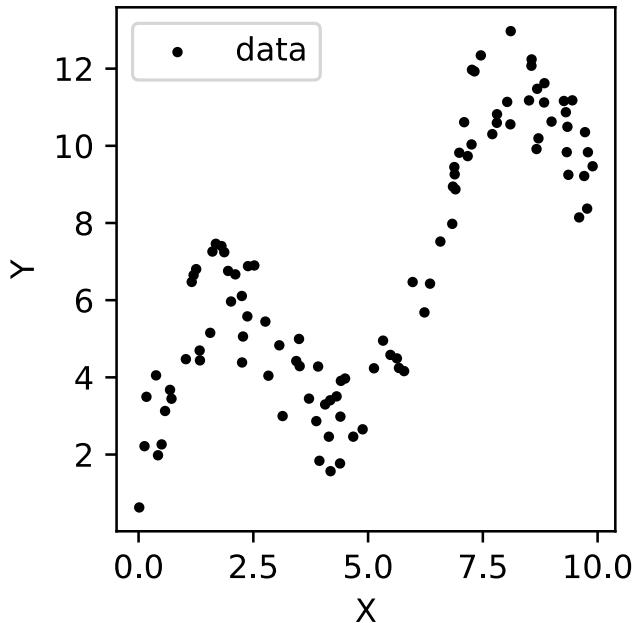
Deep Learning Timeline



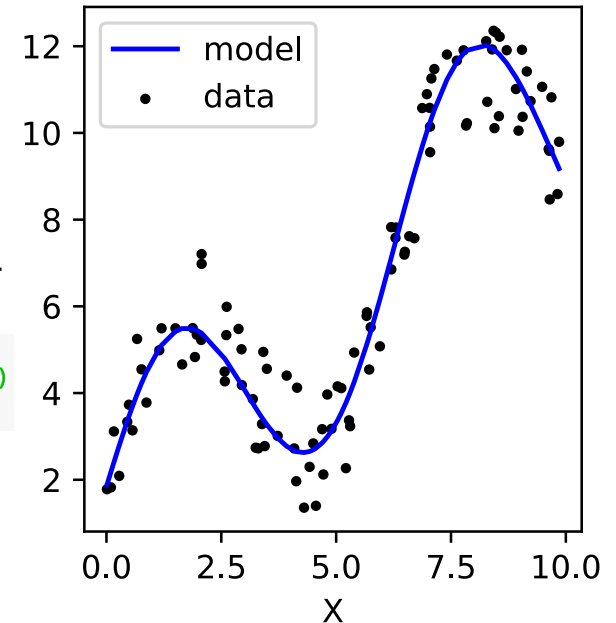
Made by Favio Vázquez

Why « trendy »?

- **It's now easy** = focus on building models, not code
 - open source software libraries
 - high level languages (Julia, Python, R, Matlab)



```
from sklearn.svm import SVR
svr_rbf = SVR(kernel='rbf', C=100)
svr_rbf.fit(x.reshape(-1,1),y)
```



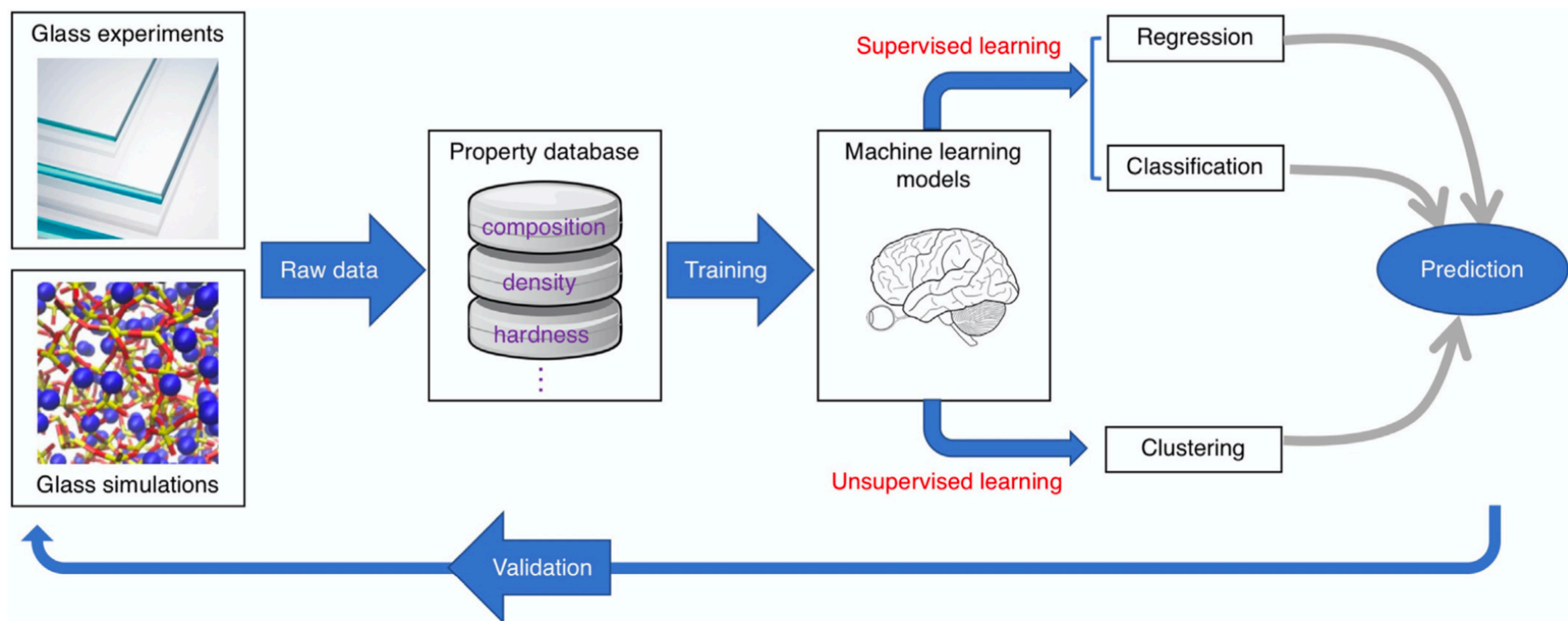
- **Internet**
 - amount and transfers of data
 - easy access to resources
- **Social media / advertisement driven**
 - two of the largest ML software libraries, Tensorflow (2015) and Pytorch (2016), « surprisingly » originate from Google and Facebook

What can it bring to us?

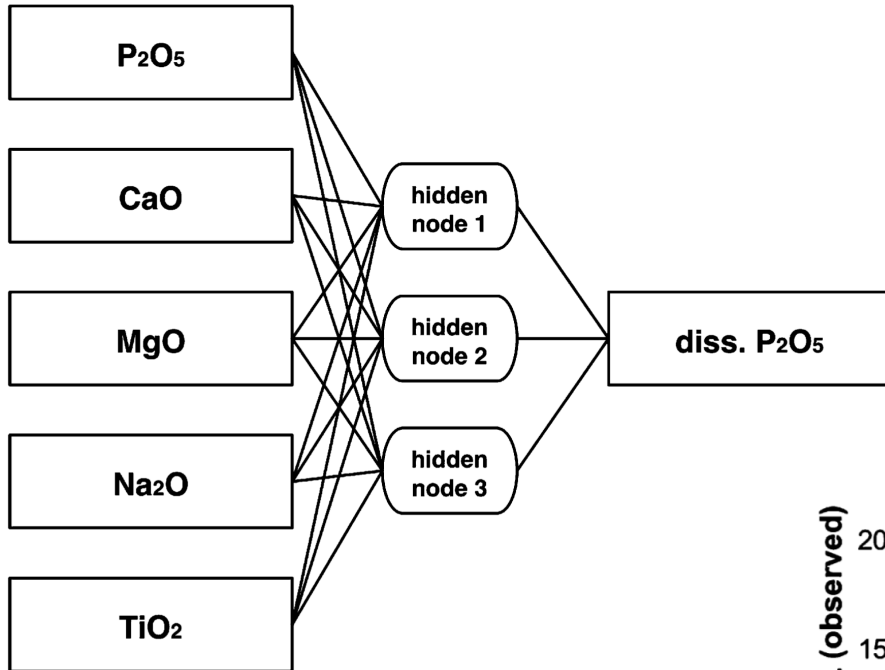
Glass: structure & properties from measurements, theories and MD simulations

Machine learning = another tool in our toolbox to, e.g.,

- analyze data and generate models
- explore datasets
- design new compositions
- detect drifts & anomalies

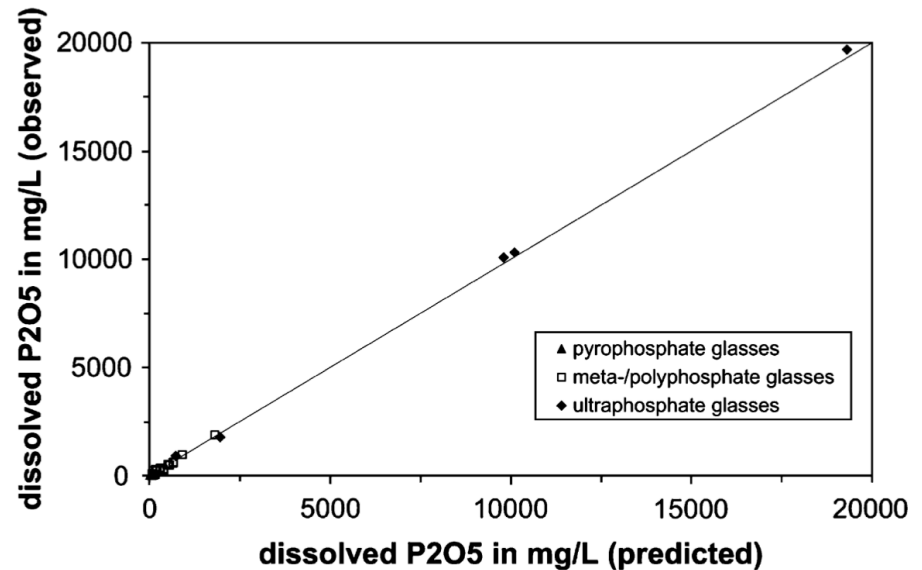


Examples of applications

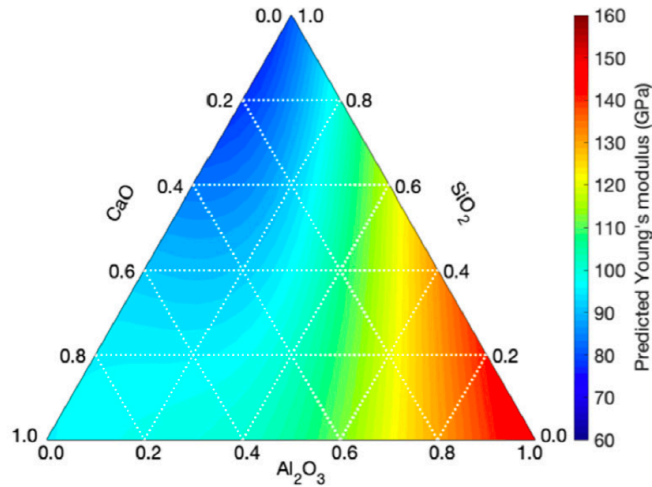


Brauer et al. 2007

Degradable implant materials: solubility of glasses in the system P_2O_5 - CaO - MgO - N



Examples of applications

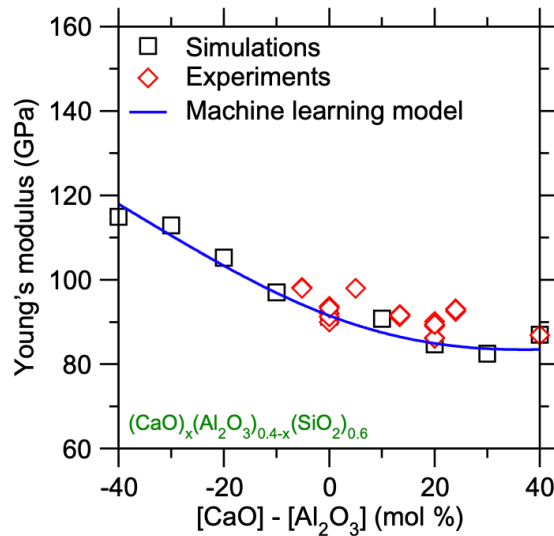


(b)

Yang et al. 2019

*Predictions of
mechanical properties
of glasses*

*Young's modulus in
CaO aluminosilicates*



(d)

**Practical example: how to predict
glass density from composition?**

Practical example: how to predict glass density from composition?

Prediction of the density of $\text{Na}_2\text{O-K}_2\text{O-Al}_2\text{O}_3\text{-SiO}_2$ glasses

Supervised ML: we know X and Y

- Practical example: prediction of the density of Na₂O-K₂O-Al₂O₃-SiO₂ glasses

- Database available at github.com/charlesll/i-melt/

	A	B	C	D	E	F	G	H	I
	Name	sio2	al2o3	na2o	k2o	d	ese_d	reference	Name_study
1	NAK83.8.0	83,9	8,7	7,4	0,0	2,317	0,005	LL2013	NAK83.8.0
2	NAK83.8.2	83,4	8,3	6,2	2,1	2,318	0,007	LL2013	NAK83.8.2
3	NAK83.8.4	83,2	8,4	4,2	4,1	2,317	0,004	LL2013	NAK83.8.4
4	NAK83.8.6	83,3	8,5	2,2	6,1	2,323	0,006	LL2013	NAK83.8.6
5	NAK83.8.8	83,1	8,6	0,1	8,2	2,313	0,007	LL2013	NAK83.8.8
6	KA8005	84,1	5,0	0,0	10,8	2,345	0,001	TS	KA8005
7	NAK75.0.25	75,0	0,0	0,0	25,0	2,426	0,005	LL2017b	NAK75.0.25
8	NAK75.0.0	75,0	0,0	25,0	0,0	2,430	0,004	LL2014	NAK75.0.0
9	NAK75.2.0	76,5	2,1	21,4	0,0	2,416	0,008	LL2014	NAK75.2.0
10	NAK75.06.0	75,2	6,4	18,4	0,0	2,402	0,001	LL2014	NAK75.06.0
11	NAK75.9.0	75,1	9,2	15,7	0,0	2,393	0,003	LL2014	NAK75.9.0
12	NAK75.12.0	75,0	12,5	12,5	0,0	2,369	0,001	LL2013	NAK75.12.0
13	NAK75.12.2	75,4	12,5	9,7	2,4	2,374	0,003	LL2013	NAK75.12.2
14	NAK75.12.5	75,3	12,4	7,4	4,8	2,368	0,003	LL2013	NAK75.12.5
15	NAK75.12.6	75,2	12,5	6,1	6,2	2,371	0,003	LL2013	NAK75.12.6
16	NAK75.12.7	75,5	12,3	5,0	7,2	2,372	0,001	LL2013	NAK75.12.7
17	NAK75.12.10	75,2	12,4	2,7	9,8	2,370	0,004	LL2013	NAK75.12.10
18	NAK75.12.12	75,1	12,8	0,1	12,1	2,357	0,008	LL2013	NAK75.12.12
19	NAK75.16.0	75,2	16,1	8,8	0,0	2,375	0,004	LL2014	NAK75.16.0
20	KA72.07	72,3	7,1	0,0	20,6	2,408	0,001	TS	KA72.07
21	NAK67.16.0	66,7	16,7	16,7	0,0	2,422	0,006	LL2017	NAK67.16.0
22	NAK67.16.16	66,7	16,7	0,0	16,7	2,401	0,005	LL2017	NAK67.16.16
23	NS66	66,7	0,0	33,3	0,0	2,483	0,001	N2006	NS66

1/ Data Importation

- ▶ We import the data (Python, library Pandas)

```
1 data = pd.read_excel("Database_IPGP.xlsx")
2
3 X = data.loc[:,["sio2","al2o3","na2o","k2o"]].values
4 Y = data.loc[:, "d"].values.reshape(-1,1)
5 XY = data.loc[:,["sio2","al2o3","na2o","k2o","d"]].values
```

$$Y = f(X), f \text{ unknown}$$

2/ Data Preparation

- ▶ We import the data (Python, library Pandas)
- ▶ **We prepare the data**
 - ▶ Split the data
 - train & validation subset(s) for training
 - test subset for final evaluation

```
1 # Splitting the data !
2 X_train_valid, X_test, Y_train_valid, Y_test = train_test_split(X, Y, test_size=0.30)
3 X_train, X_valid, Y_train, Y_valid = train_test_split(X_train_valid, Y_train_valid, test_size=0.20)
```

- ▶ **Standardize the data** = ML algorithms behave better with numbers at the same dimension, and usually close to unity
 - min-max = $(X - \min(X)) / (\max(X) - \min(X))$
 - standard scaler = $(X - \text{mean}(X)) / \text{std}(X)$

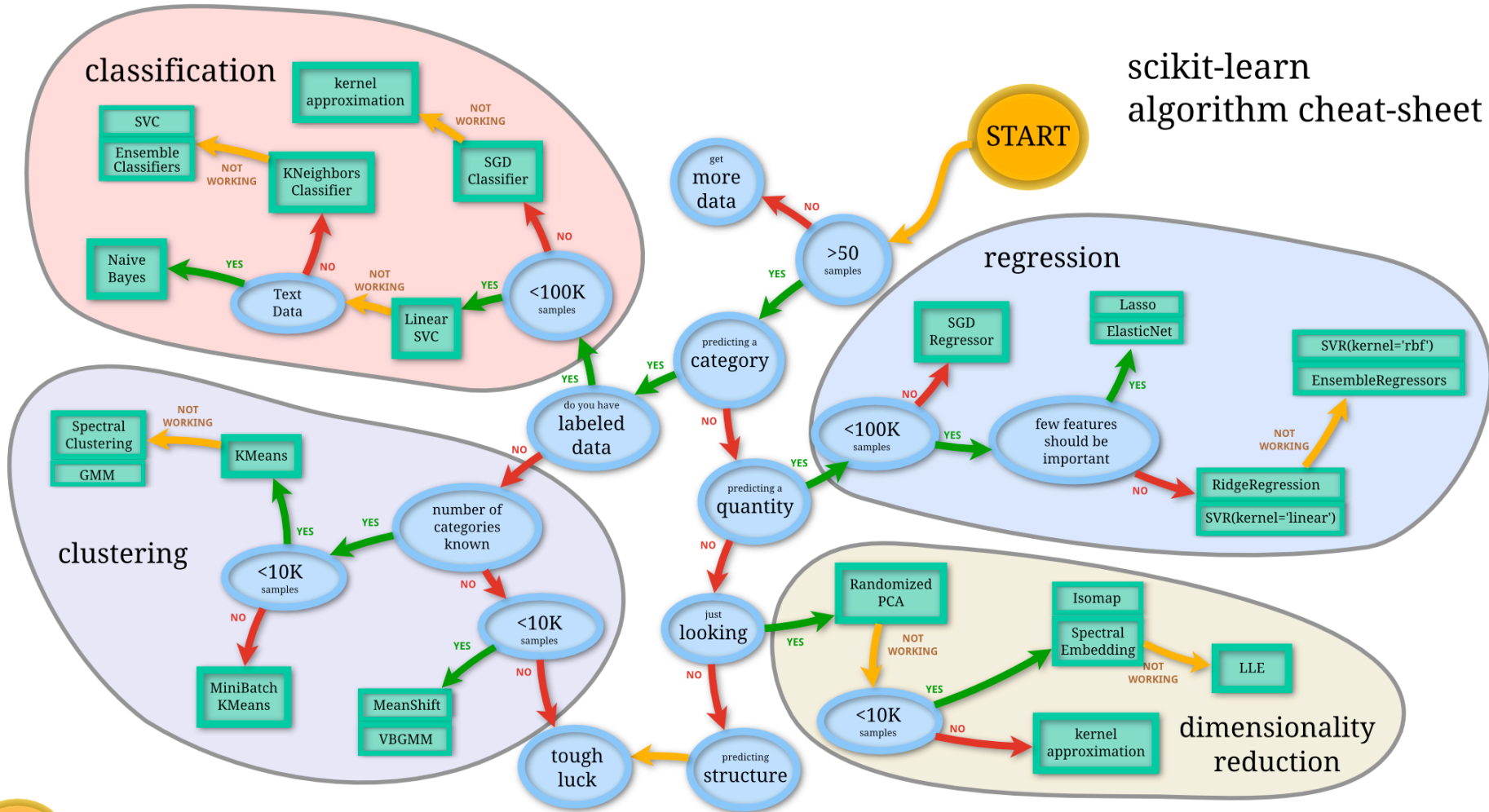
```
1 ##### Scaling X data : the composition
2 X_scaler = StandardScaler() # creating the scaler
3 # do the job
4 X_train_sc = X_scaler.fit_transform(X_train)
5 X_valid_sc = X_scaler.fit_transform(X_valid)
6 X_test_sc = X_scaler.fit_transform(X_test)
7
8 ##### Scaling the Y data
9 Y_scaler = StandardScaler() # creating the scaler
10 # do the job
11 Y_train_sc = Y_scaler.fit_transform(Y_train)
12 Y_valid_sc = Y_scaler.fit_transform(Y_valid)
13 Y_test_sc = Y_scaler.fit_transform(Y_test)
14
15 ##### Scaling the full dataset
16 XY_sc = X_scaler.fit_transform(XY)
```

4/ Model selection

- ▶ We import the data (Python, library Pandas)
- ▶ We prepare the data
 - ▶ Split the data
 - train & validation subset(s) for training
 - test subset for final evaluation
 - ▶ Standardize the data = ML algorithms behave better with numbers at the same dimension, and usually close to unity
 - min-max = $(X - \min(X)) / (\max(X) - \min(X))$
 - standard scaler = $(X - \text{mean}(X)) / \text{std}(X)$
- ▶ **We need to choose a model**

4/ Model selection

scikit-learn
algorithm cheat-sheet

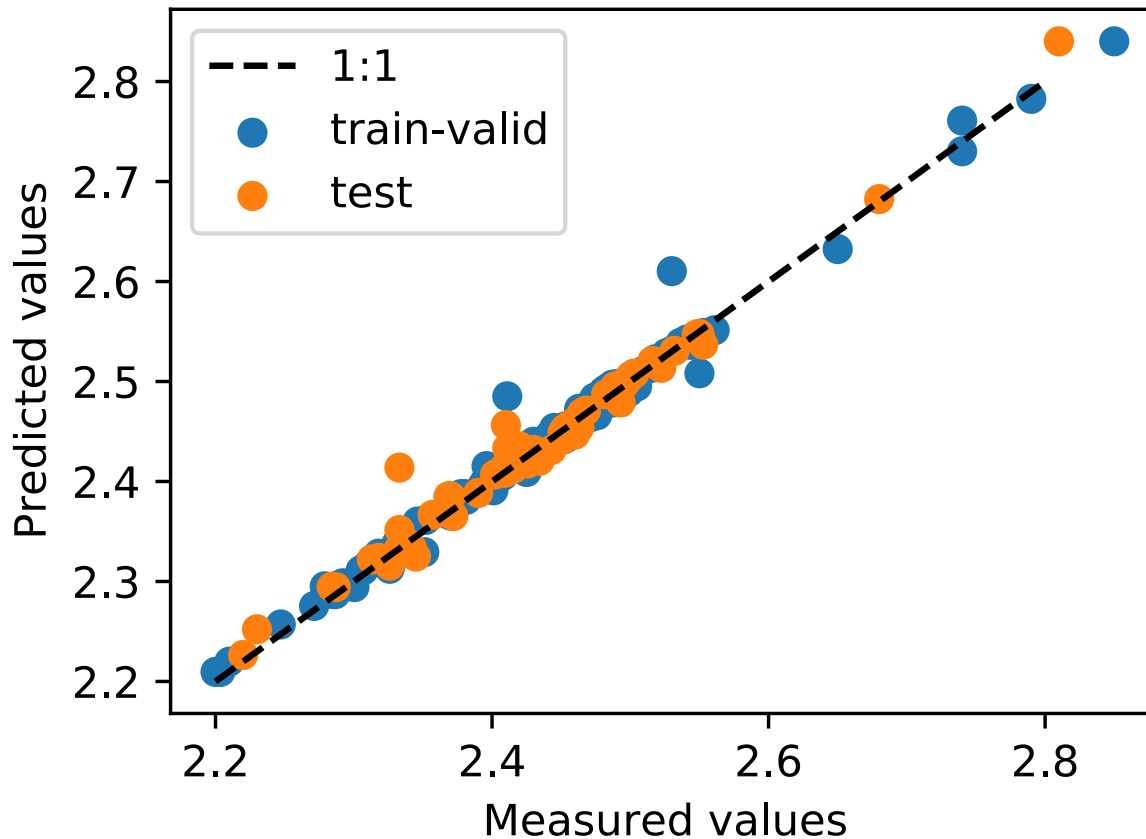


5/ Fit and predict!

- ▶ We import the data (Python, library Pandas)
- ▶ We prepare the data
 - ▶ Split the data
 - train & validation subset(s) for training
 - test subset for final evaluation
 - ▶ Standardize the data = ML algorithms behave better with numbers at the same dimension, and usually close to unity
 - min-max = $(X - \min(X)) / (\max(X) - \min(X))$
 - standard scaler = $(X - \text{mean}(X)) / \text{std}(X)$
- ▶ We need to choose a model
- ▶ **We fit the model to the data and predict things!**

The steps involved

- Prediction of the density of $\text{Na}_2\text{O-K}_2\text{O-Al}_2\text{O}_3\text{-SiO}_2$ glasses
 - ▶ *Data importation*
 - ▶ *Data preparation*
 - ▶ *Model selection*
 - ▶ *Fit data and get predictions!*



Support Vector
Machines

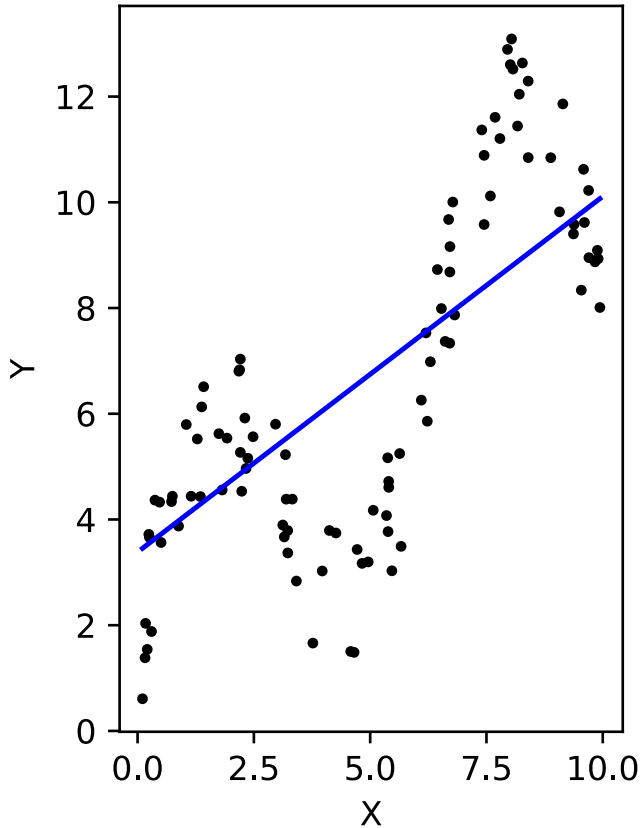
Fit well!

RMSE train: 0.01
RMSE test: 0.01

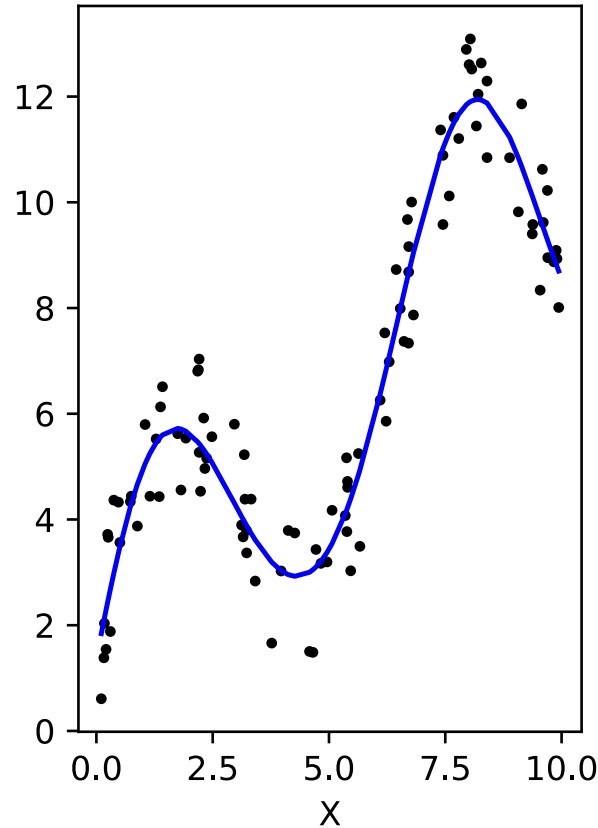
No overfitting

Overfitting

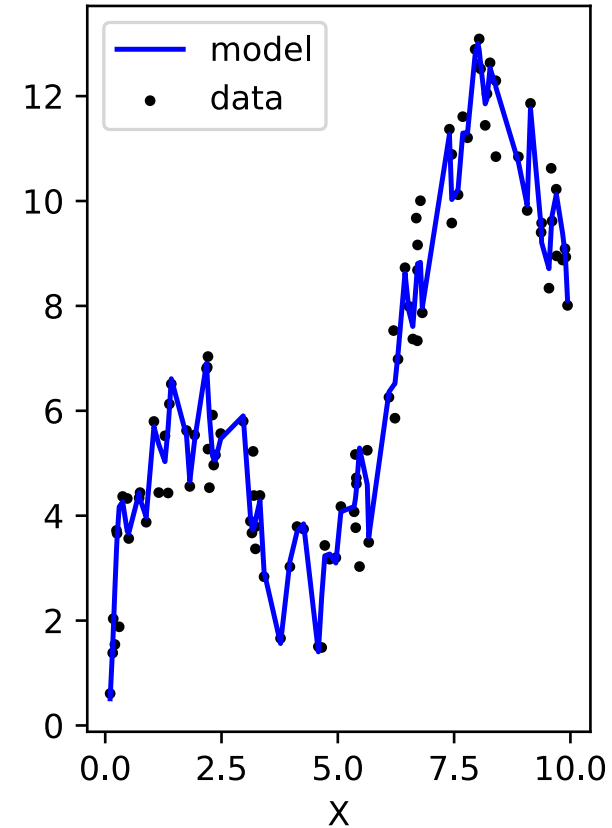
1) underfit :/



2) good :)



3) overfit :/

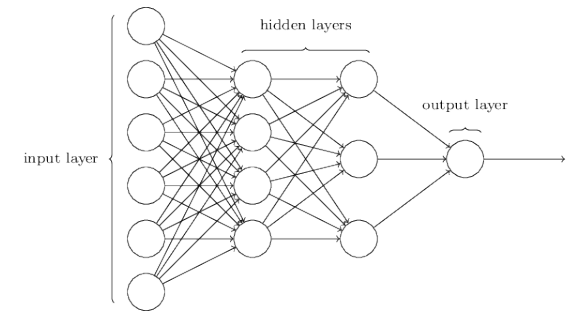
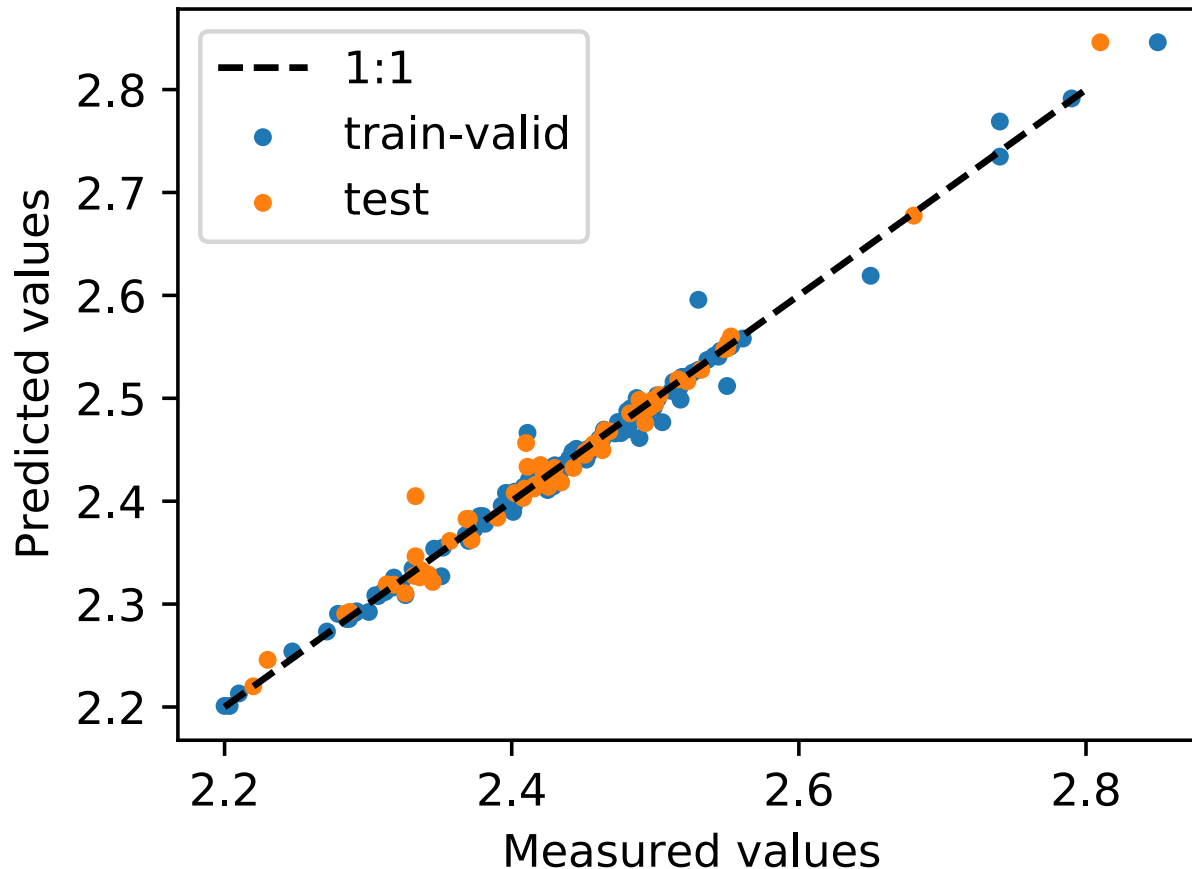


- ▶ Algorithm and mitigation methods
- ▶ Dataset size... this is why ML develops with the « big data » era!

The steps involved

- Prediction of the density of $\text{Na}_2\text{O-K}_2\text{O-Al}_2\text{O}_3\text{-SiO}_2$ glasses

- ▶ *Data importation*
- ▶ *Data preparation*
- ▶ *Model selection*
- ▶ *Fit data and get predictions!*



Multilayer perceptrons

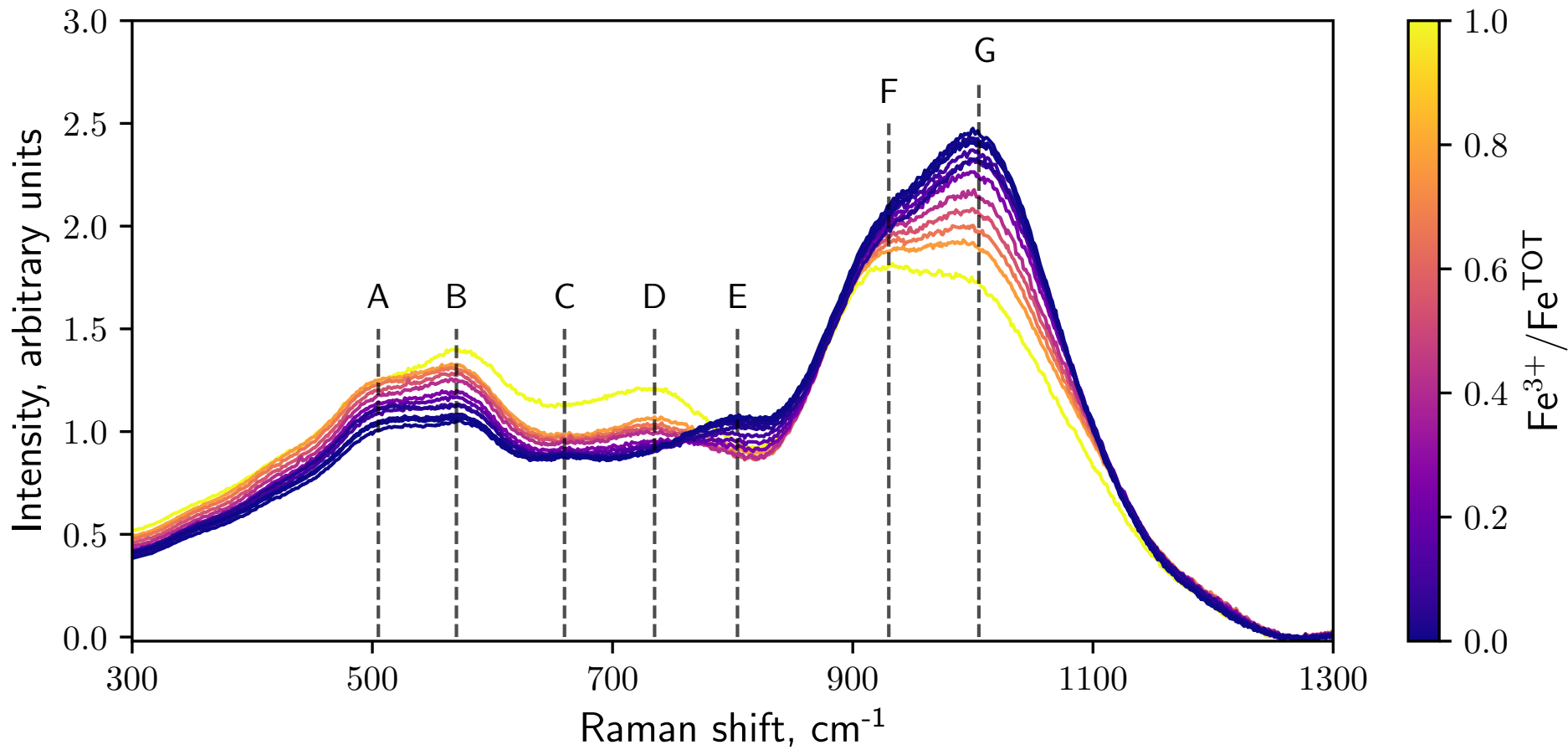
Overfitting mitigated via

- > hyperparameter tuning
- > training strategies

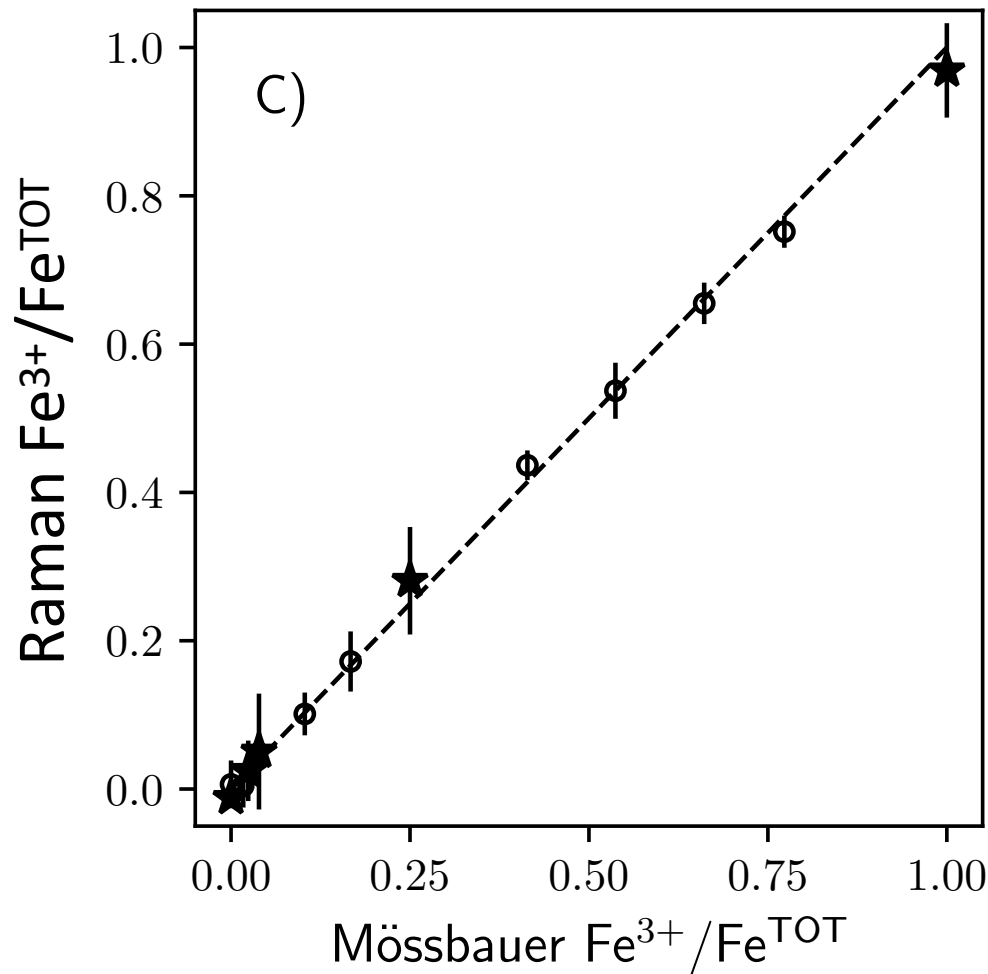
- > RMSE train: 0.01
- > RMSE test: 0.01

More about Neural Nets for Analyzing data

example: Raman spectra of Fe-bearing CMAS glasses

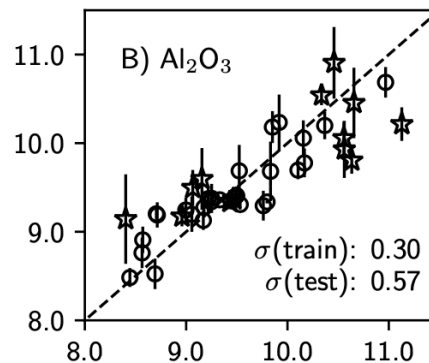
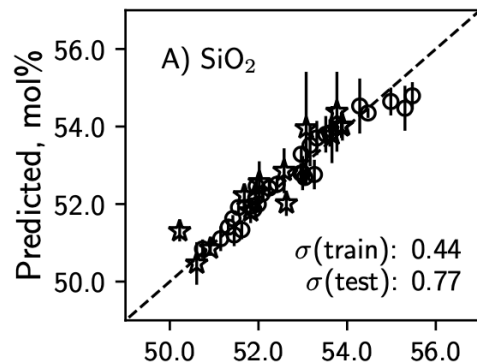


Le Losq et al., 2019,
Am. Min. 104:1032



Neural Nets for Analyzing data

Artificial neural networks + Raman spectroscopy = redox and chemical composition of glasses



Le Losq et al.,
2019, Am. Min.
104:1032

Making smarter models

- **Greybox models**

- ▶ a.k.a. physics-based ML models
- ▶ a.k.a. physics and chemistry informed ML models
- ▶ a.k.a. knowledge based ML models
- ▶ a.k.a. semiphysical ML models
- ▶ ... !

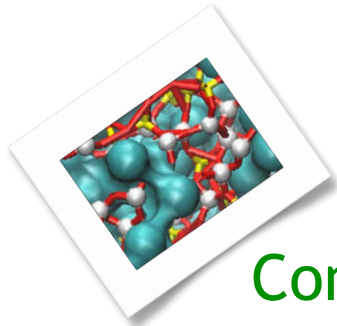
ML + physico-chemical equations
= Greybox models

Making smarter models

- **Greybox models**

- ▶ a.k.a. physics-based ML models
- ▶ a.k.a. physics and chemistry informed ML models
- ▶ a.k.a. knowledge based ML models
- ▶ a.k.a. semiphysical ML models
- ▶ ... !

ML + physico-chemical equations
= Greybox models



Blackbox:
Composition, T → Neural Network → Viscosity

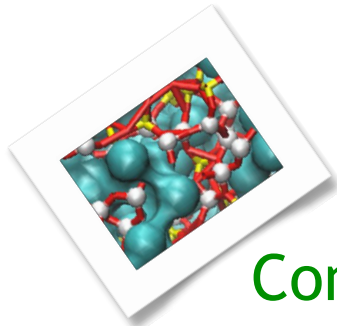


Making smarter models

- **Greybox models**

- ▶ a.k.a. physics-based ML models
- ▶ a.k.a. physics and chemistry informed ML models
- ▶ a.k.a. knowledge based ML models
- ▶ a.k.a. semiphysical ML models
- ▶ ... !

ML + physico-chemical equations
= Greybox models



Blackbox:

Composition, T \rightarrow Neural Network \rightarrow Viscosity



Greybox:

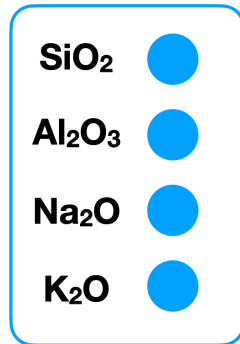
Composition \rightarrow Neural Network \rightarrow Adam-Gibbs + T \rightarrow Viscosity

Making smarter models

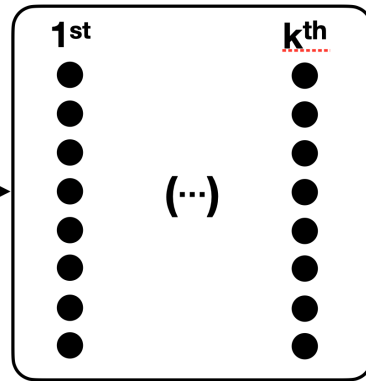
For glass: example of *i-Melt*

github.com/charlesll/i-melt/

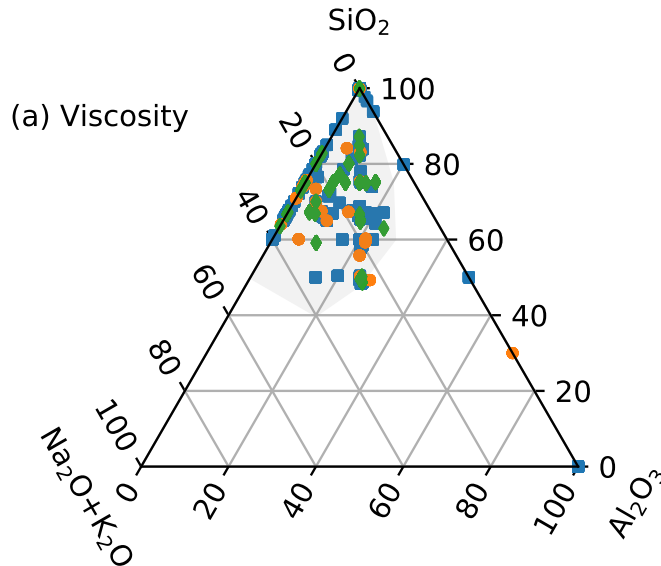
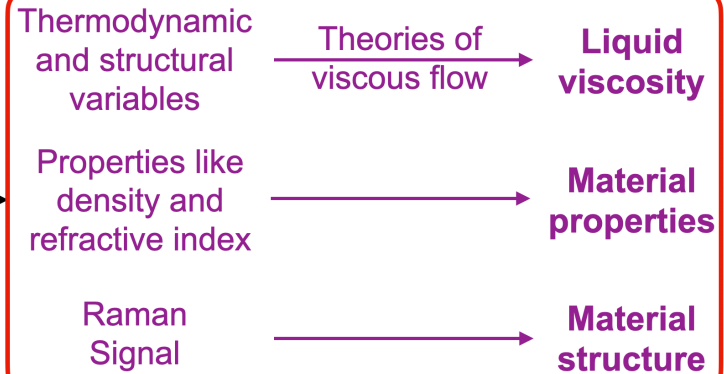
Chemistry
(model inputs)



Artificial Neural Network
ReLU units, k layers



Predictions



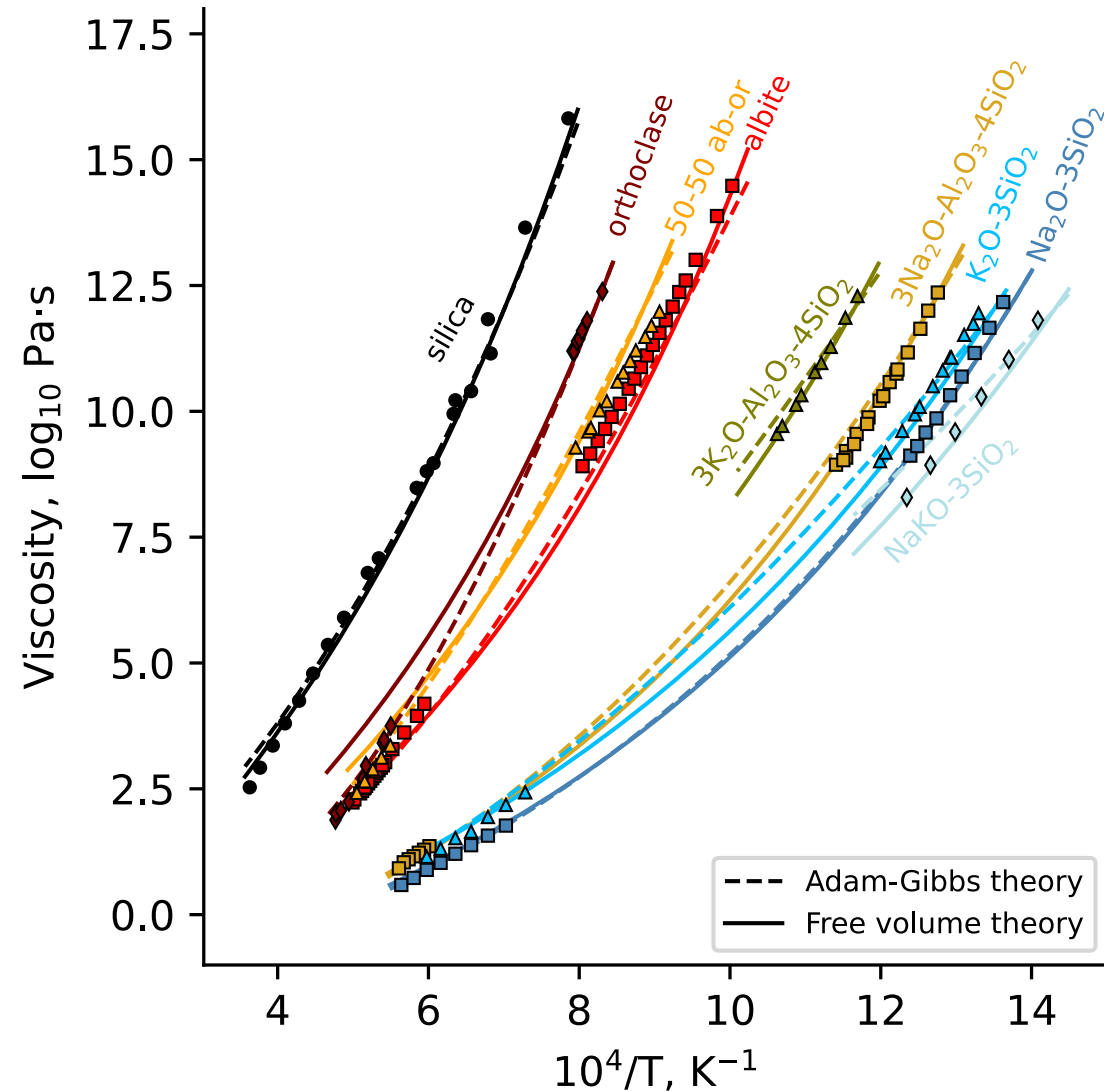
Demonstration on
the
 $\text{Na}_2\text{O}-\text{K}_2\text{O}-\text{Al}_2\text{O}_3-\text{SiO}_2$
system

Le Losq et al., 2021, GCA 314:27

Making smarter models

For glass: example of *i-Melt*

github.com/charlesll/i-melt/



Na₂O-K₂O-Al₂O₃-SiO₂ system

Viscosity ± 0.4 log unit

Density ± 0.02 g cm⁻³

Refractive index ± 0.006

$T_g \pm 19$ K

$S_{\text{conf}}(T_g) \pm 0.9$ J mol⁻¹ K⁻¹

Raman spectra $\pm \sim 20\%$

Parameters of Adam-Gibbs,
Free Volume, MYEGA, VFT,
Avramov-Milchev equations...

Making smarter models

For glass: example of *i-Melt*

github.com/charlesll/i-melt/

i-Melt: Prediction of melt and glass properties

i-Melt uses machine learning to predict the properties of glasses and melts. Select a composition using the sliders on the sidebar (left) and see predictions below. For full details [read the paper](#) and [download the code!](#)

Notes:

Glass transition

800 K

Softening point

1027 K

Working point

1365 K

Density

2.42 g/cm³

Configurational entropy

8.4 J/(mol K)

Refractive index

1.802

Melt fragility

30.7

VFT equation

$$\log_{10} \eta = -4.29 + \frac{7448.3}{T - 342.5}$$

Glass composition

SiO₂ concentration, mol%

75.00

50.00 100.00

Al₂O₃ concentration, mol%

6.00

0.00 50.00

Na₂O concentration, mol%

19.00

0.00 50.00

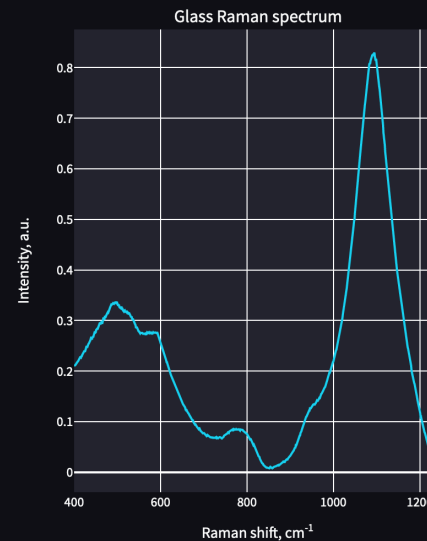
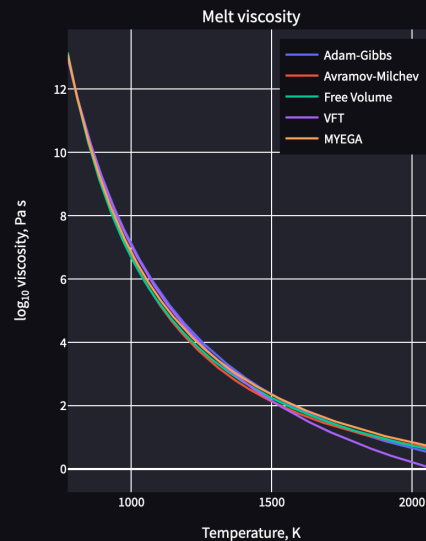
K₂O concentration, mol%

0.00

0.00 50.00

Calculate!

When you run the model, compositions will be rescaled to ensure they sum to 100%.



Manage

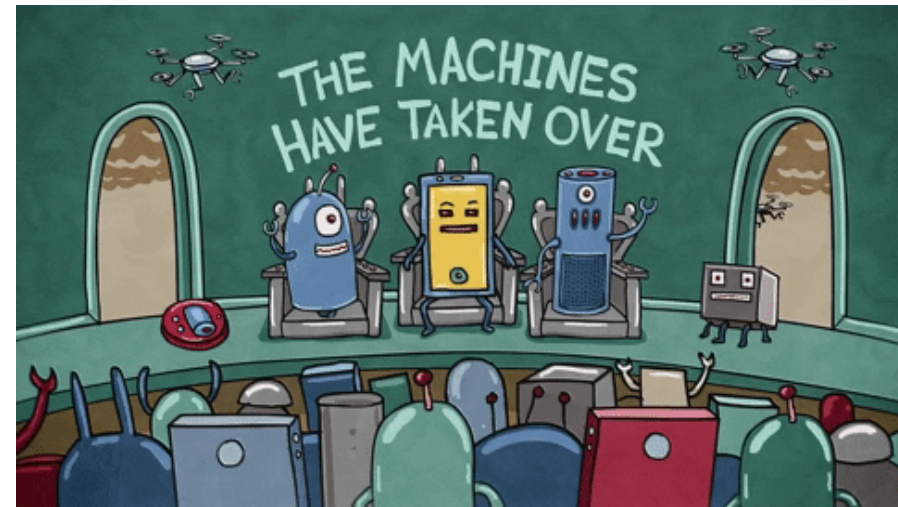
Conclusion

Theory - Models - Observation - new: machine learning

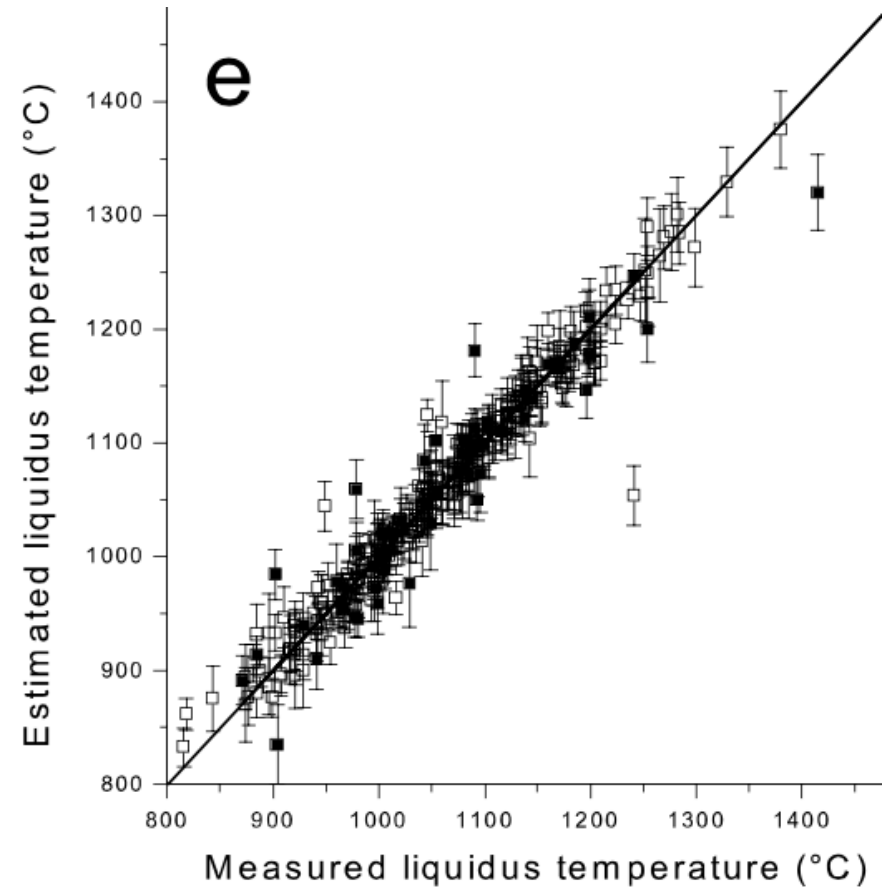
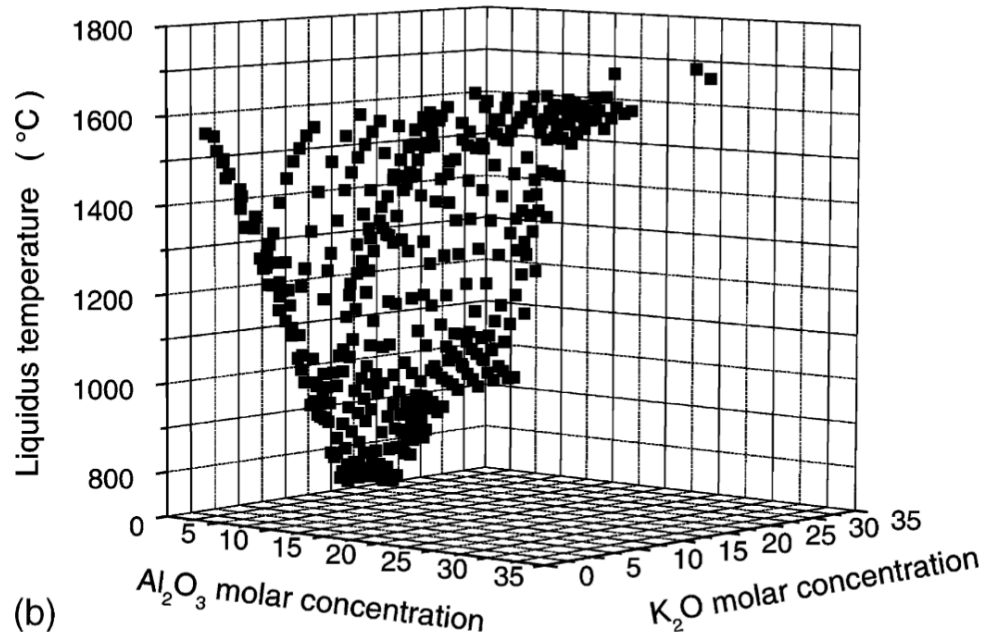
- analyze data and generate predictive models of properties
- explore datasets
- select/design new compositions
- detect drifts & anomalies
- ...

The challenges

- datasets (generation, quality...)
- algorithms and uncertainties
- interpretation
- automated systems for industry
- balance between blackbox & physics

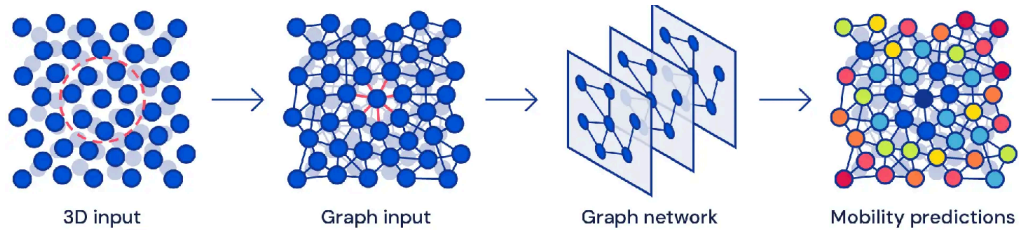


- Not « new »
- Not « artificial intelligence »



Example: prediction of liquidus temperatures of K_2O - Al_2O_3 - SiO_2 using Neural Networks by Dreyfus et Dreyfus, 2003

Examples of applications

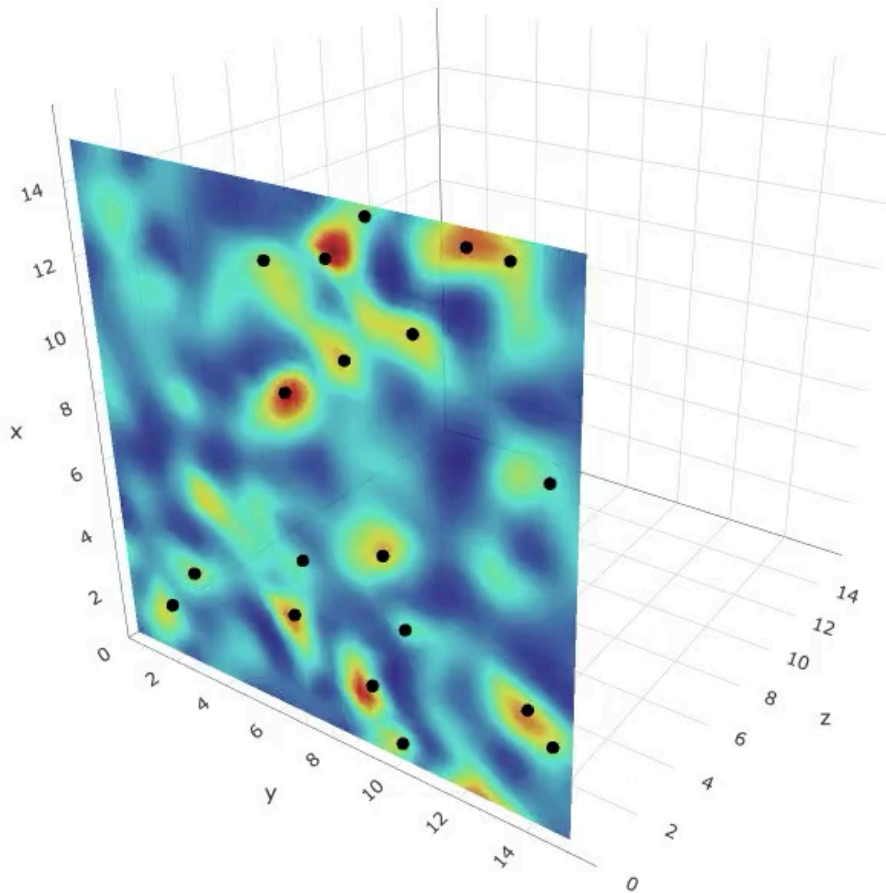


Bapst et al. 2019

DeepMind/Google

Prediction of atomic movements via graph neural networks

Better understand properties & glass transition



More about Neural Nets for Analyzing data

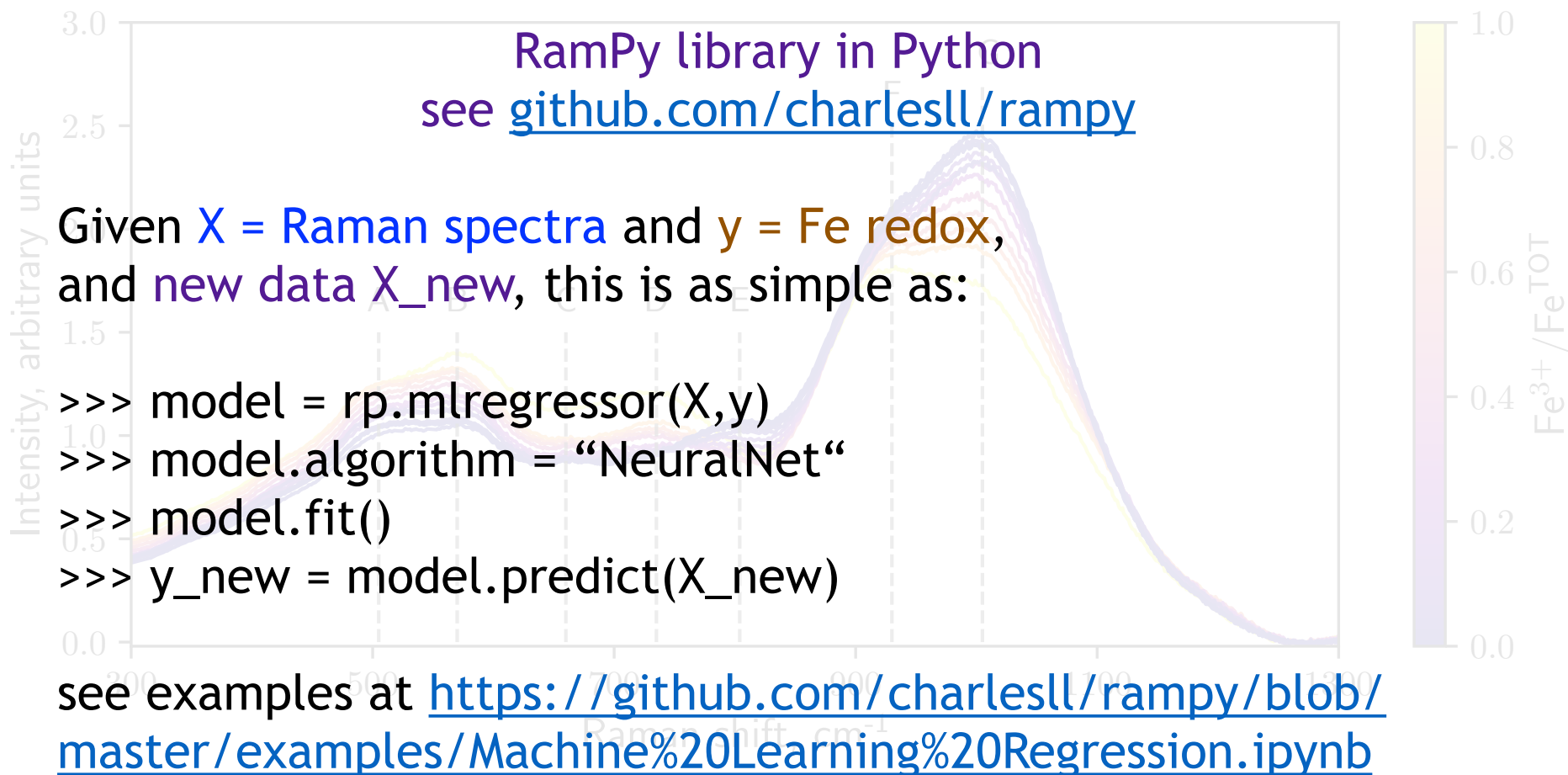
example: Raman spectra of Fe-bearing CMAS glasses

RamPy library in Python
see github.com/charlesll/rampy

Given X = Raman spectra and y = Fe redox,
and new data X_{new} , this is as simple as:

```
>>> model = rp.mlregressor(X,y)
>>> model.algorithm = "NeuralNet"
>>> model.fit()
>>> y_new = model.predict(X_new)
```

see examples at <https://github.com/charlesll/rampy/blob/master/examples/Machine%20Learning%20Regression.ipynb>



Classification of boninite magmas

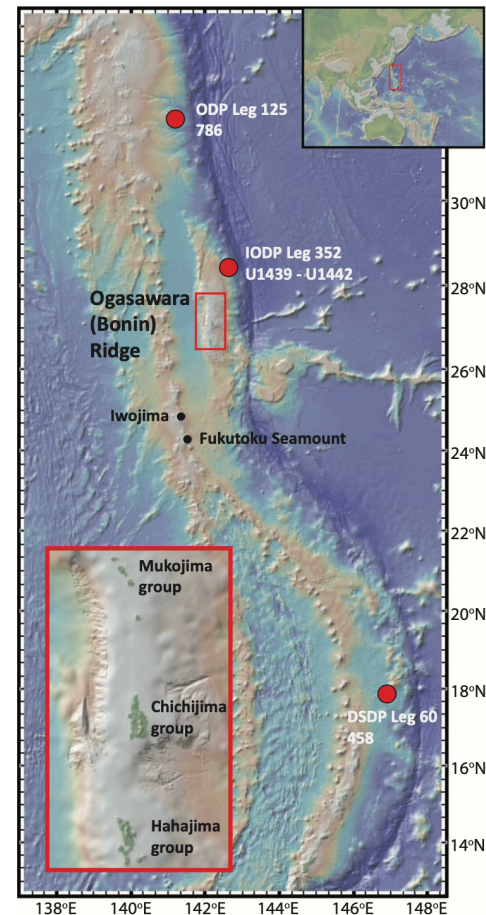
> MgO-rich & TiO₂ poor magmas, formed by partial melting of clinopyroxene-bearing harzburgite sources

> Different sources = different trends, difficult to distinguish in MgO-SiO₂

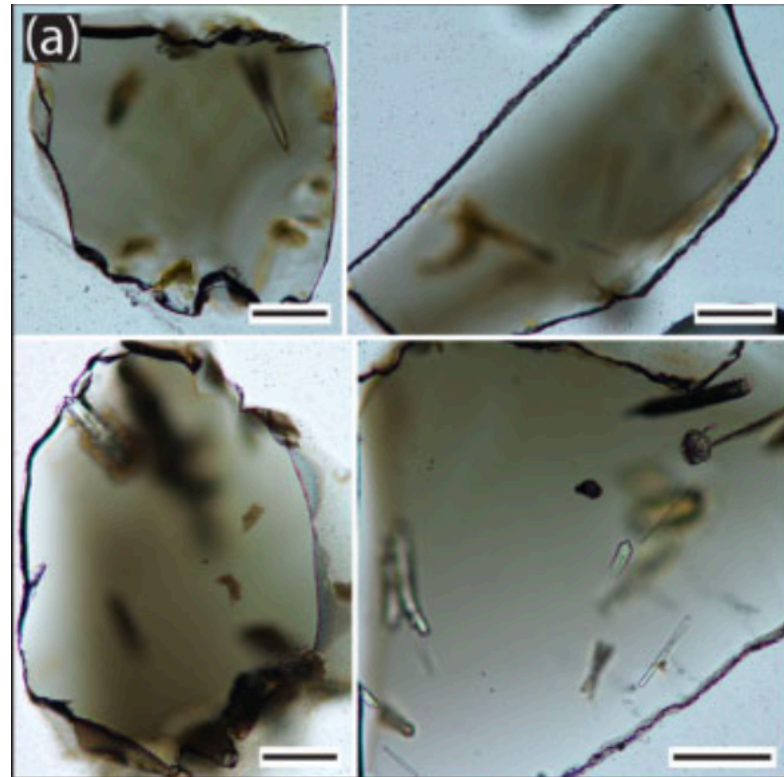
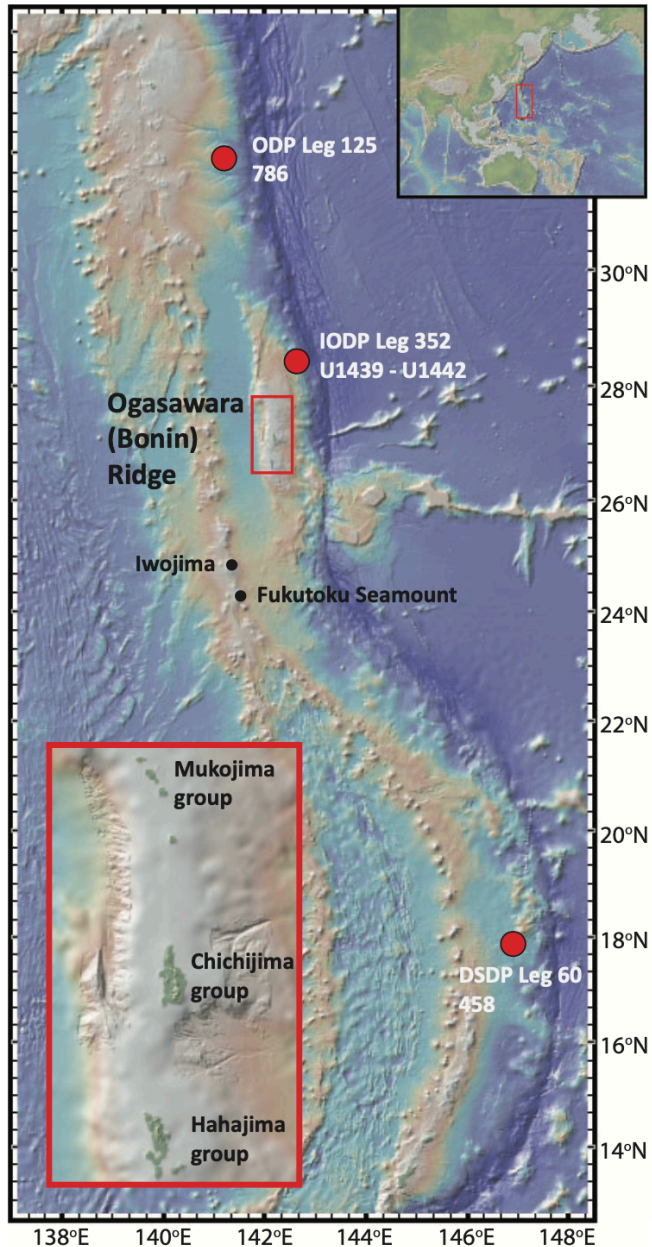
> For Ogasawara Ridge
(Kanayama et al. 2012):

- HSB: High Silica Boninite
- LSB: Low Silica Boninite

LSB = less depleted mantle source, lower T



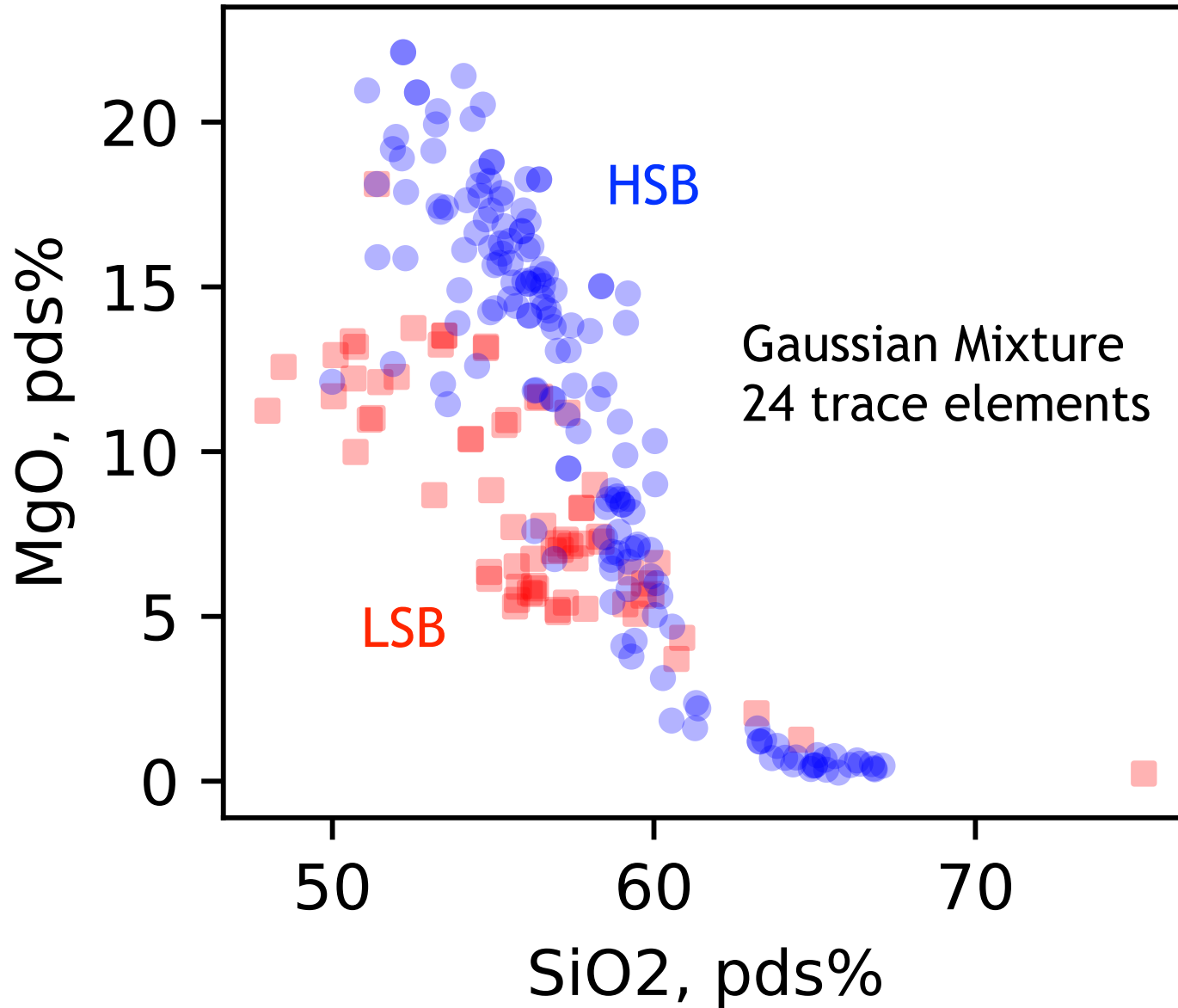
Classification of boninite magmas



bars = 100 microns

glass shards analysis (major elements + trace analysis)

Classification of boninite magmas



Classification of boninite magmas

- > Different sources = different trends, difficult to distinguish in MgO-SiO₂
- > Easy for a Gaussian mixture classification algorithm, unsupervised, trained on REE LA-ICP-MS data

Valetich, Le Losq, Arculus, Umino, Mavrogenes, Journal of Petrology 2021

github.com/charlesll/boni-and-class

