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## Numerical simulation of vitrification processes: Modeling of air bubbling in molten glass

Workshop on gases and bubbles in molten glasses | E. Sauvage

CEA-Marcoule, BP 17171, 30207 Bagnols sur Cèze, France

13 MAY 2016

## Summary

1- Vitrification technology presentation

2- Semi empirical approach

2-a Model presentation

2-b Interaction with mechanical stirring

2-c Bubbles columns interaction

3- VOF simulation



# CEA / AREVA Joint Vitrification Laboratory (LCV)



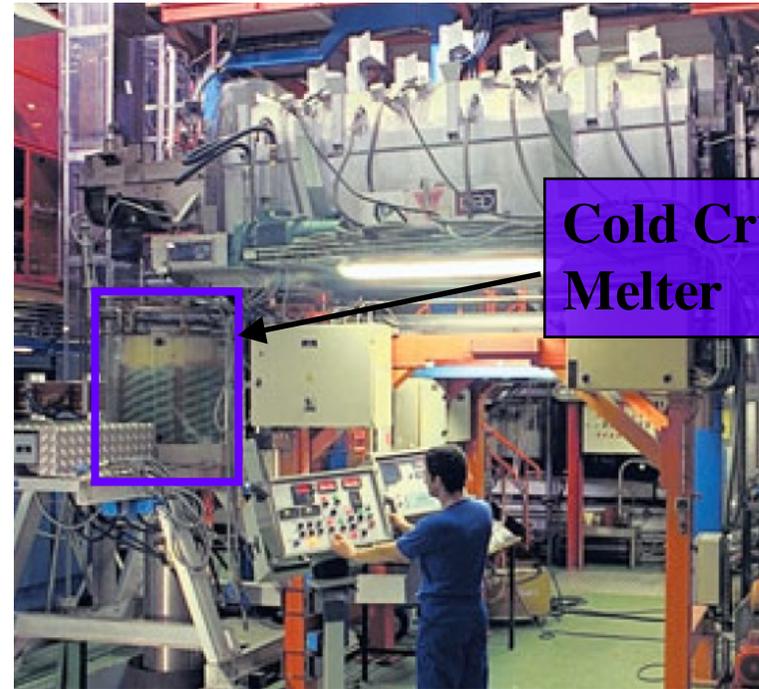
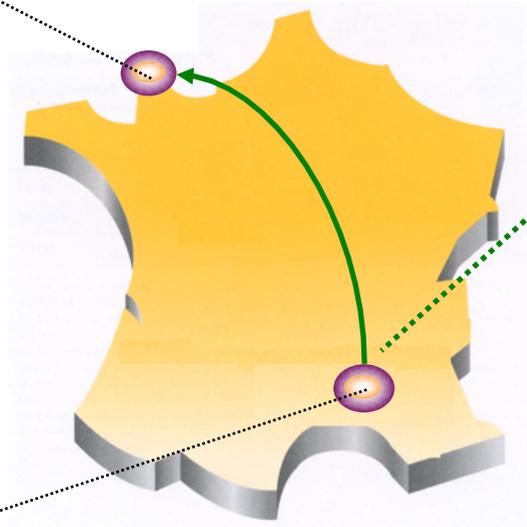
**La Hague  
(AREVA)  
Industrial plant**



**Marcoule  
(CEA)  
Research center**

## Areva

- Commercial and industrial operator of 3 vitrification plants



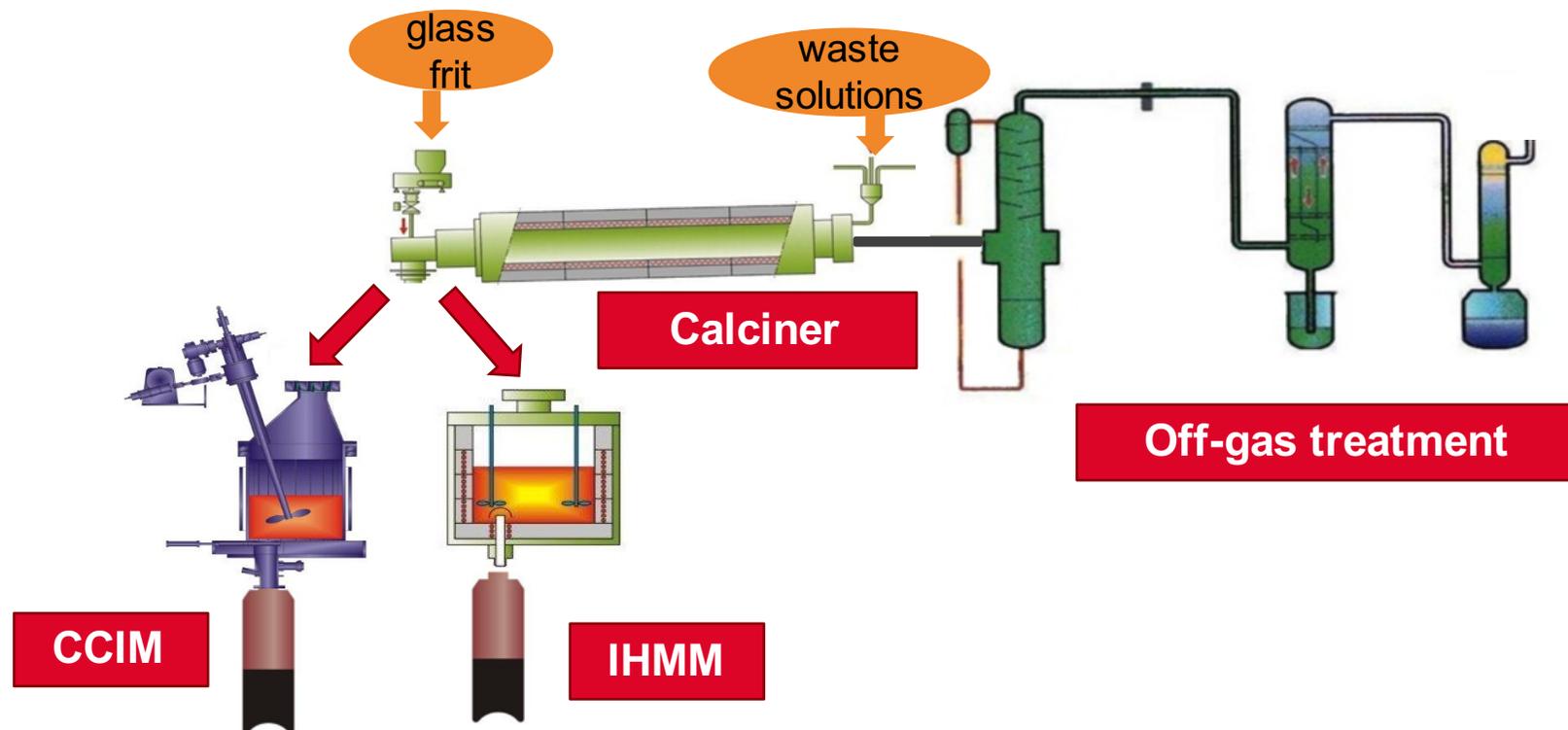
Current pilot of vitrification process  
CEA Marcoule (inactive cell)

## French Atomic Energy Commission (CEA)

- Confinement Research Engineering Department  
Waste Confinement and Vitrification Service

# VITRIFICATION PROCESS OPERATED IN THE LA HAGUE PLANT

## ➔ Industrial French Vitrification Design / A two-step vitrification process

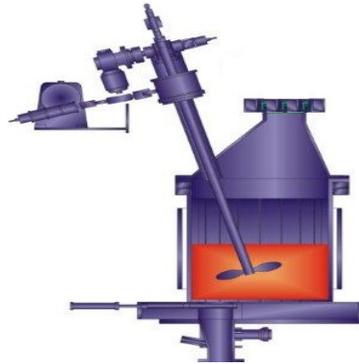


- ➔ Solution fed to a rotary calciner (evaporating, drying and calcining functions)
- ➔ Glass frit fed separately
- ➔ Melter fed continuously / poured batchwise
- ➔ Off-gas treatment unit (recycling of particulate material and purification of the gas streams)

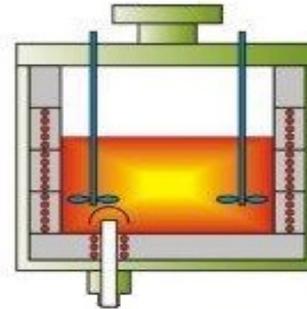
# VITRIFICATION PROCESS OPERATED IN THE LA HAGUE PLANT

## Furnaces technology

### Cold Crucible Inductive Melter



### Inductive Hot Metallic Melter



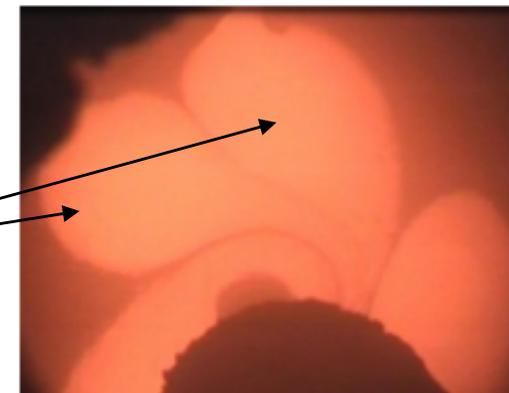
Average chemical compositions for R7T7 glass produced in the industrial facilities at La Hague

Oxides	Average composition of industrial glass (w %)
SiO <sub>2</sub>	45,6
B <sub>2</sub> O <sub>3</sub>	14,1
Al <sub>2</sub> O <sub>3</sub>	4,7
Na <sub>2</sub> O	9,9
CaO	4
Fe <sub>2</sub> O <sub>3</sub>	1,1
NiO	0,1
Cr <sub>2</sub> O <sub>3</sub>	0,1
P <sub>2</sub> O <sub>5</sub>	0,2
Li <sub>2</sub> O	2
ZnO	2,5
Oxides (PF+Zr+actinides) + Suspension of fines Actinide oxides	17
SiO <sub>2</sub> +B <sub>2</sub> O <sub>3</sub> +Al <sub>2</sub> O <sub>3</sub>	64,4

### Characteristics:

- Molten glass mass	400 kg	270 kg
- Max throughput	36 kg/h	25 kg/h
- Max temperature	>1400°C	1100°C
- Mechanical stirring	yes	yes
- Gas bubbling	yes	yes
- Approx. life time	>2 years	0.5 year
- Number in LH plant	1	5

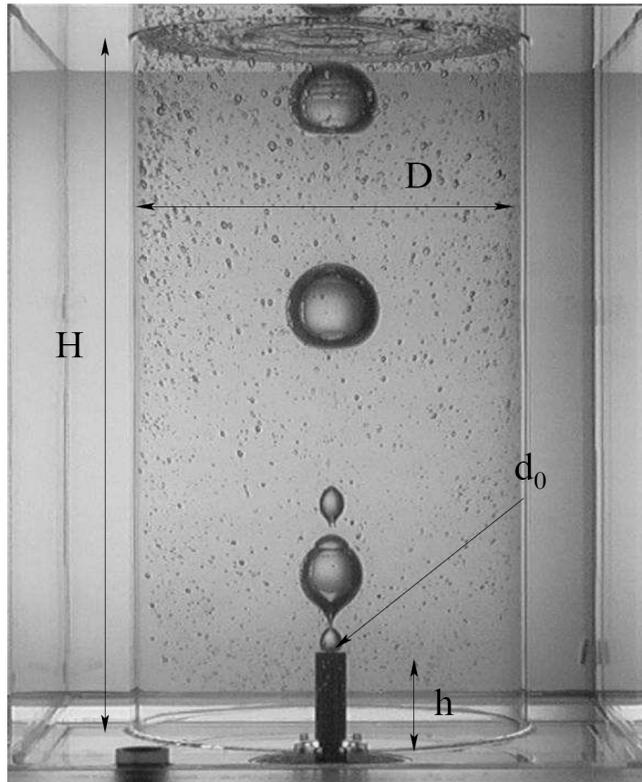
Inside view in CCIM



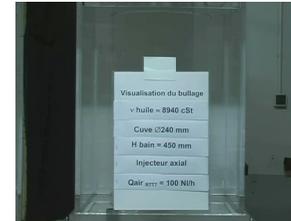
## Air bubbling overview

Experiment in hydraulic similarity with silicon oil

R. RIVA (CEA/ Grenoble)



30 to 60 cm



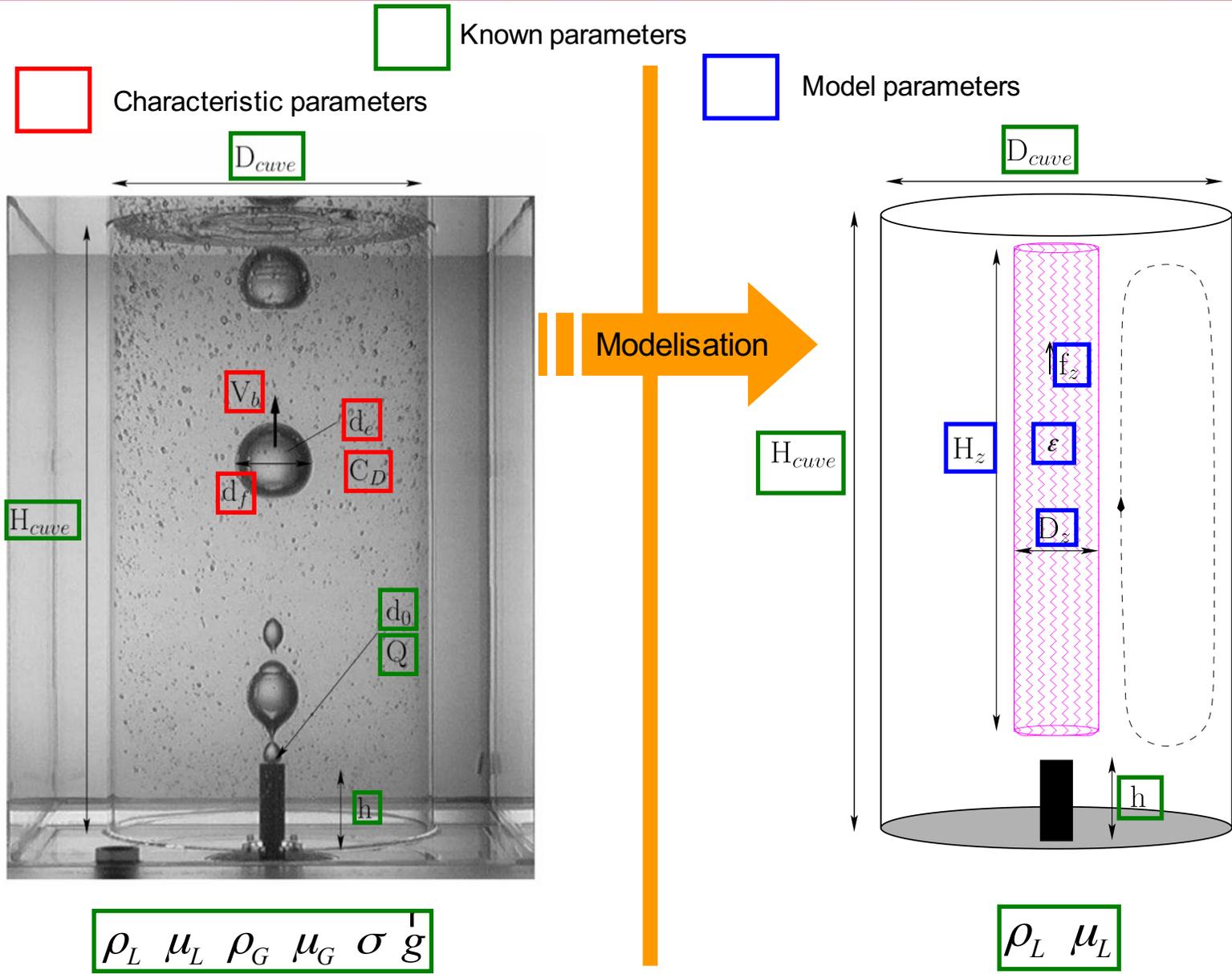
Visualisations  
rapides 250 im/s  
1 bullage  
Qair = 50 NI/h  
à Qair = 1000 NI/h  
Viscosité = 3890 cSt

- Oil with the same kinematic viscosity as glass (at a given temperature)
- Explored parameters: liquid viscosity, air flow rate, hole diameter of the injector...

Adimensionnals numbers for similarity

		Hot glass	Oil
$Mo$	$g\mu_L^4 / \rho_L \sigma^3$	1321	170616
$\log_{10}(Mo)$		3,12	5,23
$Ga$	$\rho_L^2 g d_0^3 / \mu_L^2$	0,0475	0,0475
$Re$	$\rho_L V_g d_0 / \mu_L$	63,2	63,2
$\rho^*$	$\rho_G / \rho_L$	$8,55 \cdot 10^{-5}$	$1,23 \cdot 10^{-3}$
$\mu^*$	$\mu_G / \mu_L$	$5,26 \cdot 10^{-6}$	$5,12 \cdot 10^{-6}$

# 2-a « One mesh » model



Nomenclature :

$Q$  Gas flow rate (L/h)

$g$  Gravity ( $m/s^2$ )

$d_0$  Orifice diameter (m)

$V_g$  Gas velocity (m/s)

$V_B$  Bubble rising velocity (m/s)

$d_e$  Equivalent diameter of bubble (m)

$f_z$  Body force imposed in the fluid ( $N/m^3$ )

$C_d$  Drag coefficient (-)

$V_{ol}$  Volume of a bubble ( $m^3$ )

$p$  Liquid pressure (Pa)

$\rho_L$  Liquid density ( $kg/m^3$ )

$\mu_L$  Liquid viscosity ( $m^2/s$ )

$\epsilon_g$  Volume fraction of gas

## 2-a « One mesh » model

□ = f( □ ) = experimental correlation

Jamialahmadi, M. et al, Study of Bubble Formation Under Constant Flow Conditions, *Chemical Engineering Research and Design*, **2001**, 79, 523 - 532

$$d_e = d_0 \left( \frac{5}{Bd^{1,08}} + 9,261 \frac{Fr^{0,36}}{Ga^{0,39}} + 2,147 Fr^{0,51} \right)^{\frac{1}{3}}$$

$\rho_L g d_0^2 / \sigma$

$\rho_L^2 g d_0^3 / \mu_L^2$

$V_g^2 / g d_0$

$$d_f = 1,23 d_e$$

□ = f( □ , □ ) = choice of model

Snabre, P. & Magnifotcham, F. Recirculation flow induced by a bubble stream rising in a viscous liquid  
*The European Physical Journal B*, **1998**, 4, 379-38

$$H_z \approx H_{cuve} - h_{inj}$$

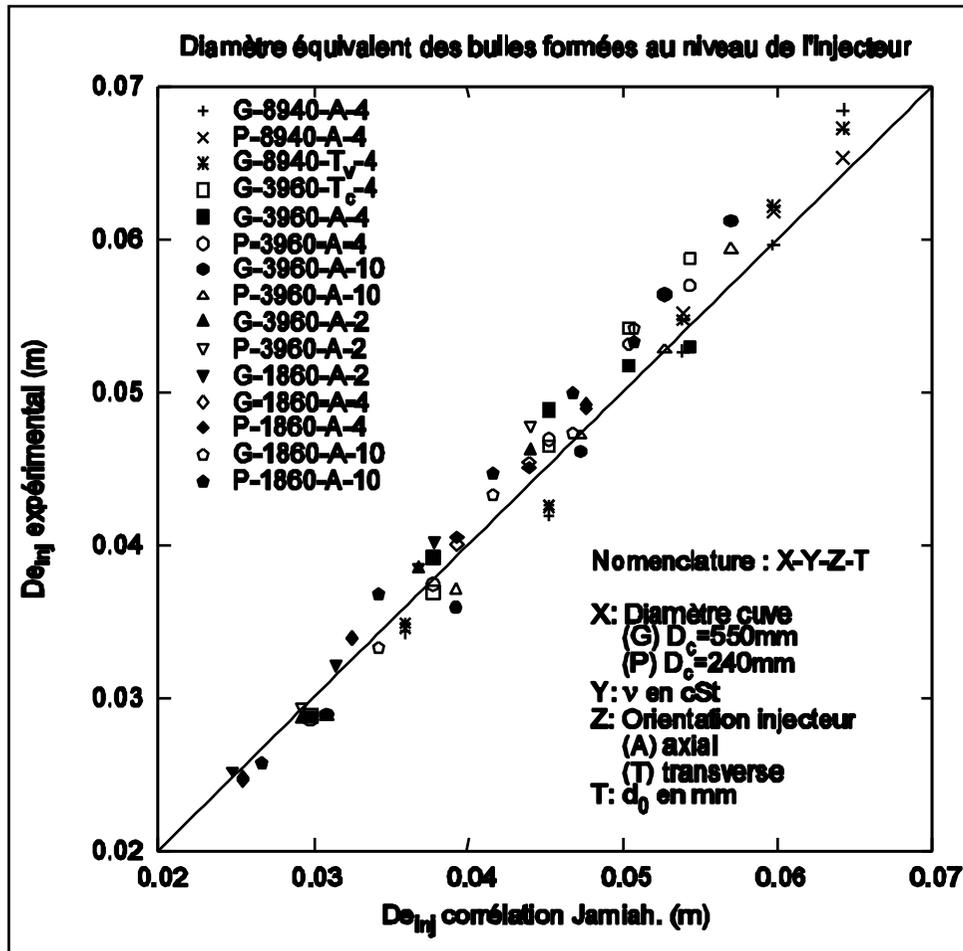
$$D_z \approx d_f$$

$$f_z \approx \rho g \varepsilon \quad [N m^{-3}]$$

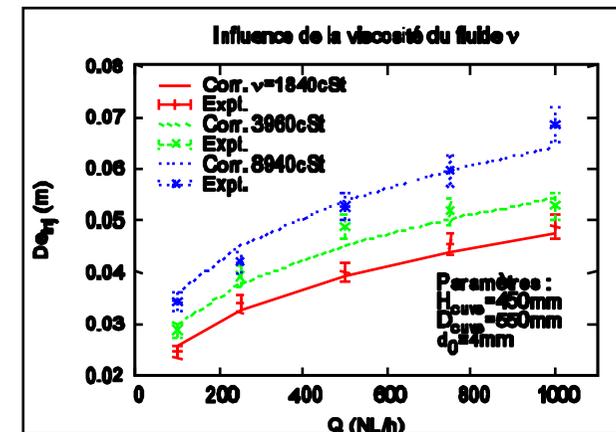
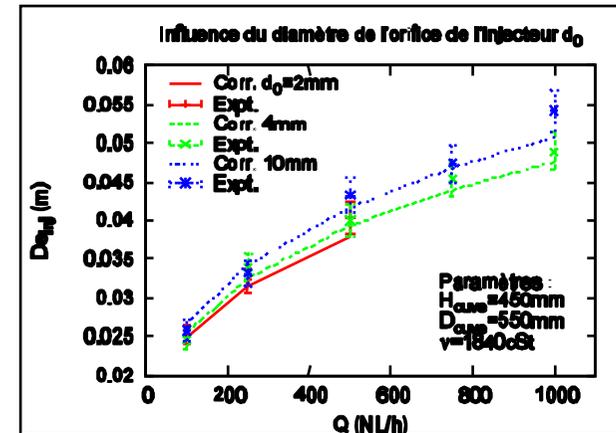
$$\varepsilon = \frac{2 \boxed{Qd_e}}{3 \boxed{V_B} V}$$

$$V_B^2 = \frac{4 d_e g (1 + \varepsilon)}{3 C_d}$$

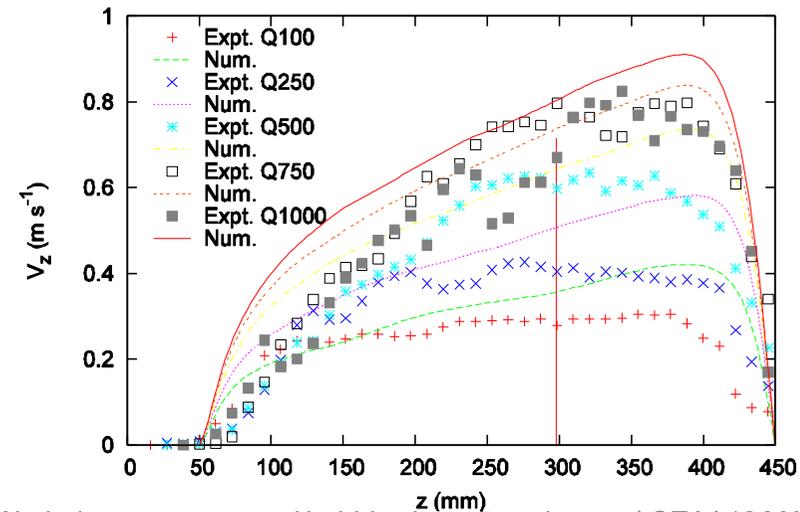
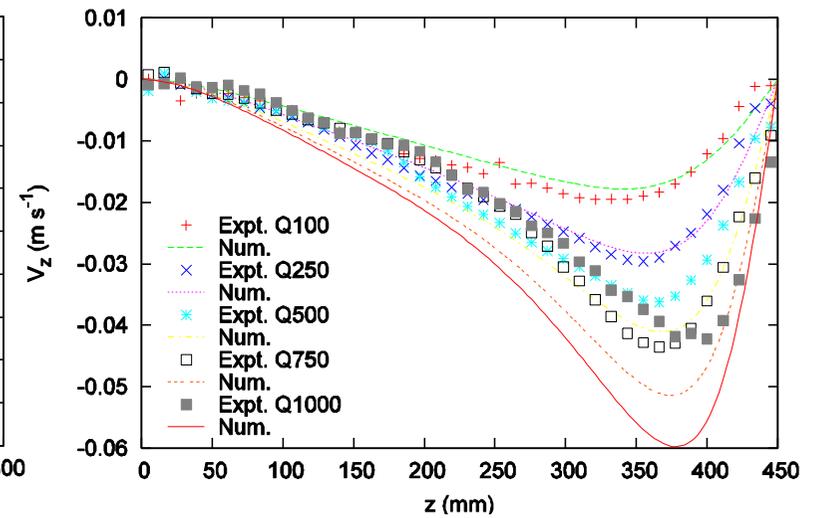
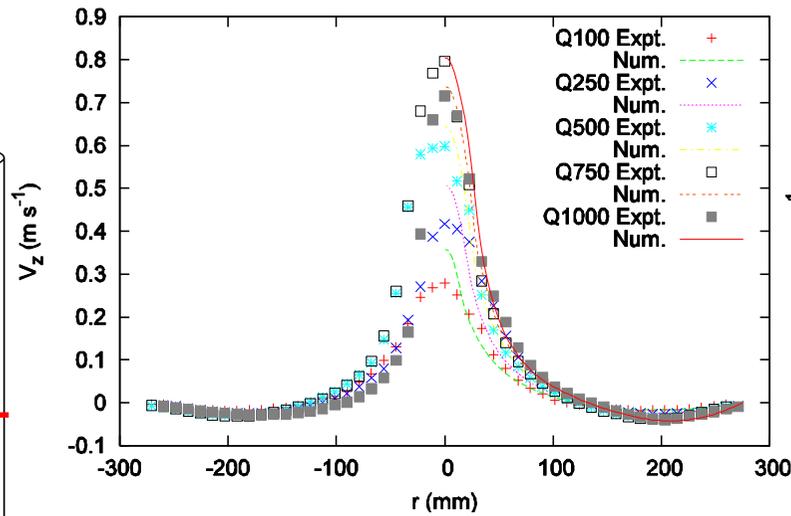
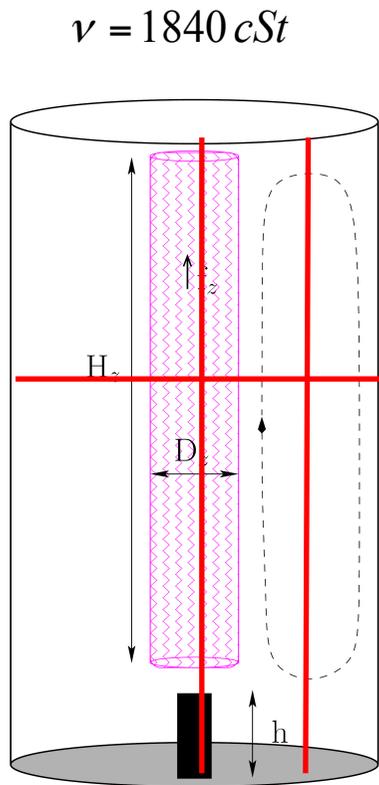
## Correlation for bubbles diameter



Jamialahmadi, M. et al, Study of Bubble Formation Under Constant Flow Conditions, *Chemical Engineering Research and Design*, 2001, 79, 523 - 532

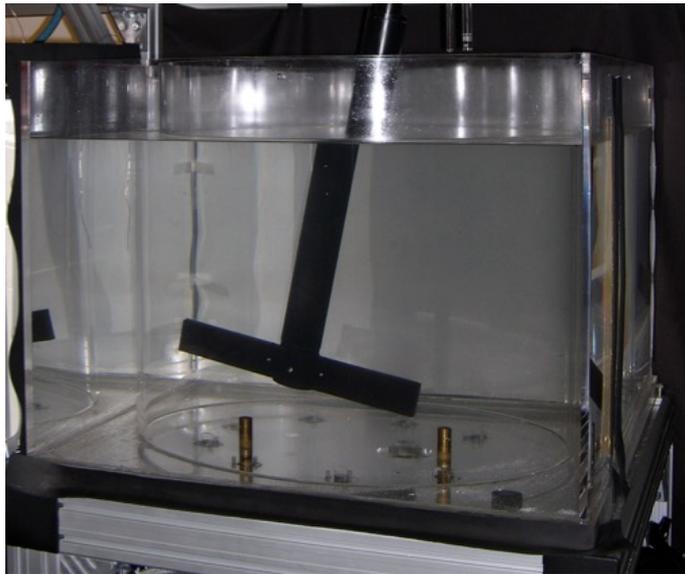


## PIV measurement vs numerical simulation

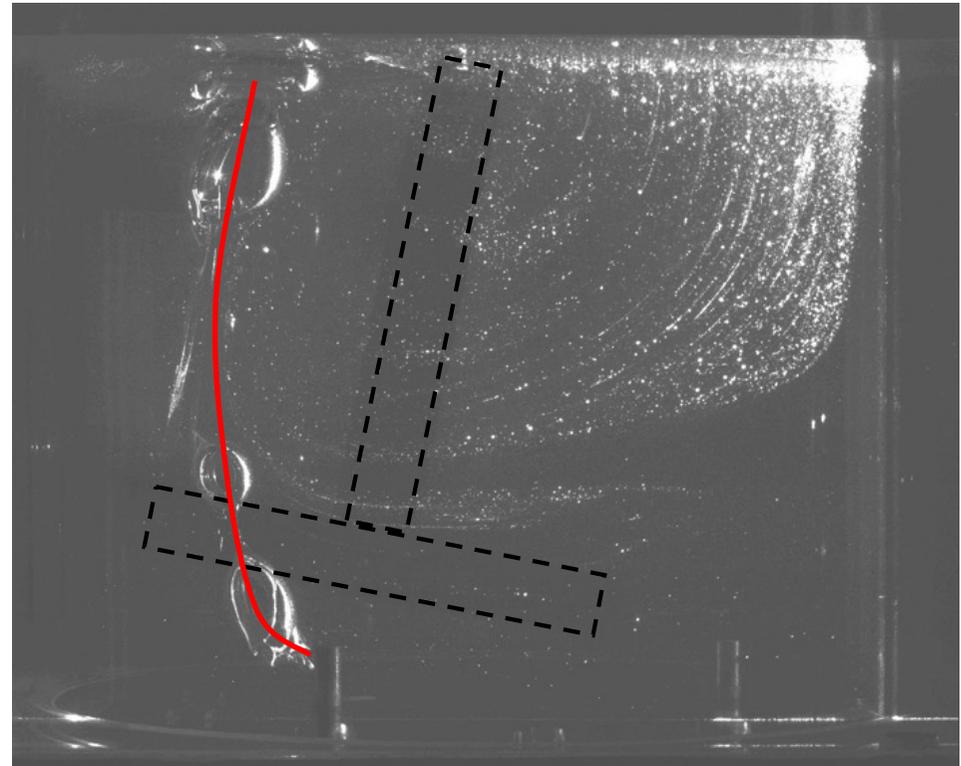


### Effect of external flow induced by the mechanical stirring

Experimental set-up



PIV measurement



Deviation of the bubble train trajectory

No influence of the rotating speed on the size of bubbles

### Trajectory of bubble train

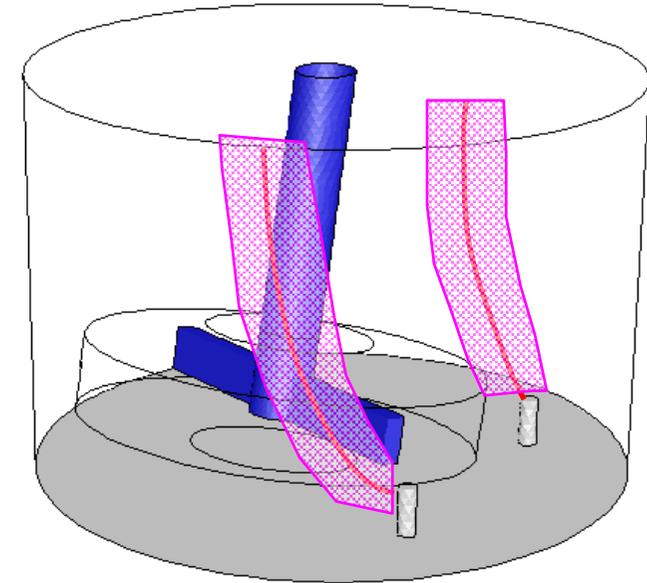
Lagrangian equation for the trajectory :

$$\frac{d\mathbf{u}_p}{dt} = F_D (\mathbf{u} - \mathbf{u}_p) + \frac{\mathbf{g}(\rho_p - \rho)}{\rho_p} + F_{\text{sup}}$$

Drag force  $F_D = \frac{18\mu}{\rho_p d_p^2} \frac{C_D \text{Re}}{24}$

$$F_{\text{sup}} = \frac{1}{2} \frac{\rho}{\rho_p} \frac{d}{dt} (\mathbf{u} - \mathbf{u}_p) + \frac{\rho}{\rho_p} \mathbf{u}_p \frac{\partial u}{\partial x_i}$$

Added mass

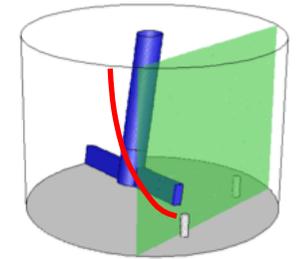


Specific drag coefficient :

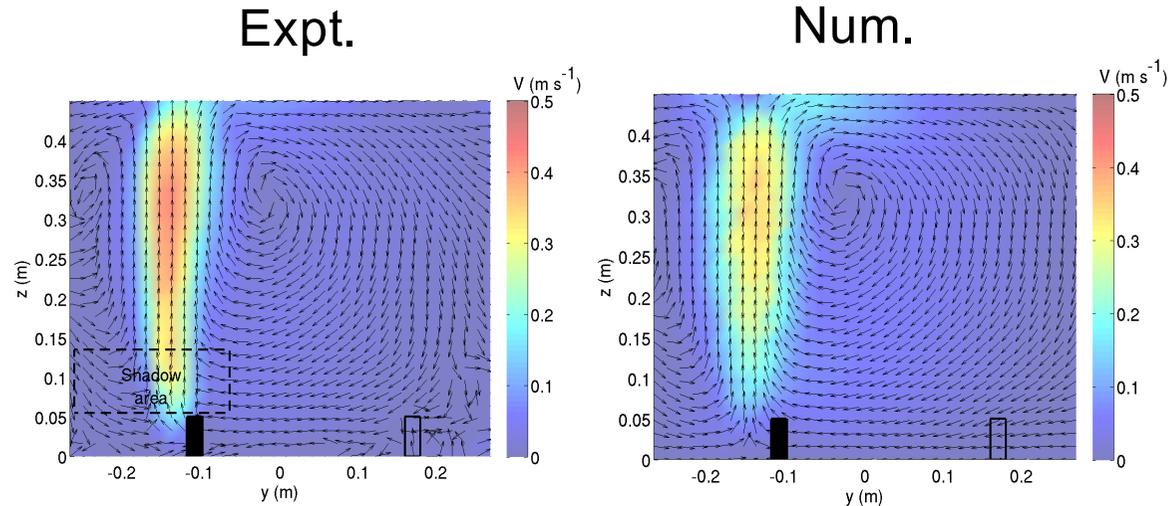
$$Cd = 1 + \frac{16}{\text{Re}}$$

with  $\text{Re} = \frac{\rho d_p |u_p - u|}{\mu}$

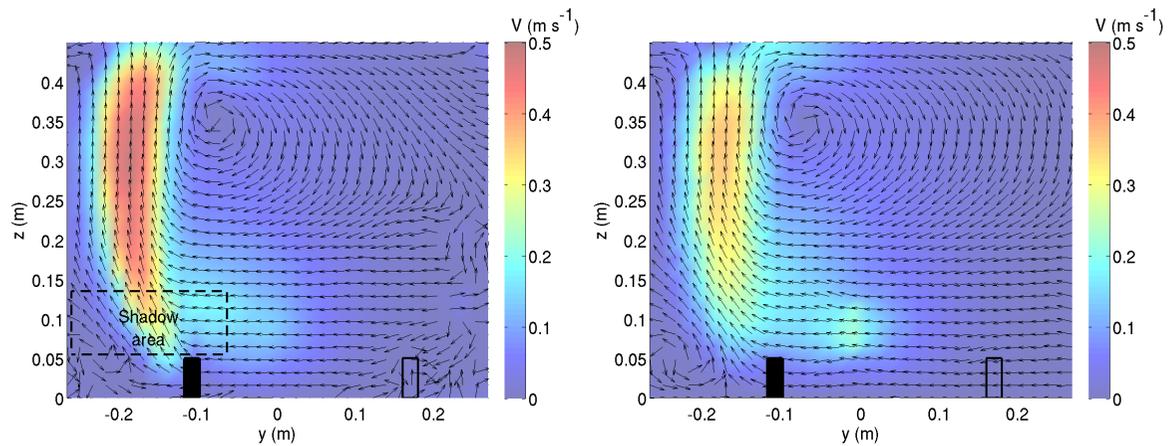
## With one Air Bubbler



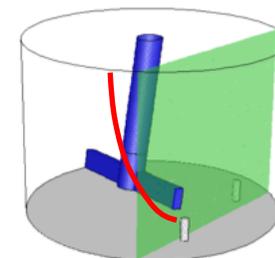
Stirring speed  
0 rpm



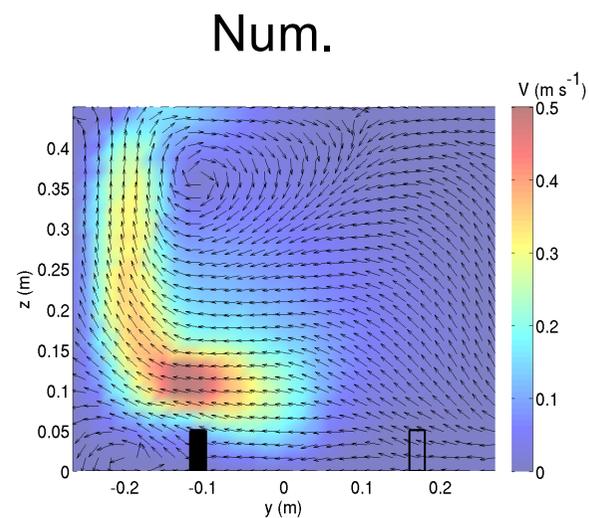
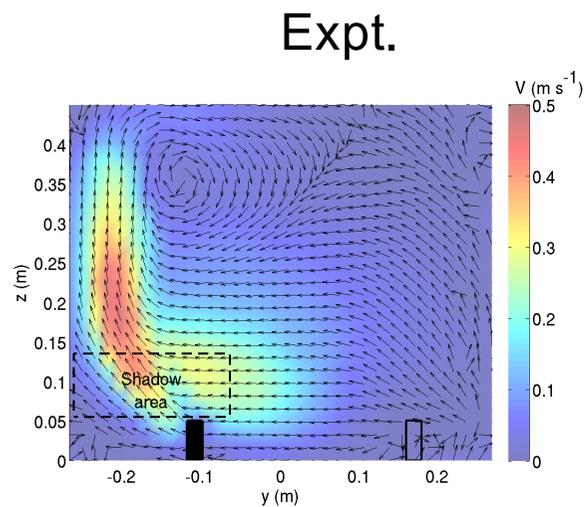
20 rpm



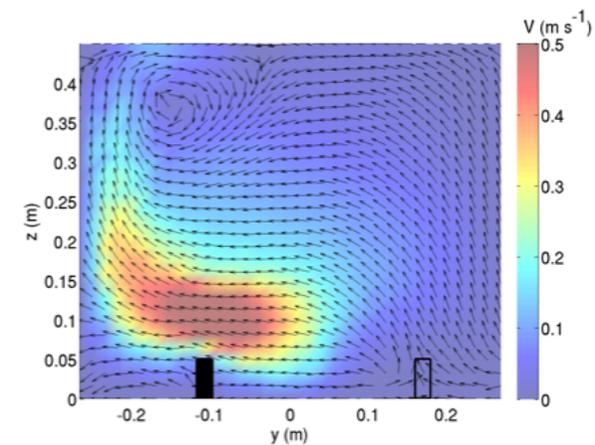
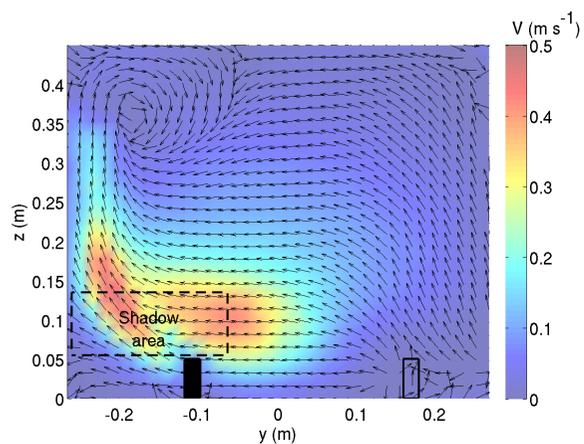
# 2-b Interaction with mechanical stirring



Stirring speed  
40 rpm



60 rpm



## Results

- A Semi empirical model, simple, validated in a specific range of bubbling, easy to set up in global calculation of the process.
- The interaction of mechanical stirrer is taken into account
  - Drawback : not predictive outside the range of validation.
- This model is used in our project of optimisation or conception of new vitrification furnace
- But some specific cases can't be simulated with this model

Visualisations  
rapides 250 im/s

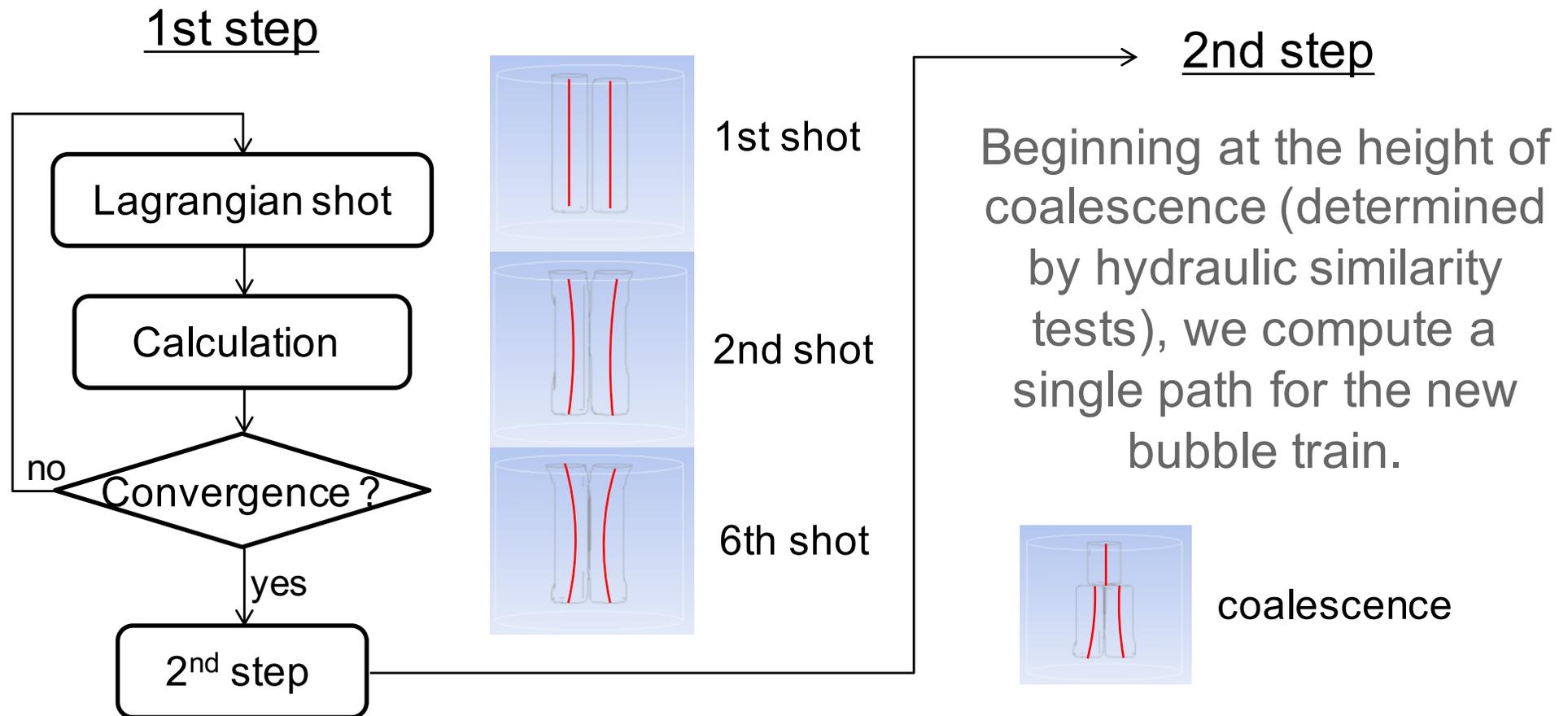
Coalescence de  
2 trains de bulles

$Q_{air} = 2 \times 100 \text{ NI/h}$   
à  $2 \times 500 \text{ NI/h}$

Ecartement = 60 mm

Viscosité = 3890 cSt

## Calculation steps with coalescence



D. Gautheron (SymHydro conference 2012)

### Modeling the gas-liquid interface

#### Volume Of Fluid (VOF) model equations

##### - Volume fraction of one phase

$$\frac{1}{\rho_L} \left[ \frac{\partial}{\partial t} (\varepsilon_L \rho_L) + \nabla \cdot (\varepsilon_L \rho_L \vec{v}_L) \right] = 0 \quad \varepsilon_L + \varepsilon_G = 1$$

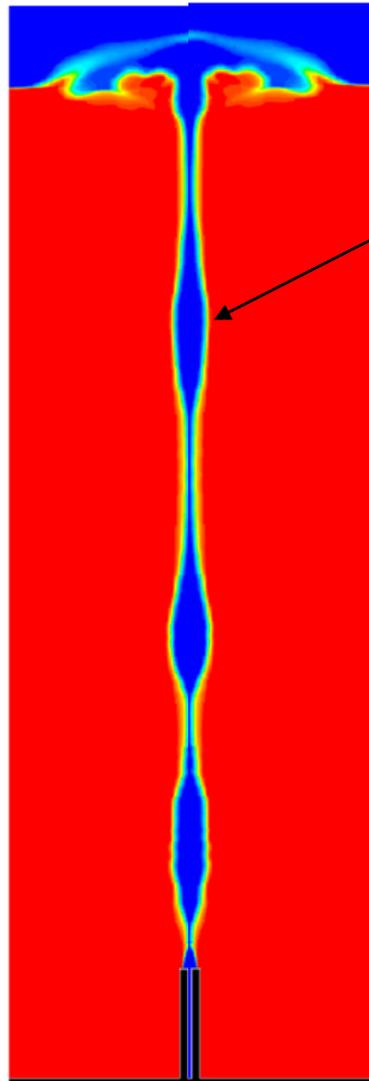
##### - Momentum equation

$$\frac{\partial}{\partial t} (\rho \vec{v}) + \nabla \cdot (\rho \vec{v} \vec{v}) = -\nabla p + \nabla \cdot [\mu (\nabla \vec{v} + \nabla \vec{v}^T)] + \rho \vec{g}$$

$$\rho = \varepsilon_L \rho_L + \varepsilon_G \rho_G \quad \mu = \varepsilon_L \mu_L + \varepsilon_G \mu_G$$

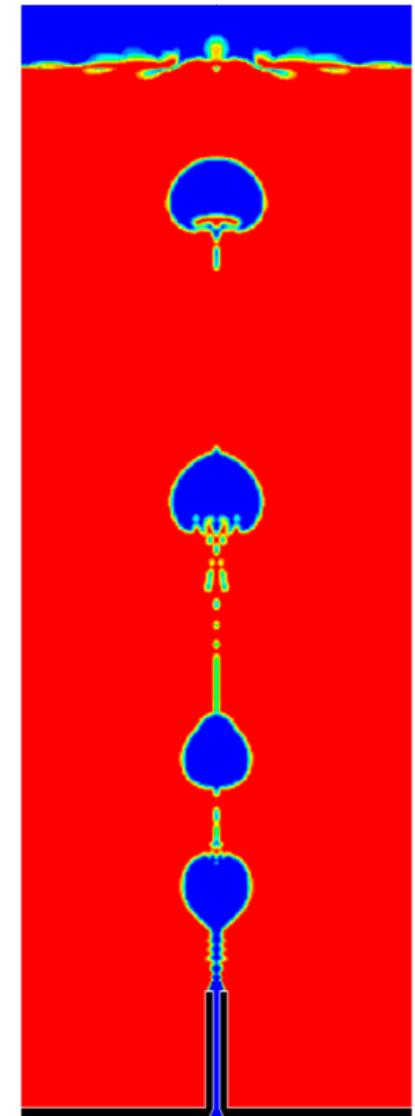
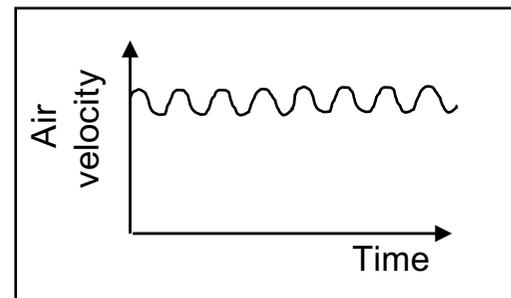
### 3 - Multiphase model

Problem :  
No bubbles  
are formed



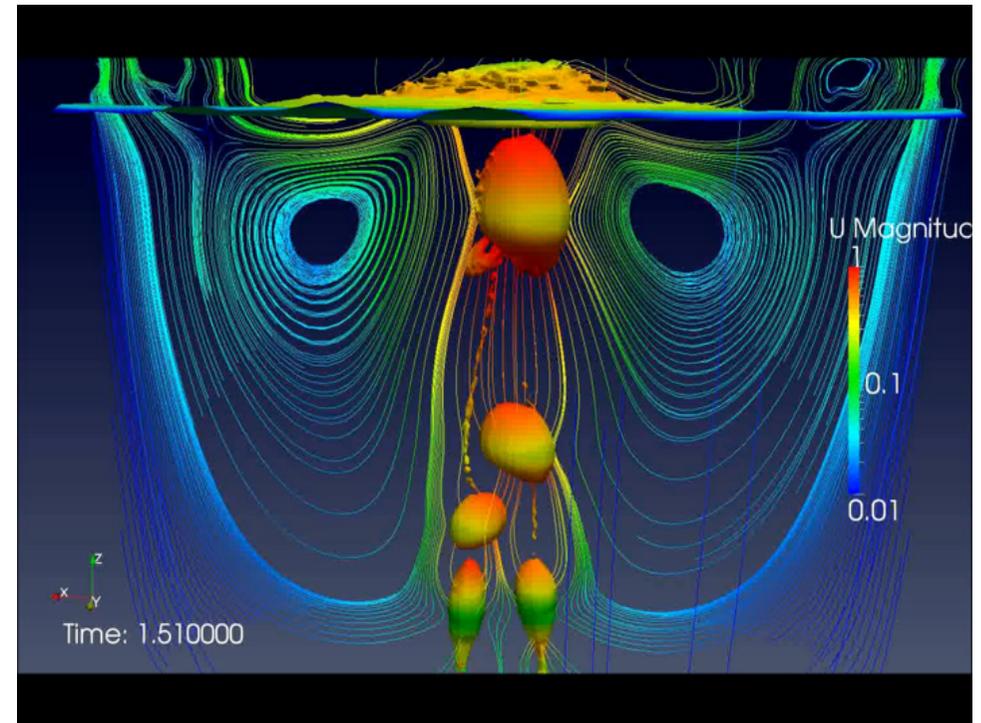
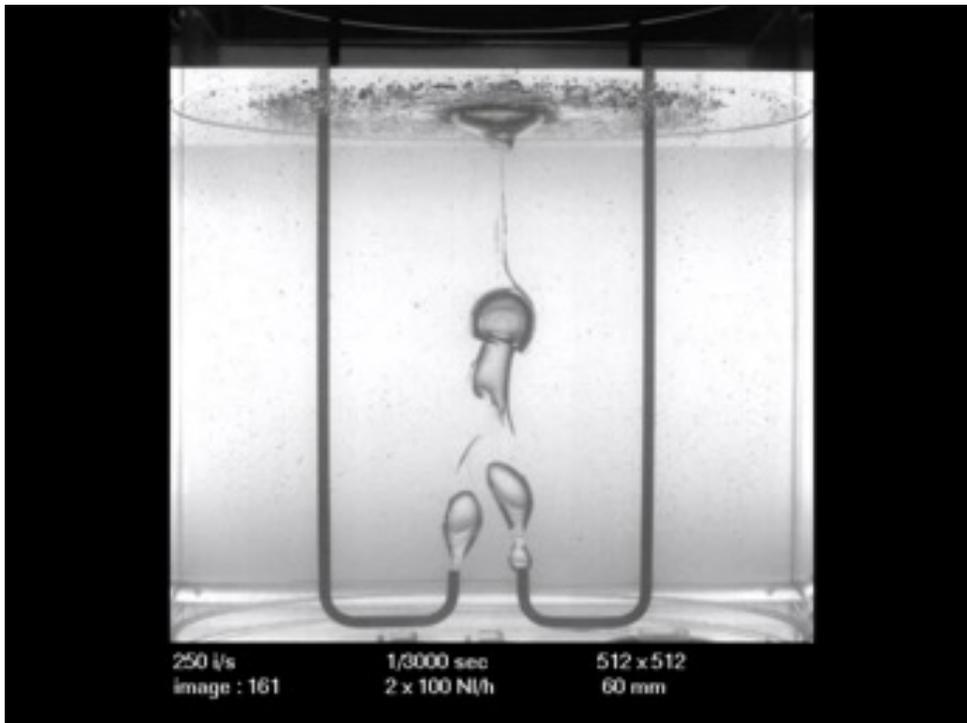
Air jet is a Rayleigh-Plateau instability. This instability should be numerically excited.

With high frequency modulation of the inlet air flow (300 Hz and 4% magnitude)



## 3- VOF Simulation

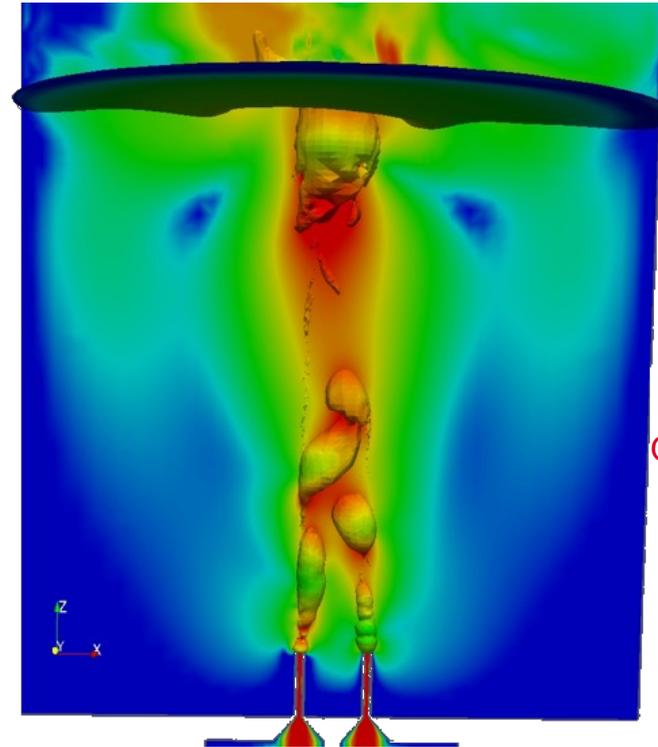
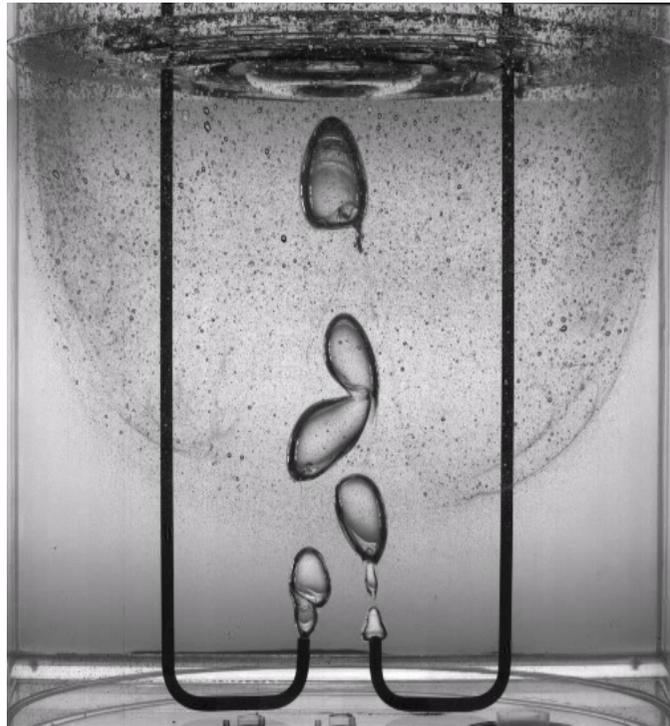
Complex diphasic flows have been successfully simulated.



Slow motion  
(real time / 10)

## Prospects : Multiphase model

**VOF model, very accurate and allowing to simulate complex configuration.  
Tool extremely useful to understand phenomena**



Openfoam software  
~2 millions mesh  
elements

Good qualitative agreement – No more experimental-based correlations

Drawback : Highly time consuming (1 week of calculation for 1 second simulated)



**Numerical Simulation of mixing molten glass with air bubbling is well advanced :**

**1 - A Semi empirical model, simple, validated in a specific range of bubbling, easy to set up in global calculation of the process.**

- The interaction of mechanical stirrer is taken into account
  - **Drawback : not predictive outside the range of validation.**

This model is used in our project of optimisation or conception of new vitrification furnace

**2 – A multiphase flow direct simulation (with VOF model) is used for specific studies involving very complex interface interaction**

## **Prospects :**

Include redox aspect

Thank you for your attention

Any questions ?

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