

# Propriétés des verres silicatés issues des bases de données et de la modélisation statistique

Exemple d'application : viscosité,  $T_g$



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Atelier TherMatHT USTV, Marcoule  
11/10/2019

Give researchers and engineers in glass science:

- A brief description of possible approaches for glass property modeling
- Basics on statistical modeling in formulation
  - Design of experiments, mixture designs
- Knowledge on database and Machine Learning for property prediction
  - Application example: viscosity and glass transition temperature prediction
- Information on where to find glass property data

## Three approaches to model a property

- Theoretical, cognitive approach

Based on our intrinsic knowledge of the phenomenon, on the fundamental laws of physics and chemistry (conservation of energy, momentum, equations of diffusion, thermodynamics,...)

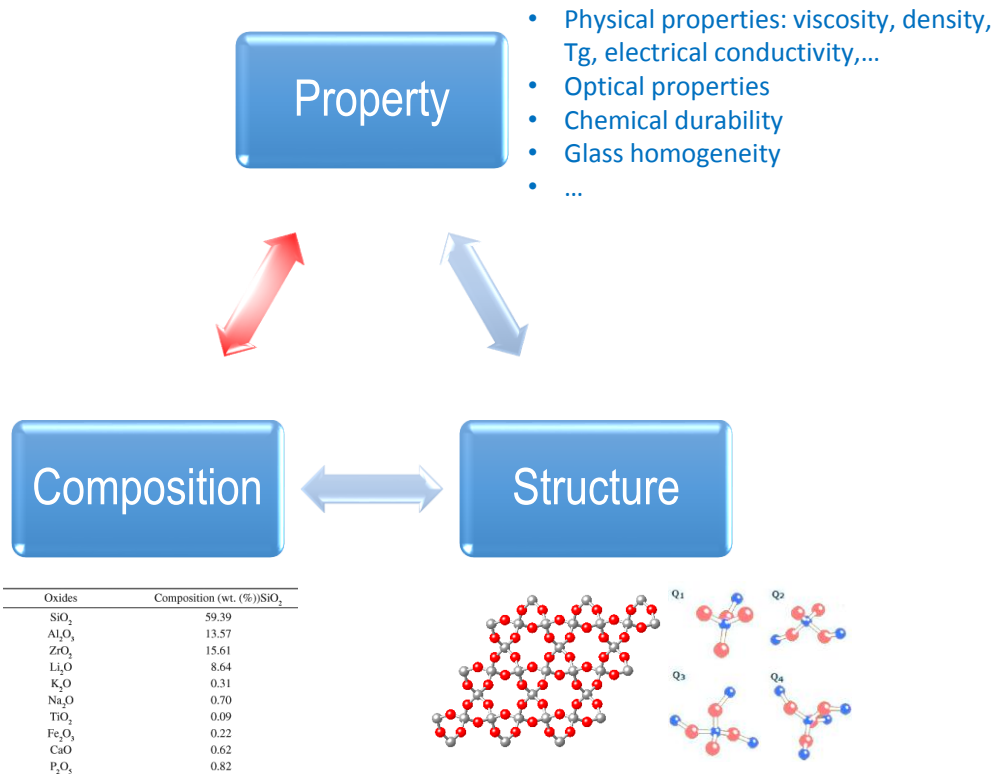
- Empirical approach

Based on a set of experimental data (*data-driven* models). Mathematical, statistical approach, which ignores any physicochemical knowledge of the phenomenon

- Mixed approach

Combination of the two previous approaches

- For these three classes of models, there are different types: linear or non-linear, static or dynamic, deterministic or stochastic, continuous or discrete,...



## Available resources in glass science and technology

- First attempt for the calculation of glass properties from their composition proposed by Winckelmann and Schott at the end of the 19<sup>th</sup> century
- Monograph by Volf in 1988 that describes best known methods [1]
- Since 1988 methods have been proposed for viscosity calculation (Lakatos, Lyon, Mazurin, Hrma, Priven, Okhotin, Fluegel,...)

[1] M.B. Volf, *Mathematical approach to glass*, Elsevier Science Publishers, Amsterdam (1988)

## Theoretical Principle of Additivity

M.B. Volf, *Mathematical Approach to Glass*, Elsevier Science Publishers, 1988

- If glass were a simple mixture of the individual oxides, the **additive equation** would be generally valid:

$$G = \sum g(G)_i x_i$$

$G$  is the property of the glass

$g(G)_i$  is the additive factor for oxide  $i$  and property  $G$

$x_i$  is the amount of oxide  $i$

- But glass is not a mixture of oxides... Errors in additive calculation could be due to the degree of cross-linking, anomalies in the cross-linked structure, phase separation, interaction between ions,...
- However, on investigating a suitably narrow composition range, where the more complex interactions can be neglected, **one can express the effect of the individual components on a certain property by the additive equation.**

## Two strategies for statistical property modeling

- Design of Experiments
- Database and Machine Learning

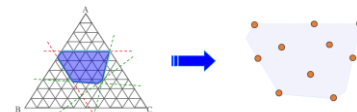
## Two strategies for statistical property modeling

### ■ Design of Experiments

- Models based on the additivity equation
- Very robust on *small* domains of composition
- Key points:

$$\hat{y}_i = \sum_{i=1}^q a_i x_i + \sum_{i=1}^{q-1} \sum_{j=i+1}^q a_{ij} x_i x_j$$

- Domain boundaries definition
- Definition of the optimal number of runs
- Model fit – avoid overfitting
- Model validation

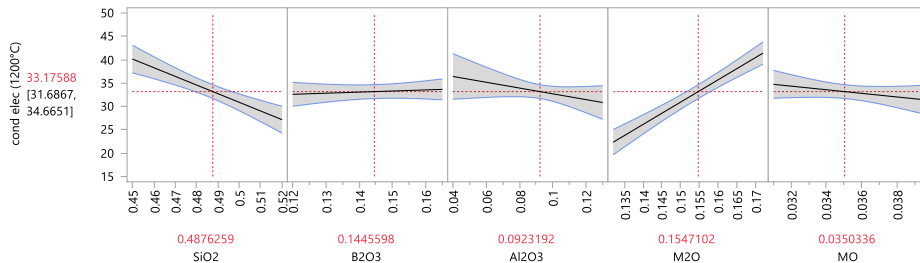
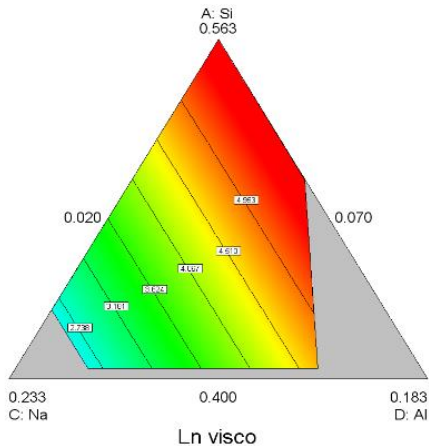


- Nice examples in nuclear glass formulation: viscosity, electrical conductivity, density, initial rate of dissolution



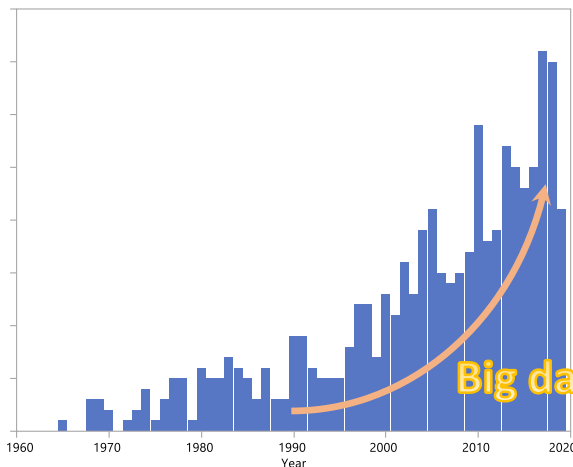
## Two strategies for statistical property modeling

### ■ Design of Experiments



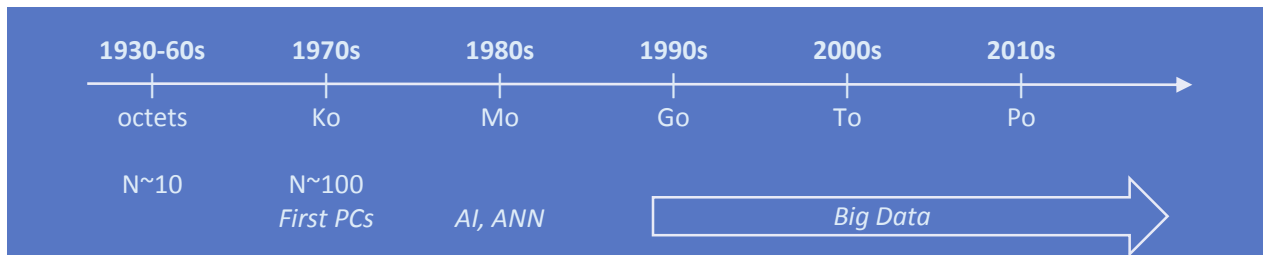
## ■ Database and Machine Learning

Published literature in the field of glass property prediction

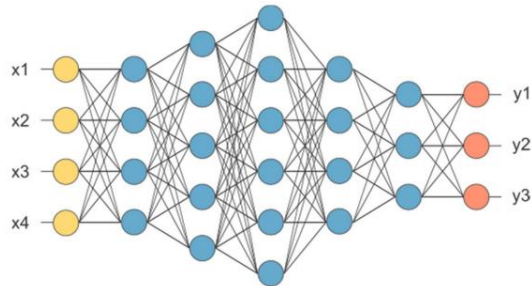
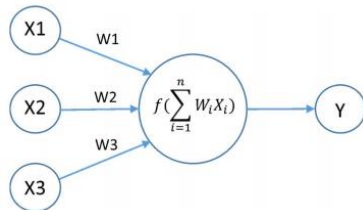


From Web of Science  
« glass » and « prediction » in publication title

Big data era

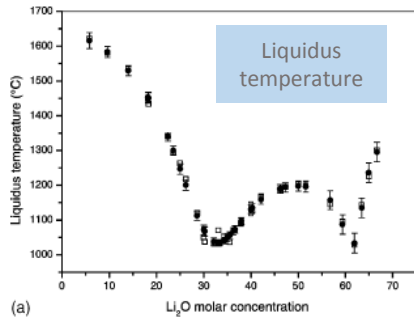


- Machine learning has seen growing application in material property determination
- Artificial Neural Networks (ANN) use interconnected mathematical nodes, or neurons, to form a network that can model complex functional relationships

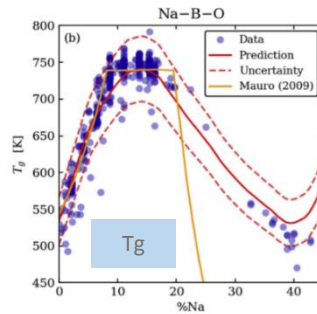


- This technique is particularly suited to problems that involve the manipulation of multiple parameters and non-linear interpolation

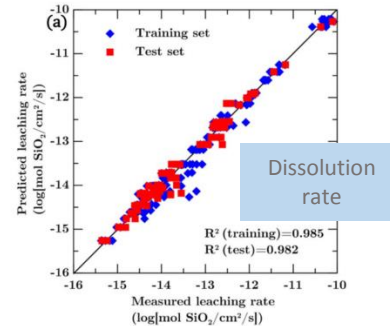
## Examples of NN application to glass property prediction



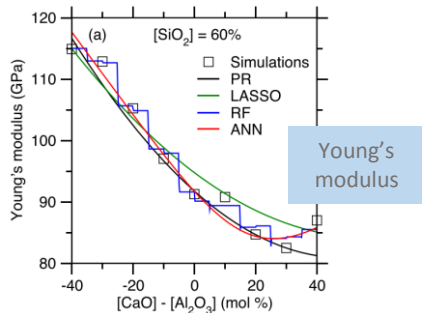
C. Dreyfus, G. Dreyfus / Journal of Non-Crystalline Solids 318 (2003) 63–78



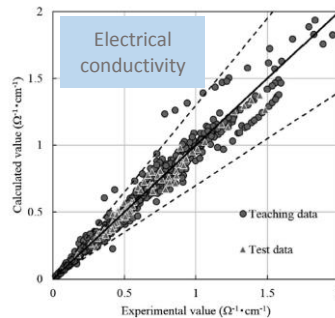
D.R. Cassar et al., Acta Materialia, 159 249-256 (2018)



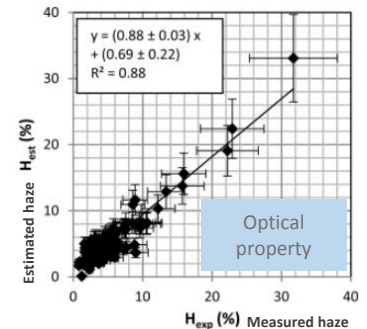
N.M. Anoop Krishnan et al. Journal of Non-Crystalline Solids 487 (2018) 37–45



K. Yang et al., Scientific Reports, 8739, 9 (2019)



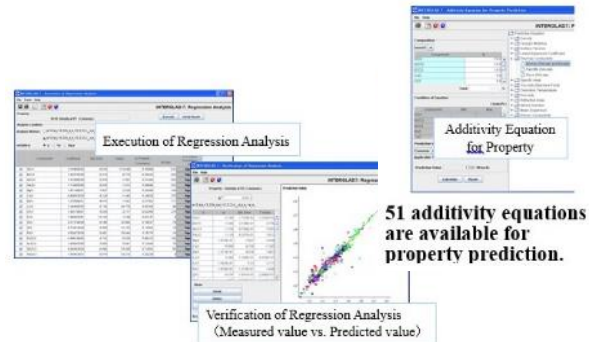
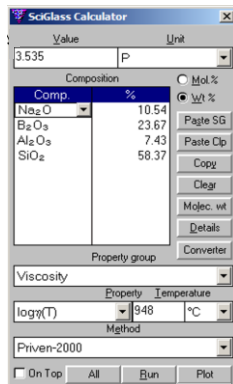
Y. Haraguchi et al., ISU International, Vol. 58 (2018), No. 6, pp. 1007–1012



A. Verney-Caron et al., Atmospheric Environment, 54 141-148 (2012)

## Available resources in glass science and technology

- SciGlass and InterGlad Information Systems
  - Data collected from the published literature
  - Embedded property calculation tools
  - More than 300 000 glasses



	Count
Number of glasses	374 405
By Number of Components	
One-component	4 785
Binary	64 689
Ternary	156 401
Four-component	46 658
Others	101 872
By Systems	
Oxide	278 477
Silicate ( $\geq 45$ mol.% $\text{SiO}_2$ )	115 423
Borate ( $\geq 45$ mol.% $\text{B}_2\text{O}_3$ )	37 158
Germanate ( $\geq 45$ mol.% $\text{GeO}_2$ )	10 558
Phosphate ( $\geq 40$ mol.% $\text{P}_2\text{O}_5$ )	23 334
Tellurite ( $\geq 30$ mol.% $\text{TeO}_2$ )	17 004
Halide	17 137
Chalcogenide	37 460

By Properties	Count
Acoustical properties	282
Chemical durability	34 290
Crystallization	26 577
Density	82 459
Density at 20°C	77 133
Density at 800°C	772
Density at 1000°C	1 066
Density at 1200°C	837
Density at 1400°C	987
Molar/spec. volume at 20°C	77 133
Dielectric properties	11 219
Diff., permeat., & solub. of gases	2 120
Elastic properties	14 748
Electrical resistivity	42 490
logr at 20°C	14 767
logr at 100°C	14 361
logr at 150°C	15 256
logr at 300°C	12 058
logr at 800°C	2 072
logr at 1000°C	2 632
logr at 1200°C	2 227
logr at 1400°C	2 218
TK-100	12 934
Glass formation	74 081

By Properties	Count
Heat capacity	3 357
C <sub>p</sub> at 20°C	926
C <sub>p</sub> at 200°C	675
C <sub>p</sub> at 400°C	511
C <sub>p</sub> at 800°C	320
C <sub>p</sub> at 1000°C	201
C <sub>p</sub> at 1200°C	186
C <sub>p</sub> at 1400°C	140
Internal friction	1 499
Ion diffusion	2 090
M <sub>g</sub>	18 040
Magnetic properties	4 725
Microhardness	13 746
Optical properties	71 613
Stress-optic coef.	1 231
Strength	3 663
Surface tension	5 128
s at T>T <sub>g</sub>	4 318
s at 900°C	771
s at 1200°C	951
s at 1300°C	1 384
s at 1400°C	830
T <sub>liq</sub>	53 517
T <sub>g</sub>	74 759
Thermal expansion coefficient	57 975
Thermal conductivity	1 700
Thermal diffusivity	901
Thermal endurance	1 117

	Count
Visc. standard points	17 542
Littleton Point	3 771
Annealing Point	3 907
Strain Point	5 948
Softening Point	7 763
Viscosity	37 205
$T_1$ (log[h,P]=1)	4 377
$T_2$ (log[h,P]=2)	5 653
$T_3$ (log[h,P]=3)	10 247
$T_4$ (log[h,P]=4)	9 746
$T_5$ (log[h,P]=5)	5 673
$T_6$ (log[h,P]=6)	5 260
$T_7$ (log[h,P]=7)	4 911
$T_8$ (log[h,P]=8)	5 236
$T_9$ (log[h,P]=9)	5 495
$T_{10}$ (log[h,P]=10)	6 044
$T_{11}$ (log[h,P]=11)	6 512
$T_{12}$ (log[h,P]=12)	6 330
$T_{13}$ (log[h,P]=13)	5 141

	Count
Viscosity	37 205
logh at 500°C	2 128
logh at 600°C	3 681
logh at 700°C	4 006
logh at 800°C	4 409
logh at 900°C	4 937
logh at 1000°C	5 403
logh at 1100°C	6 147
logh at 1200°C	7 424
logh at 1300°C	8 383
logh at 1400°C	8 831
logh at 1500°C	7 169
logh at 1600°C	3 703
logh at 1700°C	1 019
logh at 1800°C	396
logh at 2000°C	144
logh at 2200°C	44
logh at 2500°C	11



SciGlass Professional 7.10

Query Options Window Help

Unit settings: 10

### Queries for Tables

- Common Query
- Author Index
- Patent Index
- Trademark Index
- Subject Index
- Spectral Index
- Table by Number

### Queries for Glasses

- Experimental Data
- Predicted Properties
- Similar Compositions

### Ternary Diagrams

- Property Diagram
- Glass Formation

### Others

- SciGlass Calculator
- Database Browser
- SciGlass Statistics

Search for glasses belonging to a certain concentration range with prescribed values of experimentally measured properties

### Search for Glasses (Experimental Data)

Included	Min	Max	Excluded	System
SiO <sub>2</sub>				SiO <sub>2</sub>
B <sub>2</sub> O <sub>3</sub>				P <sub>2</sub> O
Na <sub>2</sub> O				RO
Al <sub>2</sub> O <sub>3</sub>				P <sub>2</sub> O <sub>3</sub>
CaO				RO <sub>2</sub>
MgO				P <sub>2</sub> O <sub>5</sub>
ZnO				RO <sub>3</sub>
MoO <sub>3</sub>				Halides
Fe <sub>3</sub> O <sub>4</sub>				Others

System Type: All

Required: 0.5 m%  
 Considered as components  
 Ignored

Kind of %: Molar %

Composition by analysis

Components To Search For:  
 Selected components only  
 Other components allowed  
 up to Any %

Property	Unit	Min	Max

And  Or

Clear Open... Run Close

SciGlass Professional 7.10

Query Options Window Help

10 Unit settings

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Included	Min	Max	Excluded	System	System Type
SiO <sub>2</sub>				SiO <sub>2</sub>	All
B <sub>2</sub> O <sub>3</sub>				P <sub>2</sub> O	
Na <sub>2</sub> O				RO	
Al <sub>2</sub> O <sub>3</sub>				P <sub>2</sub> O <sub>3</sub>	
CaO				RO <sub>2</sub>	
MgO				P <sub>2</sub> O <sub>5</sub>	

Kind of %

**List of Glasses (Experimental Data)**

Code	Glass #	Author	Year	Na <sub>2</sub> O	Density at 20°C, g/cm <sup>3</sup>
281	20790	Akimov V.V.	1960	15.0	2.335
281	20815	Akimov V.V.	1960	20.0	2.387
281	20843	Akimov V.V.	1960	25.0	2.431
281	20868	Akimov V.V.	1960	30.0	2.474
281	20878	Akimov V.V.	1960	33.3	2.490
454	22559	Matusita K.	1991	34.0	2.430
524	23704	Colbert W.	1946	25.0	2.415
521	23700	Safford H.W.	1947	50.0	2.580
548	24171	Heinemann I.	1993	33.3	2.487
557	141061	Dubrovo S.K.	1965	20.0	2.388
1572	9725	Harsell W.B.	1966	25.01	2.422
1572	9726	Harsell W.B.	1966	25.01	2.422

617 0 Mol.% Clear Close

Search for glasses belonging to a certain concentration range with prescribed values of experimentally measured properties

SciGlass Professional 7.10

Query Options Window Help

Unit settings: 10

Queries for Tables:

- Common Query
- Author Index
- Patent Index

Search for Glasses (Experimental Data)

Included	Min	Max	Excluded	System	System Type
SiO <sub>2</sub>				SiO <sub>2</sub>	All
B <sub>2</sub> O <sub>3</sub>				P <sub>2</sub> O	
Na <sub>2</sub> O				RO	
Al <sub>2</sub> O <sub>3</sub>				P <sub>2</sub> O <sub>3</sub>	

(33655) Brower W.S., 1972

Measurements of liquidus temperature by quenching method with error  $\pm 2.5$  K. Note. Numerical values were taken from a figure.

Reference:  
Brower W.S., Parker H.S., Roth R.S. and Waring J.L., Phase equilibrium and crystal growth in the system lithium oxide-molybdenum oxide, J.Cryst.Growth, 1972, vol. 16, No. 2, p. 115-120.

Glass Formation

Others:

- SciGlass Calculator
- Database Browser
- SciGlass Statistics

Search for glasses belonging to a certain concentration range with prescribed values of experimentally measured properties

454	22559	Matusita K.	1991	34.0	2.430
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1572	9726	Harsell W.B.	1966	25.01	2.422

Density at 20°C, g/cm<sup>3</sup>

- 2.335
- 2.387
- 2.431
- 2.474
- 2.490
- 2.430
- 2.415
- 2.580
- 2.487
- 2.388
- 2.422
- 2.422

617 0 Mol.% Clear Close

SciGlass Professional 7.10

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- Property Diagram
- Glass Formation

**Others**

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- Database browser
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Search for glasses belonging to a certain concentration range with prescribed values of experimentally measured properties

**Search for Glasses (Experimental Data)**

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Na <sub>2</sub> O				RO
Al <sub>2</sub> O <sub>3</sub>				P <sub>2</sub> O <sub>3</sub>
CaO				RO <sub>2</sub>
MgO				P <sub>2</sub> O <sub>5</sub>
ZnO				RO <sub>3</sub>
MoO <sub>3</sub>				Helides
Fe <sub>3</sub> O <sub>4</sub>				Others

**System Type**

All

requies: 0.5 m%  
 Considered as components  
 Ignored

**Kind of %**

Molar %

Composition by analysis

**Components To Search For**

Selected components only  
 Other components allowed  
up to Any %

Property	Unit	Min	Max
----------	------	-----	-----

And  Or

Clear Open... Run Close



SciGlass Calculator

Value: 2.346 Unit: P

Composition

Chemical	Value
SiO <sub>2</sub>	58.36
B <sub>2</sub> O <sub>3</sub>	23.67
Al <sub>2</sub> O <sub>3</sub>	7.43
Na <sub>2</sub> O	10.54

Mol. %  
 Wt %

Paste SG  
 Paste Clp  
 Copy  
 Clear  
 Molec. wt  
 Details  
 Converter

Property group: Viscosity

Property: log $\eta$ (T) Temperature: 1100 °C

Method: Priven-2000

On Top All Run Plot

Calculation results

Method	Result
Belousov and Akulova	-
Belousov and Firsov	-
Braginsky	-
Flom and Kotman	-
Flugel-2005	2.913
Giordano and Dingwell	-
Goto et al.	-
Hrma-2001	2.687
Hrma-95	4.012
Kozyukov and Mazurin	-
Lakatos-75	4.534
Lakatos-76	-
Lakatos-78	-
Lakatos-79	1.695
Leko	-
Lyon-74	2.237
Mazurin et al.	-
Okhotin	-
Priven (Na-Al-Si)	-
Priven-2000	2.346
Priven-98	3.118
Sasek	-
Shaw	-
Urbain et al.	-

Export Copy

SciGlass Calculator

Value: 2.346 Unit: P

Composition

Component	Value
SiO <sub>2</sub>	58.36
B <sub>2</sub> O <sub>3</sub>	23.67
Al <sub>2</sub> O <sub>3</sub>	7.43
Na <sub>2</sub> O	10.54

Mol.%  
 Wt.%

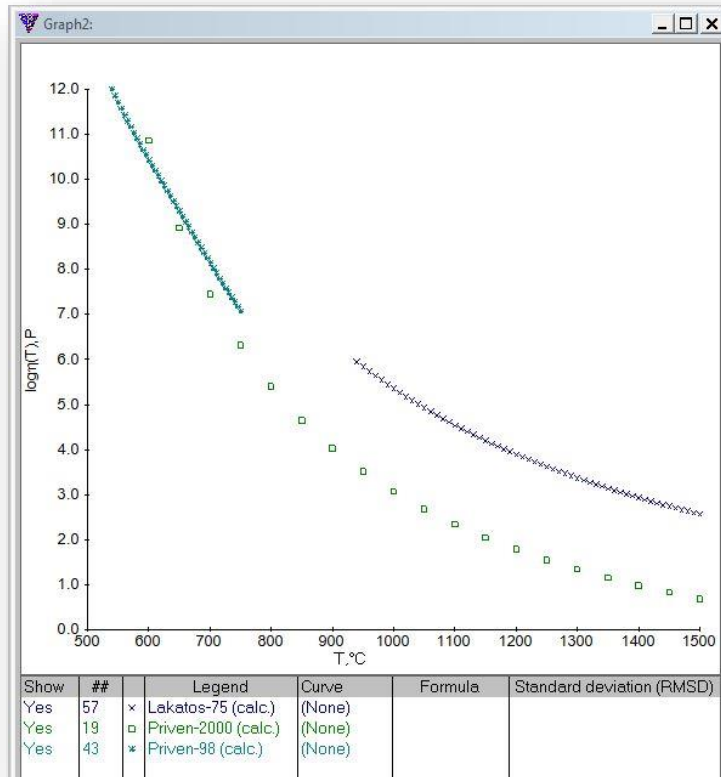
Paste SG  
 Paste Clp  
 Copy  
 Clear  
 Molec. wt  
 Details  
 Converter

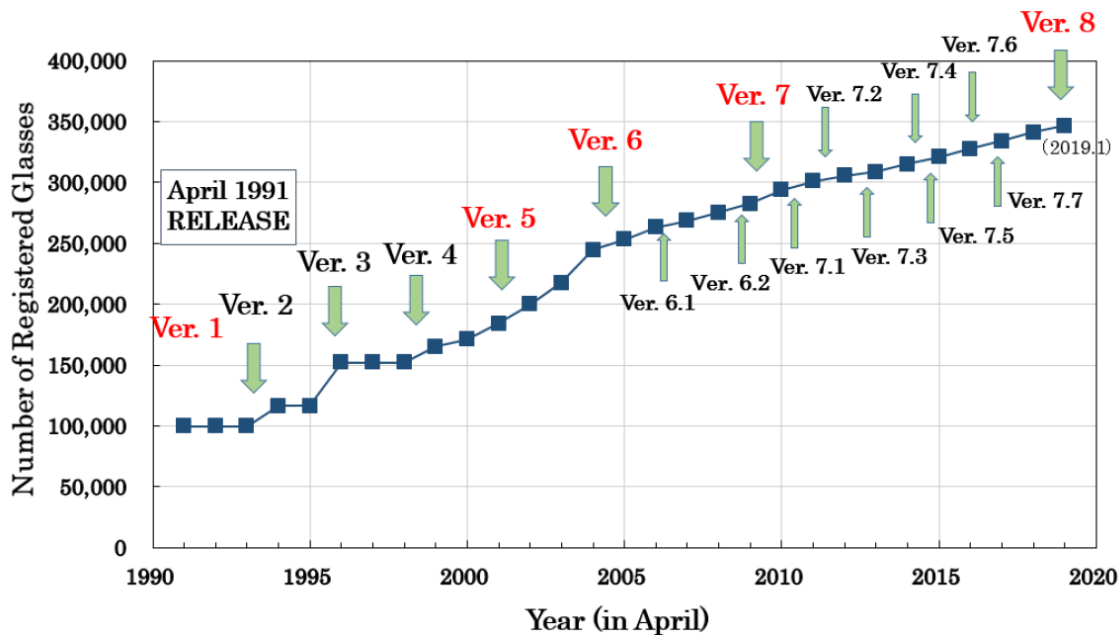
Property group: Viscosity

Property: log $\eta$ (T) Temperature: 1100 °C

Method: Priven-2000

On Top





INTERGLAD 8 : Search Structure Data

File Tools Help

State Glass

Composition

mass%  mol%  at%    Numerical

Main	Component	OR	Component	OR	Component	OR	Component	%min	%max
<input type="checkbox"/>	AND		SiO2	OR		OR			
<input type="checkbox"/>	AND		B2O3	OR		OR			
<input type="checkbox"/>	AND		Al2O3	OR		OR			
<input type="checkbox"/>	AND		Na2O	OR		OR			
<input type="checkbox"/>	AND		FeO	OR	Fe2O3	OR	Fe3O4		

% =< Total of Main Components

Structure

	Description	Element	Unit	Value Min	Value Max
AND					
AND					

Measurement Method

IR - Visible  Visible - UV  Lumines / IR - Visible  Lumines / Visible - UV  
 Raman  NMR  Moessbauer  XPS  ESR  X-ray  
 Neutron  XAFS  Calc (MO,MD,etc)  Others

Measurement Condition

Temperature   
Pressure

Data Source

AND

First Author

DB Site

INTERGLAD Data  
(  Server  Local )  
 User Data

Glass System

AND	
AND	

Glass ID  --

Max Data

INTERGLAD 8 : Glass Structure



# Available resources for nuclear glass property data

- Published reports from Pacific Northwest National Laboratory (PNNL)

**PNNL-2261, Rev. 1**  
09/2009

Pacific Northwest  
NATIONAL LABORATORY  
PNNL  
PNNL-2261, Rev. 1  
09/2009

**Glass Property Models and Constraints for Estimating the Glass to be Produced at Hanford by Implementing Current Advanced Glass Formulation Efforts**

JD Vienna DC Skorski  
DS Kim J Matyas

July 2013

U.S. DEPARTMENT OF  
**ENERGY**

Prepared for the U.S. Department of Energy  
under Contract DE-AC06-76RL01830

**Glass Property Data and Models for Estimating High-Level Waste Glass Volume**

JD Vienna  
A Fluegel  
DS Kim  
P Hema

October 2009

PNNL-14060

**Database and Interim Glass Property Models for Hanford HLW and LLW Glasses**

J. Vienna  
D. Kim  
P. Hema

PNNL-11037  
UC-816  
Project Technical Information

**Development of Models and Software for Liquidus Temperatures of Glasses of HWVP Products: Final Report**

P. R. Hrma P. Wu  
J. D. Vienna G. Eriksson  
A. D. Pelton S. Degtarev

March 1996

Prepared for the U.S. Department of Energy  
under Contract DE-AC06-76RLO 1830

Pacific Northwest National Laboratory  
Operated for the U.S. Department of Energy  
by Battelle Memorial Institute

**Battelle**  
**MASTER**

PNL-10359, VOL. 1  
UC-728  
2020

PROPERTY/COMPOSITION RELATIONSHIPS FOR HANFORD HIGH-LEVEL WASTE GLASSES MELTING AT 1150°C

Volume 1: Chapters 1 - 11

Principal Investigators and Authors  
P. R. Hrma  
G. F. Piepel

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D. K. Peeler  
M. H. Langowski

December 1994

Prepared for  
the U.S. Department of Energy  
under Contract DE-AC06-76RLO 1830

**MASTER**

## Big Data vs. Good Data



- Statistical modeling requires highly reliable experimental data
- Unfortunately the quality of published data differs from each other greatly

*O.V. Mazurin / Journal of Non-Crystalline Solids 351 (2005) 1103–1112*

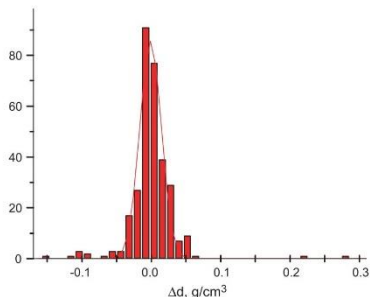


Fig. 2. A histogram of the differences between the values calculated by the equation describing the approximating curve in Fig. 1 and experimental values of density of sodium borate glasses. The solid line is the Gaussian approximation of the presented data.

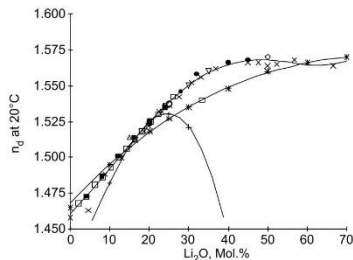


Fig. 8. Comparison of the curves approximating the composition dependencies of the refractive index for binary lithium borate glasses according to the data published by Conzone et al. [9] and Lorosch et al. [14] with the curve approximating the results for sets of data taken from papers published earlier [10–13]. (+): data by Conzone; (\*): data by Lorosch.

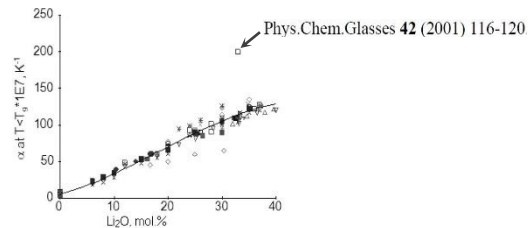


Fig. 2. Thermal expansion coefficient of solid lithium silicate glasses

## Big Data vs. Good Data



- Statistical modeling requires highly reliable experimental data
- Unfortunately the quality of published data differs from each other greatly

*O.V. Mazurin / Journal of Non-Crystalline Solids 351 (2005) 1103–1112*

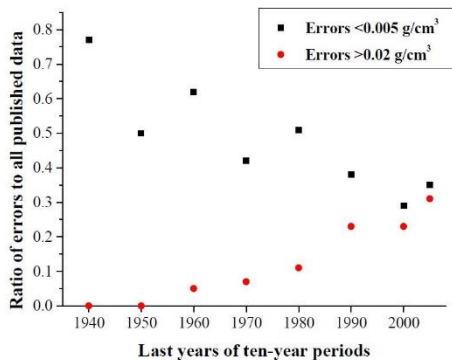


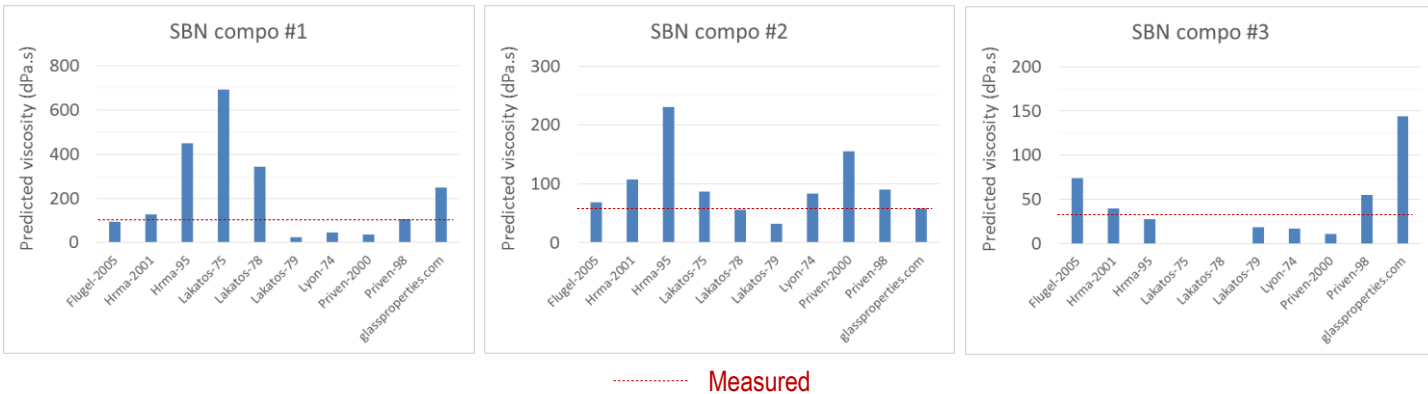
Table 3. Changes in number of co-authors of papers

Year	1930	1950	1975	2000
Average number of co-authors	1.6	1.6	2.8	3.1
Maximal number of co-authors	4	4	9	10

# Viscosity prediction

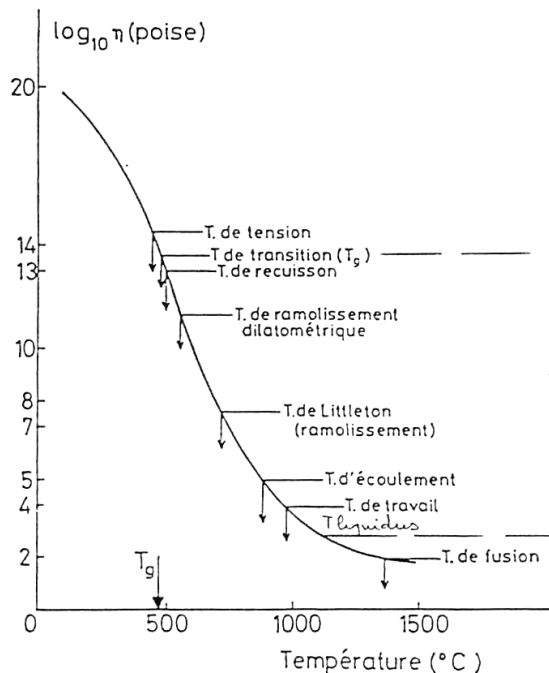
Viscosity is a property which is difficult to calculate

- Example : Prediction using well-known literature models (from SciGlass) on simple SBN glass (1200°C)



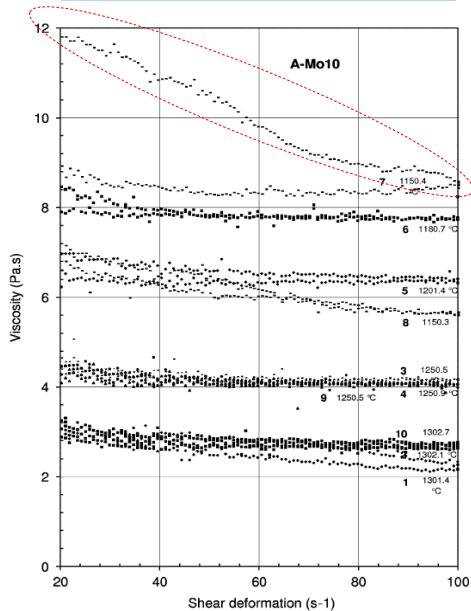
- Motivation for developing internal prediction tool

- Range of viscosity values is very wide vs temperature and vs composition



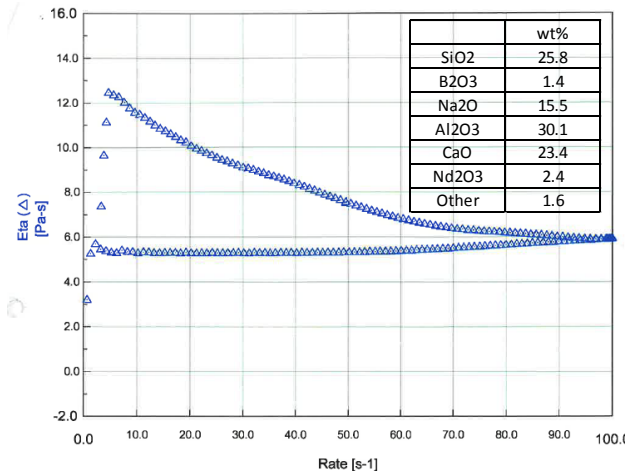
- Viscosity temperature dependence is highly sensitive to phase separation and crystallization

## Phase separation



Oxide mol%	AMo10 batch no. 5052
SiO <sub>2</sub>	46.5
Na <sub>2</sub> O	11.0
B <sub>2</sub> O <sub>3</sub>	14.4
Li <sub>2</sub> O	0.2
CaO	7.9
MoO <sub>3</sub>	5.1
P <sub>2</sub> O <sub>5</sub>	1.6
Al <sub>2</sub> O <sub>3</sub>	5.4
ZnO	5.4
ZrO <sub>2</sub>	2.0
Nd <sub>2</sub> O <sub>3</sub>	0.2
Minors	0.3
Sum	100.0

## Crystallization



## Our viscosity database

- Internal CEA database  
(mainly borosilicate glass)
- SciGlass and InterGlad Information Systems  
(all types of glass)
- Pacific Northwest National Laboratory database  
(borosilicate glass) *Grateful acknowledgement to J. Vienna from PNNL*
- About 16,000 data of composition and viscosity
- Temperature range: 900-1500°C



# General database



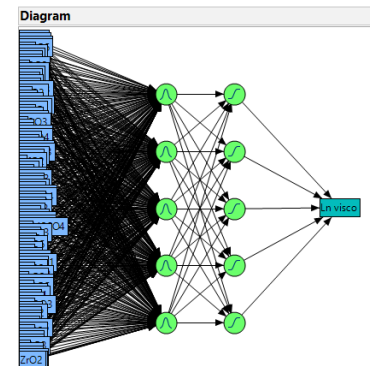
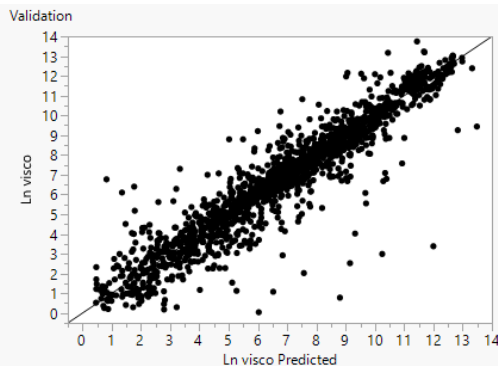
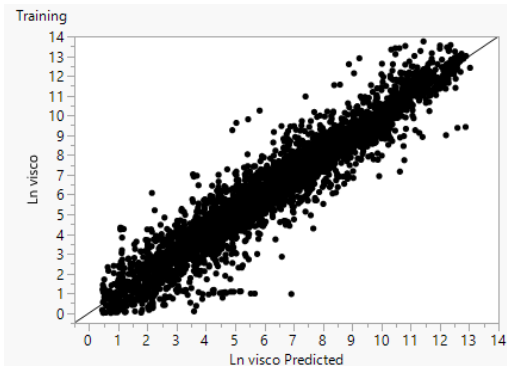
Photo courtesy of [www.sciencesetavenir.fr](http://www.sciencesetavenir.fr)

## What we learnt from the past

- We applied several machine learning techniques to build viscosity models (neural nets, boosted tree, random forest,...)
- The **whole database** (about 16,000 data) was considered and partitioned into training set and validation set
- But at the end, **no statistical model** with acceptable predictive capability was found to predict the viscosity



- NN are unable to predict efficiently glass viscosity on big database...



Training	
Ln visco	
Measures	Value
RSquare	0.9287269
RMSE	0.7518628
Mean Abs Dev	0.496624
-LogLikelihood	6435.0916
SSE	3208.6293
Sum Freq	5676

Validation	
Ln visco	
Measures	Value
RSquare	0.8822247
RMSE	0.9682362
Mean Abs Dev	0.5912263
-LogLikelihood	2545.9066
SSE	1721.2158
Sum Freq	1836

## *Dynamic and automatic* dataset for model training

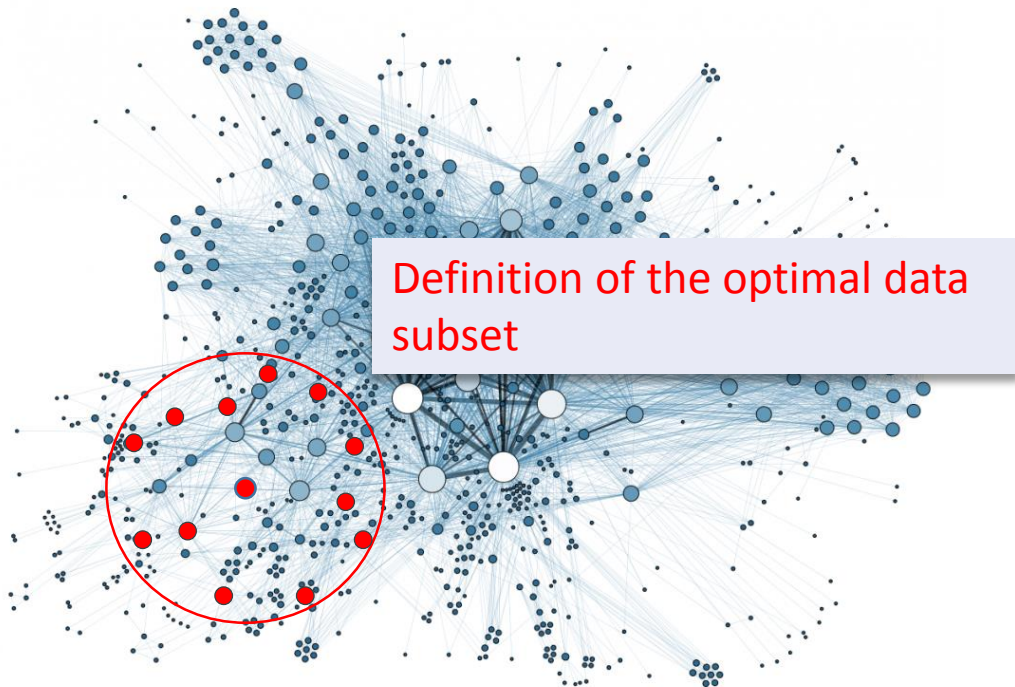
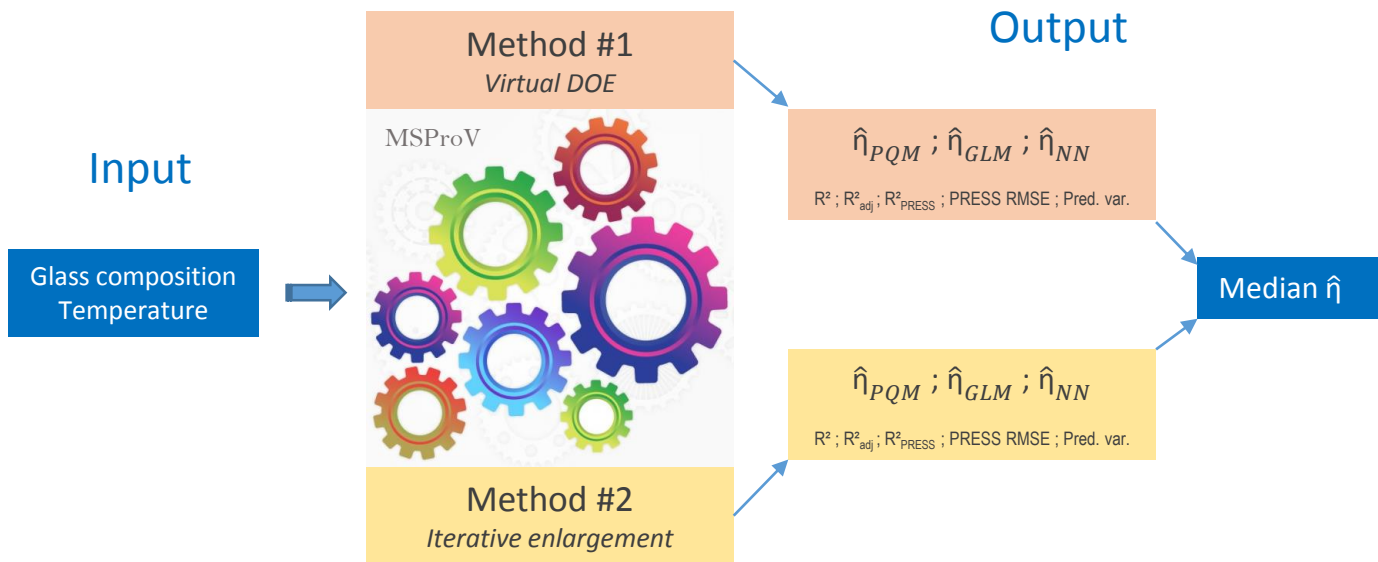


Photo courtesy of [www.sciencesetavenir.fr](http://www.sciencesetavenir.fr)

## MSProV schematic diagram



Algorithms coded in JSL language (JMP software from SAS Institute)

## Key parameters

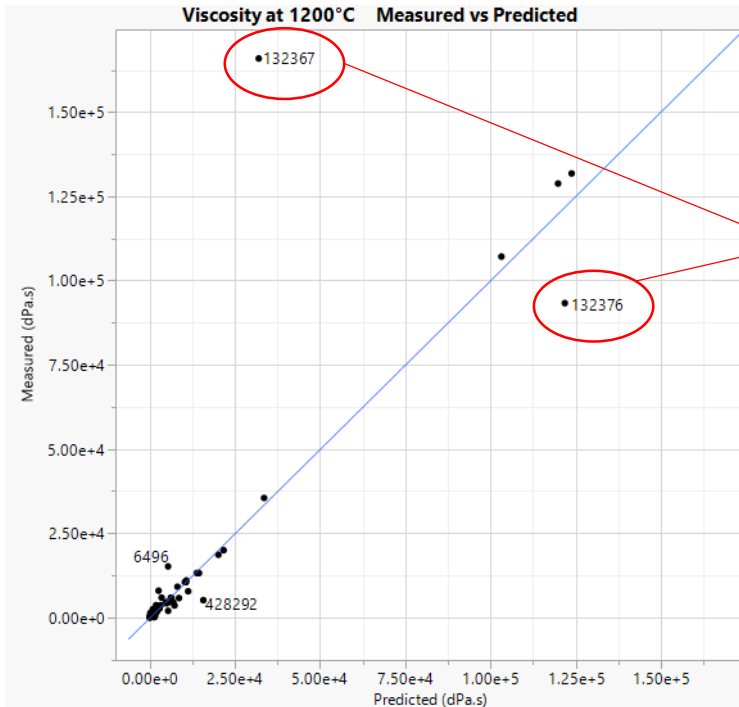
- Inputs from glass science experts on the nature and roles of oxides
- These inputs were implemented in MSProV algorithms
  - weights and type of distance calculation between *similar* glasses
- Origin and reliability of the data, viscosity measurement device

## Results for viscosity prediction

- MSProV global database for viscosity prediction contains 15,569 glasses (all silica glass)
- 230 glasses extracted for testing MSProV capability to predict viscosity at 1200°C

Viscosity prediction relative error	Borosilicate glass for nuclear waste	Sodo alumino silica glass	Overall
	N=73	N=55	N=230
Quantile 50% (median)	11%	18%	17%
Quantile 75%	19%	35%	34%
Quantile 90%	37%	73%	77%

## Results for viscosity prediction



Num	132367	Num	132376
Origin	SCIGLASS	Origin	SCIGLASS
Year	1994	Year	1994
	%wt		%wt
Al <sub>2</sub> O <sub>3</sub>	12,50	Al <sub>2</sub> O <sub>3</sub>	19,01
B <sub>2</sub> O <sub>3</sub>	7,50	B <sub>2</sub> O <sub>3</sub>	6,79
BaO	20,00	BaO	9,43
CaO	2,50	CaO	4,11
SiO <sub>2</sub>	57,50	MgO	1,42
		SiO <sub>2</sub>	57,35
		SrO	1,86
Visc. exp. (dPa.s) 1200°C	165 959	Visc. exp. (dPa.s) 1200°C	93 325

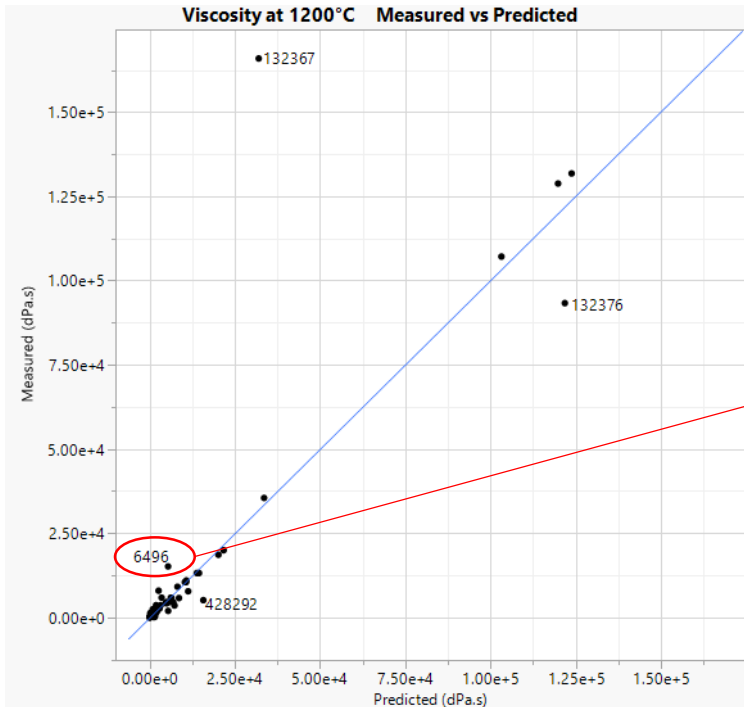
SciGlass reference: US Patent 5374595

Experimental error not mentioned

High %Al<sub>2</sub>O<sub>3</sub> and/or %BaO



## Results for viscosity prediction



<b>Num</b>	<b>6496</b>
Origin	SCIGLASS
Year	1968
	%wt
Al <sub>2</sub> O <sub>3</sub>	21,10
B <sub>2</sub> O <sub>3</sub>	7,40
BaO	3,50
CaO	13,50
SiO <sub>2</sub>	54,50
Visc. exp. (dPa.s) 1200°C	15 136

Experimental device (1968)

High %Al<sub>2</sub>O<sub>3</sub>

# Tg prediction

## Prediction results

- MSProV global database for Tg prediction contains 20,201 glasses (all silica glass)
- 100 glasses extracted for testing MSProV capability

Tg prediction error	Borosilicate glass		Sodo aluminosilica glass		Overall	
	N=80		N=20		N=100	
	Rel.	Abs.	Rel.	Abs.	Rel.	Abs.
Quantile 50% (median)	1,4%	7°C	1,7%	10°C	1,5%	7°C
Quantile 75%	2,8%	13°C	3,2%	17°C	2,9%	14°C
Quantile 90%	5,1%	29°C	4,2%	19°C	4,7%	26°C

# General conclusion

- When glass composition is too complex, properties can not be predicted from theoretical models
- In this case, statistical modeling using empirical data is an alternative way to predict glass properties
- Excellent predictive models can be obtained by using a Design of Experiments methodology, on small domains of composition
- Glass property information systems containing published data are commercially available
- Machine Learning has seen growing application in material property determination on big data sets
- Several physical and chemical glass properties can be well predicted by using Neural Nets

# THANK YOU FOR YOUR ATTENTION



## Acknowledgments

- Glass elaboration and characterization teams, R&D Scientist from CEA Marcoule

V. Ansault, T. Blisson, M. Chartier, V. Debono, V. Lemaitre, S. Mure, B. Penelon, J. Renard, C. Vallat, J.L. Dussossoy, M. Fournier, I. Giboire, I. Hugon, A. Laplace, M. Neyret, O. Pinet, E. Régnier, S. Schuller, S. Vaubaillon, F. Bart, J. Lacombe, C. Ladirat, S. Gin

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- Pacific Northwest National Laboratory

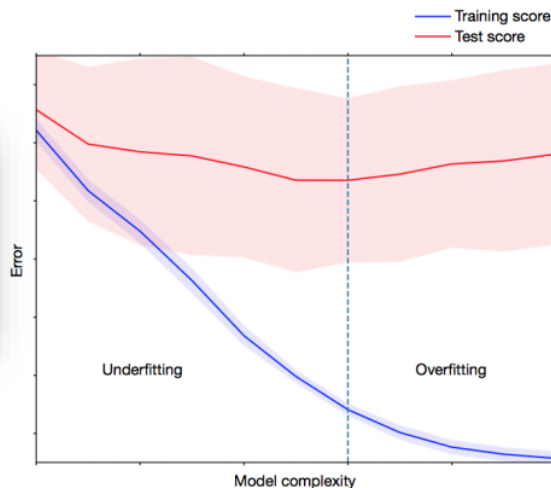
J. Vienna

- JMP, SAS Institute

B. Jones

## Advice when building predictive models

- Beware of overfitting (principle of parsimony)



from K. T. Butler et al. *Machine learning for molecular and materials science*  
Nature, 2018

## SBN1

Component	Mol. %	Wt %
B <sub>2</sub> O <sub>3</sub>	18.04	20.23
SiO <sub>2</sub>	67.73	65.56
Na <sub>2</sub> O	14.23	14.21

## SBN2

Component	Mol. %	Wt %
B <sub>2</sub> O <sub>3</sub>	8.467	9.61
SiO <sub>2</sub>	67.73	66.34
Na <sub>2</sub> O	23.8	24.05

## SBN3

Component	Mol. %	Wt %
B <sub>2</sub> O <sub>3</sub>	19.57	21.86
SiO <sub>2</sub>	60.86	58.68
Na <sub>2</sub> O	19.57	19.46

**Chemical composition range of R7T7 glasses produced in the AREVA - La Hague plant workshops**

Oxides	Specified interval for the industry (wt%)		Average composition of industrial glasses (wt%)
	min	max	
SiO <sub>2</sub>	42.4	51.7	45.6
B <sub>2</sub> O <sub>3</sub>	12.4	16.5	14.1
Al <sub>2</sub> O <sub>3</sub>	3.6	6.6	4.7
Na <sub>2</sub> O	8.1	11.0	9.9
CaO	3.5	4.8	4.0
Fe <sub>2</sub> O <sub>3</sub>	< 4.5		1.1
NiO	< 0.5		0.1
Cr <sub>2</sub> O <sub>3</sub>	< 0.6		0.1
P <sub>2</sub> O <sub>5</sub>	< 1.0		0.2
Li <sub>2</sub> O	1.6	2.4	2.0
ZnO	2.2	2.8	2.5
Oxides (PF + Zr + actinides)	7.5	18.5	17.0
Fines suspension			
Actinide oxides			0.6